



4. Model fitting

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Seattle, June 2011

Regression commands

Two of the most important R commands;

- `lm()`: fits **L**inear **M**odels
- `glm()`: fits **G**eneralized **L**inear **M**odels

(If you've used SAS, its `glm` is **not** the same as R's)

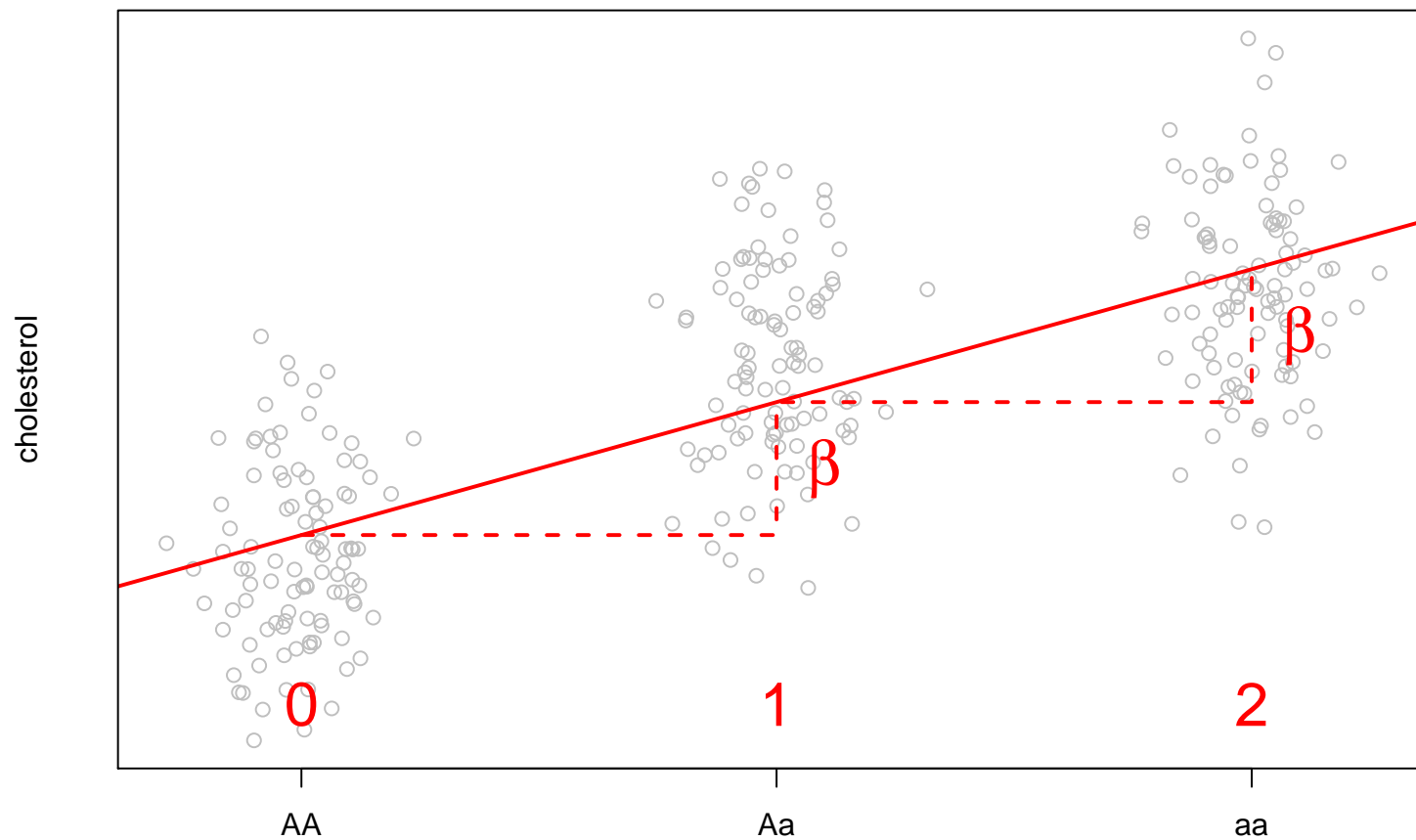
'Linear Regression' and 'Logistic Regression' are special cases.

There's a lot to learn here – entire graduate courses! – so the help files are huge. How are `lm()`, `glm()` used in genetics?

Linear regression, with SNPs

Many analyses fit the 'additive model'

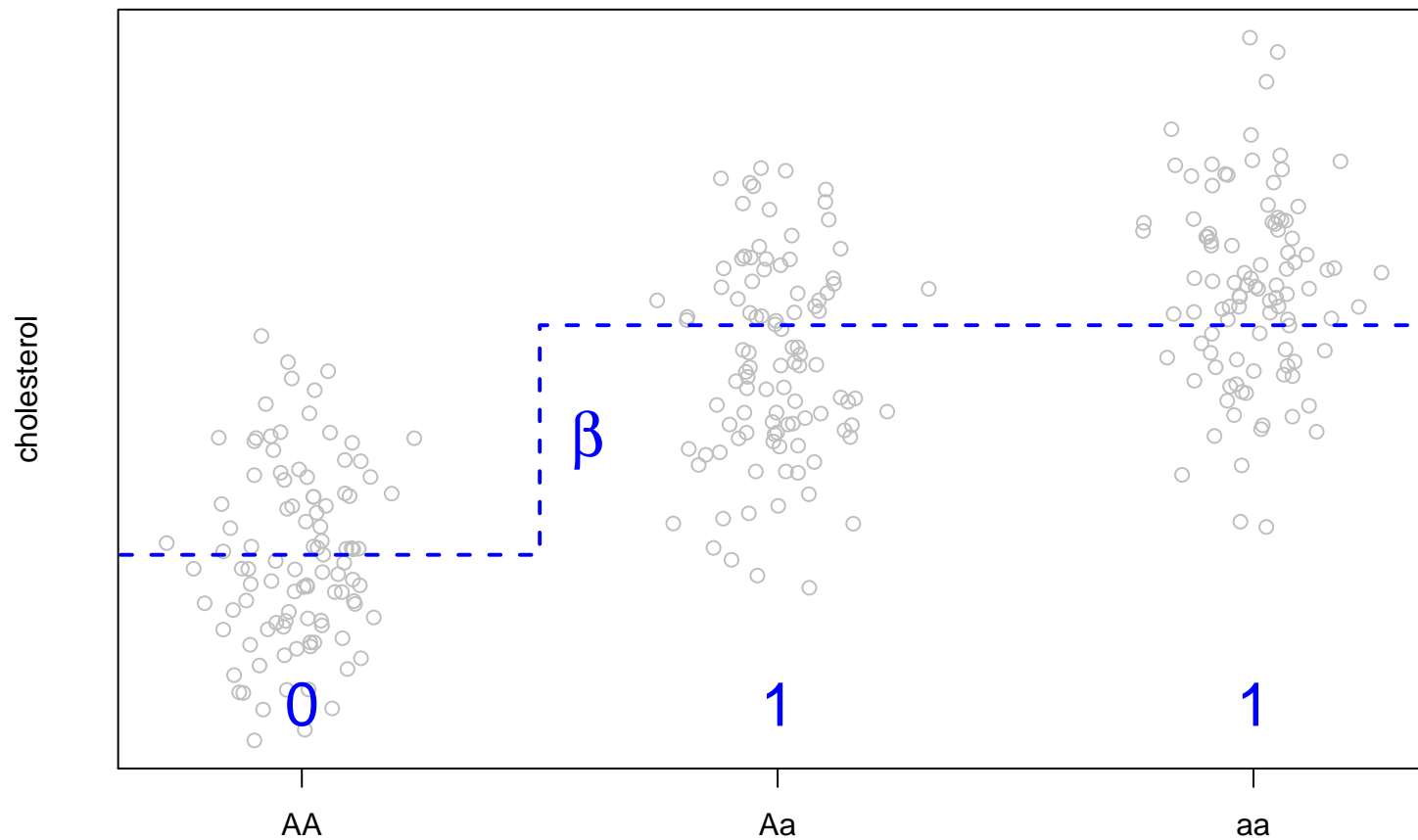
$$y = \beta_0 + \beta \times \# \text{minor alleles}$$



Linear regression, with SNPs

An alternative is the 'dominant model';

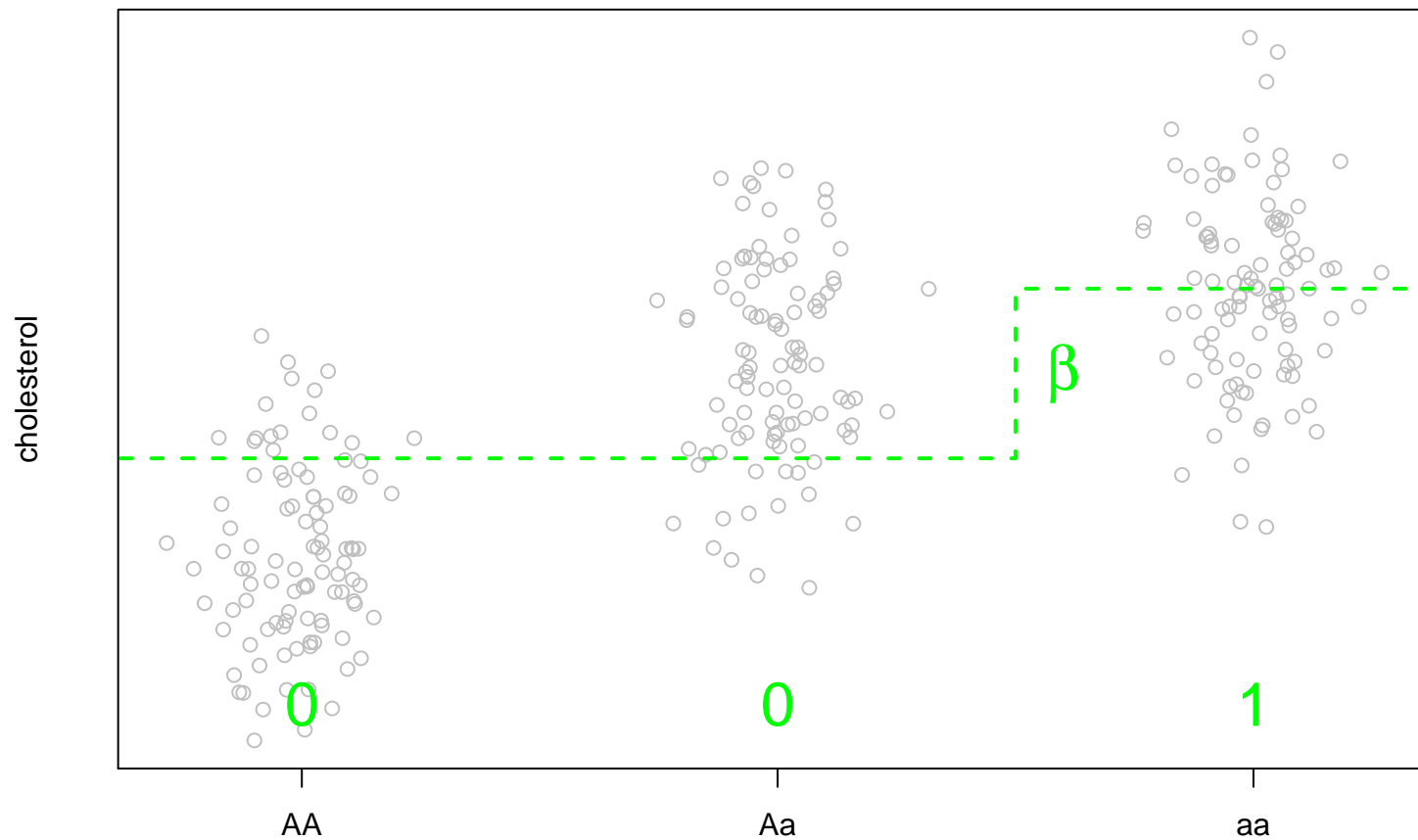
$$y = \beta_0 + \beta \times (G \neq AA)$$



Linear regression, with SNPs

or the 'recessive model';

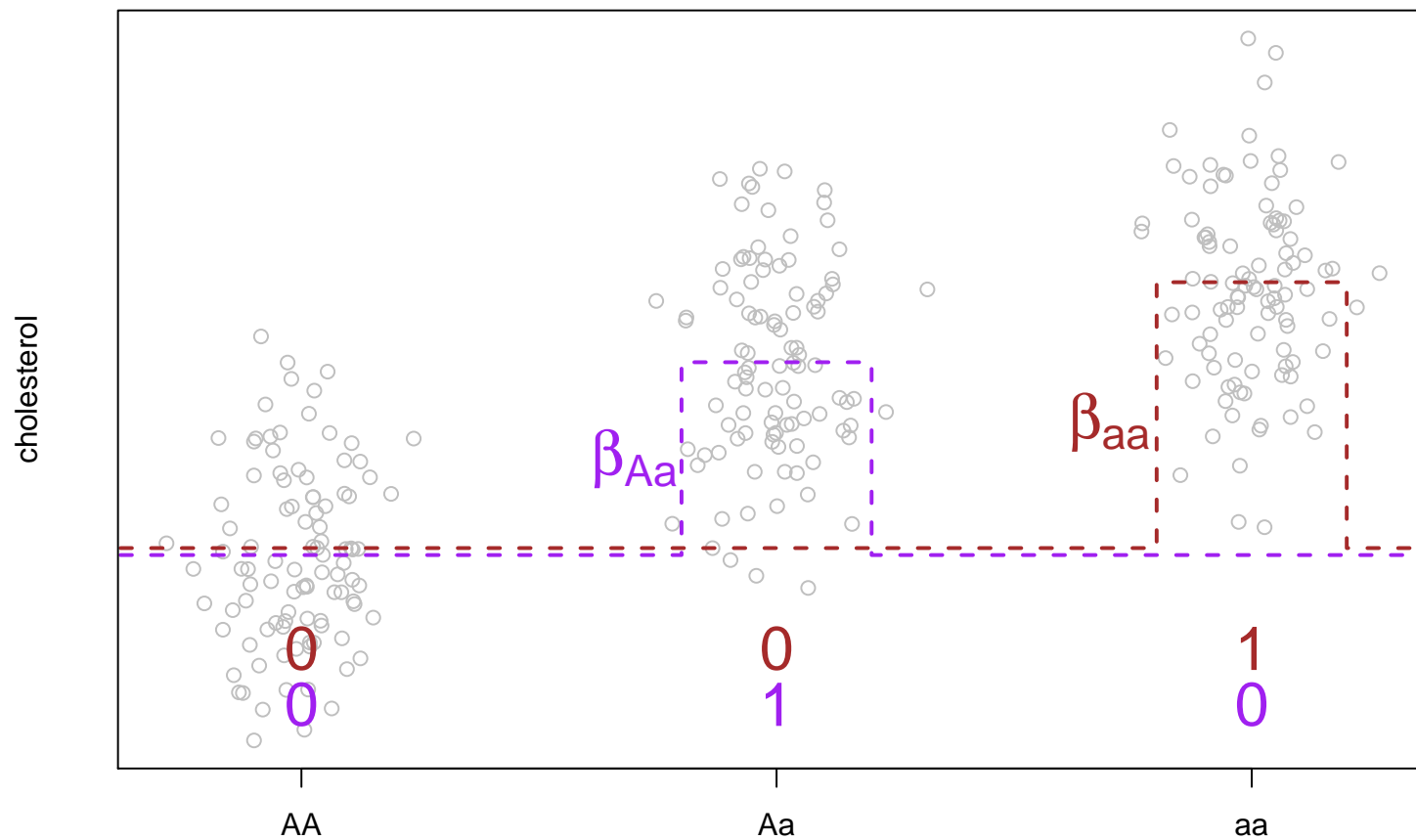
$$y = \beta_0 + \beta \times (G == AA)$$



Linear regression, with SNPs

Finally, the 'two degrees of freedom model';

$$y = \beta_0 + \beta_{Aa} \times (G == Aa) + \beta_{aa} \times (G == aa)$$



Use of `lm()` in genetics

The `lm()` command fits all of these, in the same way. Formally,

```
lm(outcome ~ genetic.predictor, [...] )
```

estimates the association between outcome and predictor

The **optional** arguments [...] might be

- `data = my.data` – your dataset
- `subset = race=="CEPH"` – use partial data
- `weights =` – for advanced analyses

Use of `lm()` in genetics

How to make the `genetic.predictor` variable? Suppose you had genotypes stored as character strings ("AA"/"Aa"/"aa") in a vector `g`. You might use these commands;

Chosen Model	Command to define variable
Additive	<code>genetic.predictor <- (g=="Aa") + 2*(g=="aa")</code>
Dominant	<code>genetic.predictor <- (g=="Aa") (g=="aa")</code>
Recessive	<code>genetic.predictor <- g=="aa"</code>
2 degs of freedom	<code>genetic.predictor <- factor(g)</code>

When R meets FALSE or TRUE in a 'math' setting, it will **coerce** them to be zero or one. So `1 + 2*TRUE` is 3, `TRUE + 2*FALSE` is 1, etc. Using `factor()` sets up several binary variables

- There are *many* other ways to do this!
Use `table(g, genetic.predictor)` to check your method
- Often, genotypes may be stored as 0/1/2. This is easier to work with in R – but makes it harder to decide if A/C/G/T is the minor allele, or risk allele.

lm(): Estimates, Intervals, p-values

lm() produces **point estimates** for your model;

```
> genetic.predictor <- (g=="Aa") + 2*(g=="aa") #using additive model
> my.lm <- lm( cholesterol ~ genetic.predictor )
> my.lm
```

Call:

```
lm(formula = cholesterol ~ genetic.predictor)
```

Coefficients:

(Intercept)	predictor
0.2104	0.9507

– also available via `my.lm$coefficients` or `coef(my.lm)`.

The coefficients in the output tell you the **additive increase** in outcome associated with a **one-unit** difference in the genetic predictor.

The coefficient for predictor is in units of cholesterol per 'a' allele

lm(): Estimates, Intervals, p-values

You will also want **confidence intervals**;

```
> confint.default(my.lm)
                2.5 %    97.5 %
(Intercept) 0.08391672 0.3368275
predictor    0.85279147 1.0486953
```

Remember to **round these numbers** to an appropriate number of significant figures! (2 or 3 is usually enough)

We are **seldom** interested in the Intercept

lm(): Estimates, Intervals, p-values

Two-sided **p-values** are also available;

```
> summary(my.lm)
```

```
Coefficients:
```

```
              Estimate Std. Error t value Pr(>|t|)
(Intercept)  0.21037    0.06426   3.274  0.00119 **
predictor    0.95074    0.04977  19.101 < 2e-16 ***
```

```
---
```

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

- In this data, we have **strong evidence** of an **additive effect** of the minor allele on cholesterol
- `summary(my.lm)` gives **many** other details – ignore for now
- Confidence intervals are just $\text{Estimate} \pm 2 \times \text{Std.Error}$

Use of `glm()` in genetics

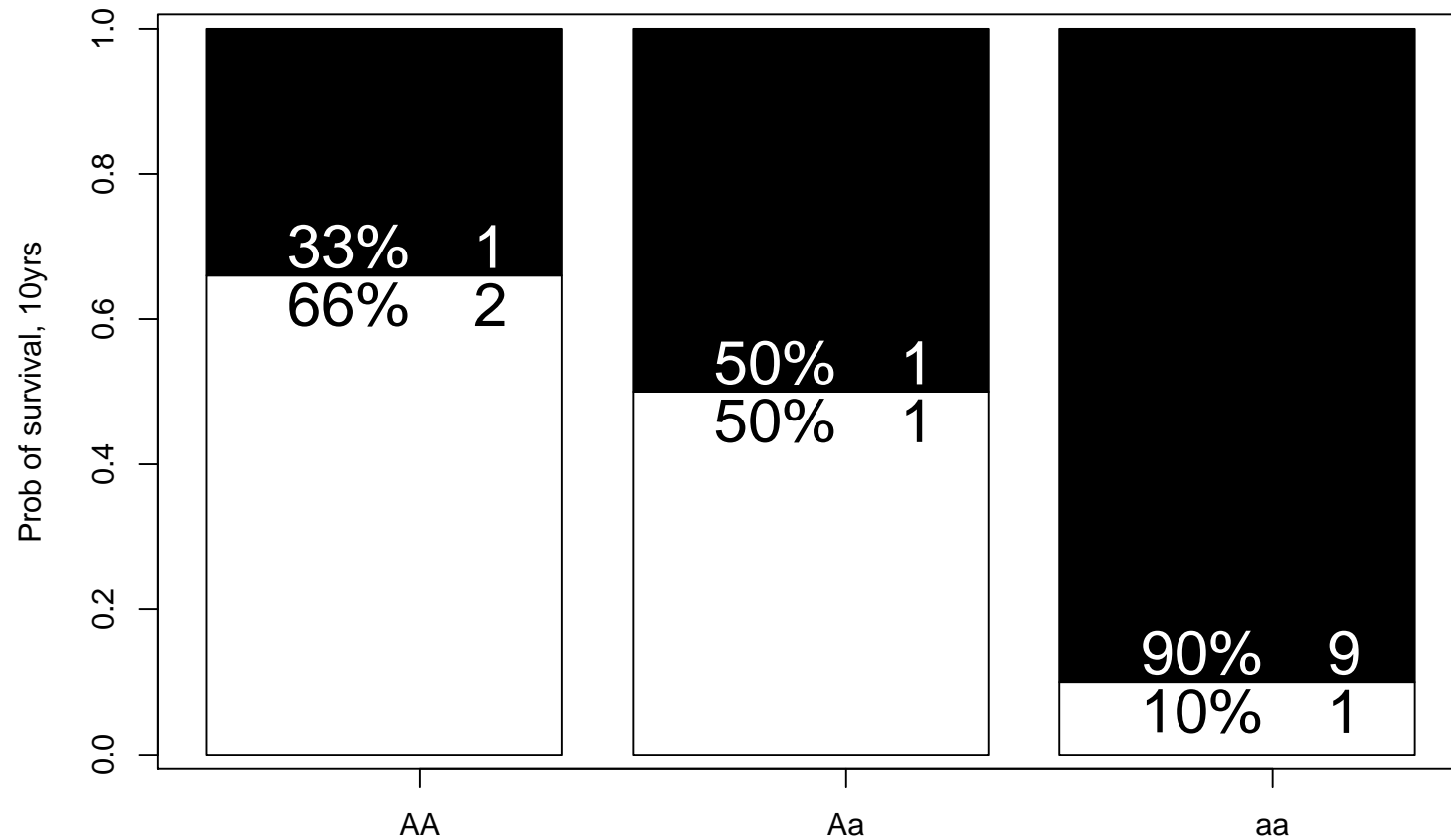
Logistic regression is the 'default' analysis for **binary outcomes**

Outcome	Type	Regression	Scale
Cholesterol Blood Pressure BMI	Continuous	Linear	Difference in Outcome
Death Stroke BMI>30	Binary	Logistic	Ratio of odds

What are **odds**? Really just **probability**...

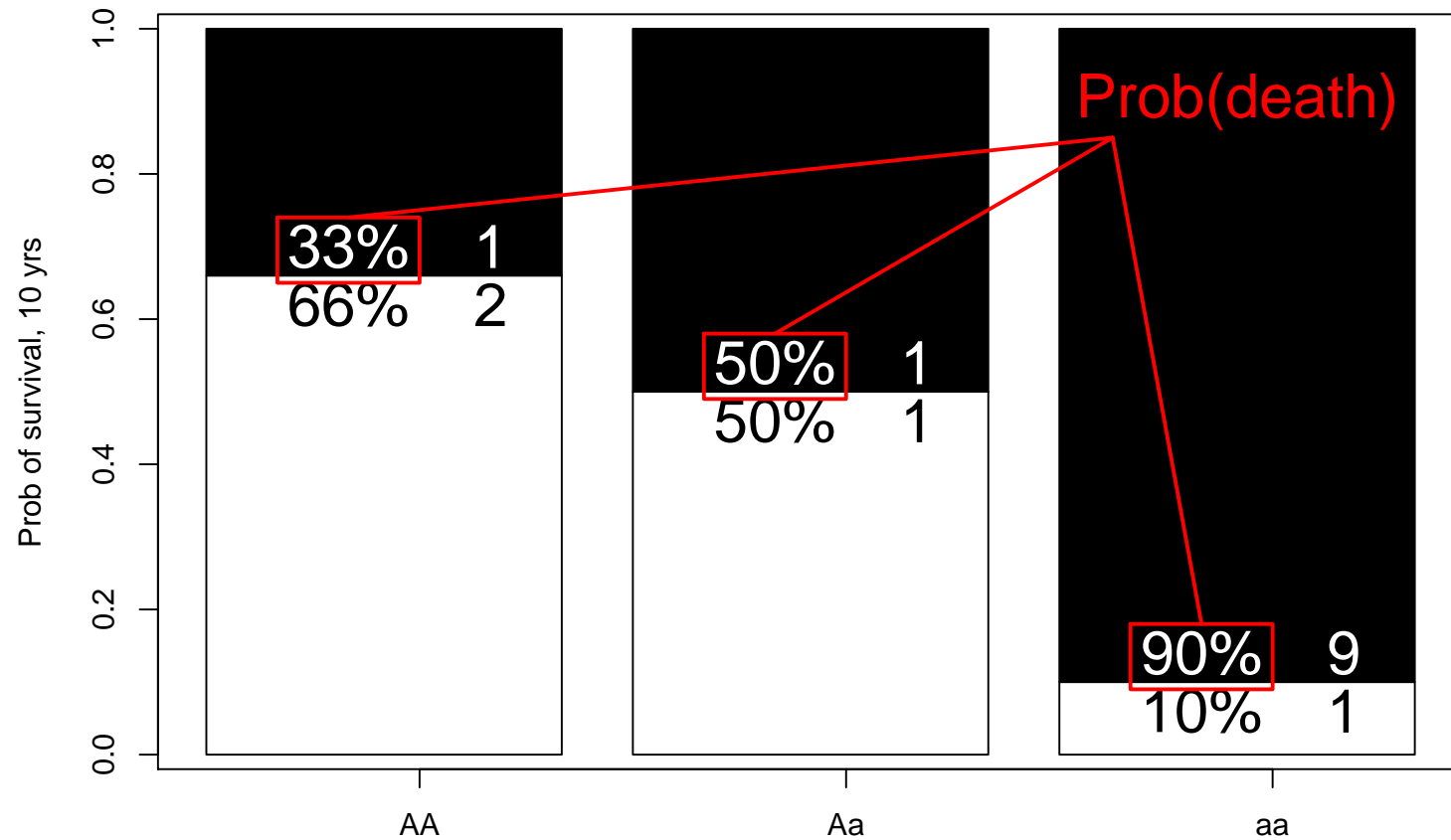
Use of `glm()` in genetics

Odds are a [gambling-friendly] measure of chance;



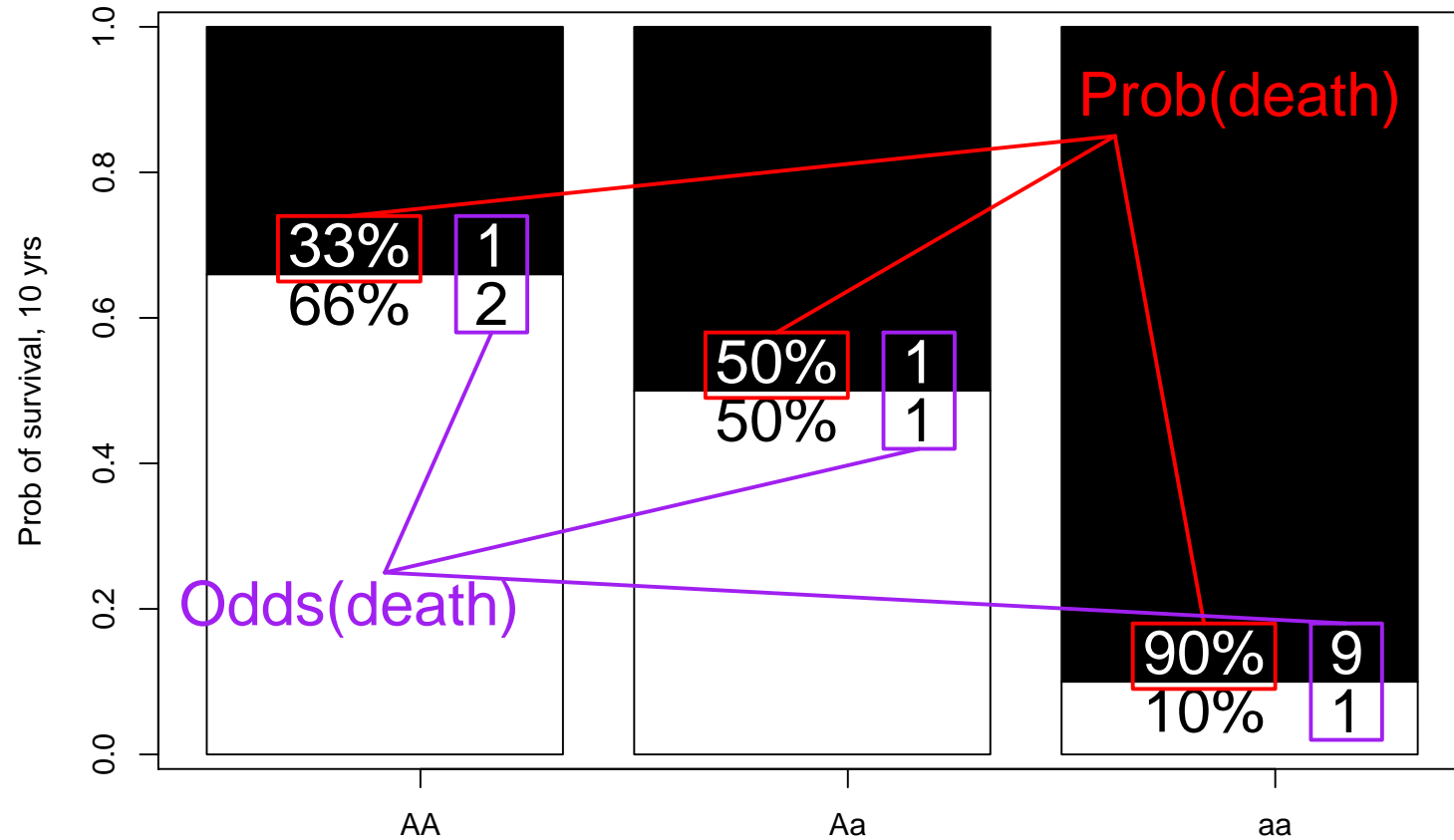
Use of `glm()` in genetics

Odds are a [gambling-friendly] measure of chance;



Use of `glm()` in genetics

Odds are a [gambling-friendly] measure of chance;



– so what are **odds ratios**?

Use of glm() in genetics

Using the data from slide 4.12 ;

```
> genpred2 <- factor(g) # the 2df model
> glm1 <- glm( dead10yrs ~ genpred2, family=binomial)
> coef(glm1)
      pred2Aa      pred2aa
      0.6931      2.8904
```

- These are **log odds ratio** estimates; to transform to OR, use $e^{0.6931} = 2$, $e^{2.8904} = 18$
- They are given **relative to the baseline group** – ‘AA’ in this case
- Don’t forget the `family=binomial` argument!

Use of `glm()` in genetics

Confidence intervals, p-values as with `lm()`, **for the log odds ratios**;

```
> confint.default(glm1)
```

	2.5 %	97.5 %
genpred2Aa	0.1201986	1.2660957
genpred2aa	2.1148912	3.6658523

```
> summary(glm1)
```

	Estimate	Std. Error	z value	Pr(> z)
genpred2Aa	0.6931	0.2923	2.371	0.01773 *
genpred2aa	2.8904	0.3957	7.305	2.77e-13 ***

Use `exp()` to get odds ratio estimates, intervals; p-values are **scale-independent**

The formula syntax

We saw `lm(y ~ genetic.predictor)` and `glm(y ~ genpred2)`. To see how phenotype depends on *several* covariates, we specify e.g.

$$y \sim \text{genotype.pred} + \text{age} + \text{sex}$$

– formally, this gives *multivariate regression*; the `genotype.pred` coefficients reflect the genotype effects *adjusted for age and sex*

- Separate covariates with '+'. This is *not* addition!
- For now, make predictor variables first, then do regression. It's possible to do everything in one step, but use of e.g. '+' will confuse R – unless you're careful.
- For keen people; in the formula syntax, * indicates that interactions should be fitted, I() insulates mathematical operations, -1 removes the intercept... see `?formula`
- For *very* keen people; `vcovHC()` in the `sandwich` package provides 'robust' standard errors; `coefTest()` in the `lmtest` package can use them to give 'robust' tests.