

# fastSKAT:

Sequence Kernel Association  
Tests for large sets of markers

...and applications for analyzing LDL cholesterol  
in whole-genome sequencing data

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TOPMed Data  
Co-ordinating Center





# What is SKAT?

- SKAT (Wu, Lee et al, 2011) tests association between a trait and **multiple** variants; maintains power well across many possible 'signals'
- For M variants, N subjects, takes  $MN \times \min(M,N)$  steps
- In large WGS work (TOPMed, CHARGE-S, etc) this **limits** SKAT analysis – too slow and/or insufficient CPU time, even with parallel processing



# How to do SKAT tests faster?

SKAT compares statistic to reference – a sum of  $\min(M,N)$  terms;

$$\lambda_1 \chi_1^2 + \lambda_2 \chi_1^2 + \lambda_3 \chi_1^2 + \lambda_4 \chi_1^2 + \lambda_5 \chi_1^2 + \lambda_6 \chi_1^2 + \lambda_7 \chi_1^2 + \dots + \lambda_{\min(M,N)} \chi_1^2$$

Approximate this by;

from Stochastic SVD

Satterthwaite approximation

$$\lambda_1 \chi_1^2 + \lambda_2 \chi_1^2 + \lambda_3 \chi_1^2 + \lambda_4 \chi_1^2 + \dots + \lambda_{100} \chi_1^2 + \text{remainder term}$$

Or even less, if genotype data sparse

Instead of  $MN \times \min(M,N)$  time, takes  $MN \times 100$  time: **fast**

# Stochastic SVD?



$$\lambda_1, \lambda_2, \lambda_3, \dots, \lambda_{100}$$



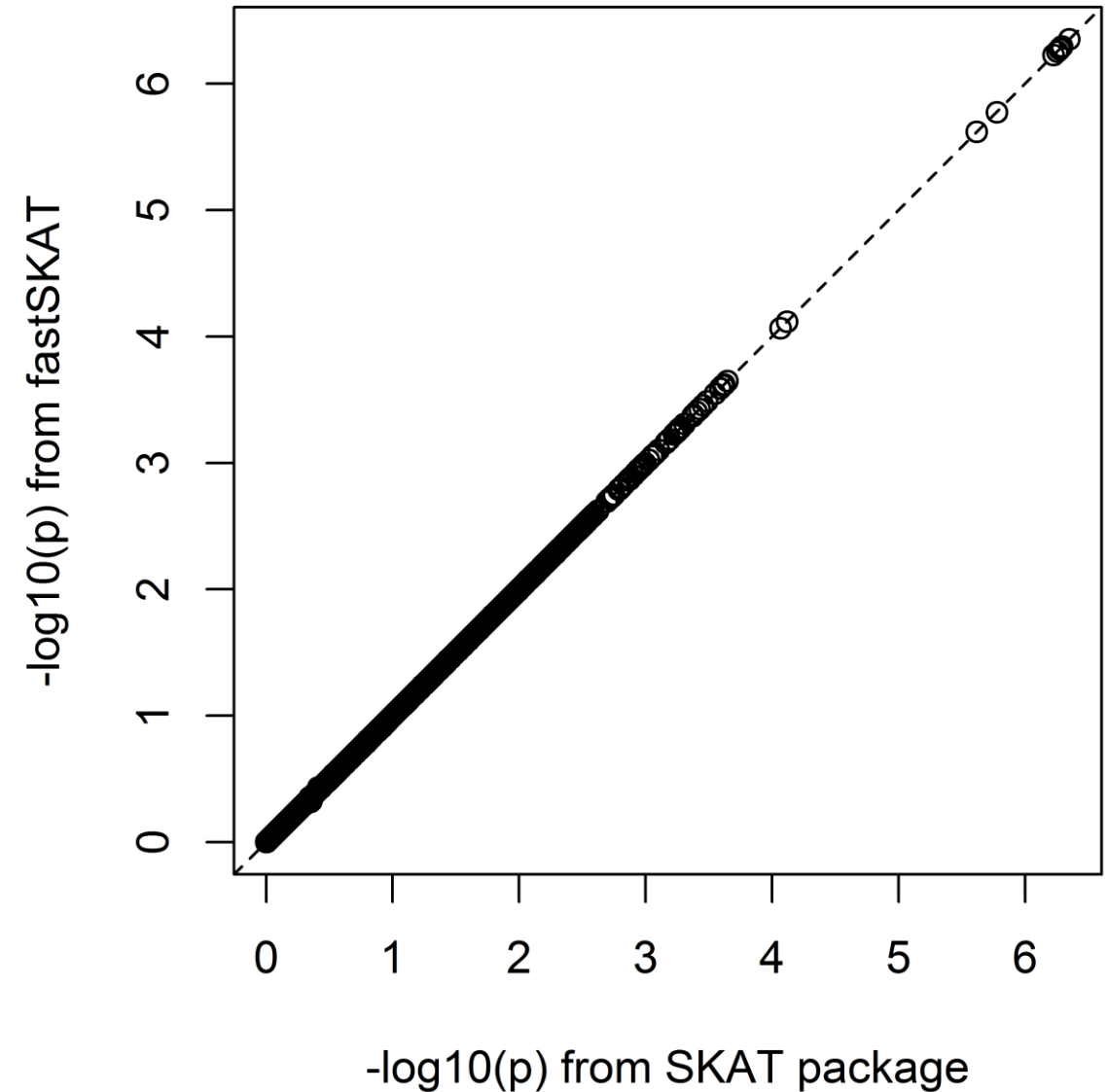
Galinsky et al (2016, AJHG) use it for fastPCA; **fastSKAT** does inference



Does it work?

- Yes, as well as SKAT does;

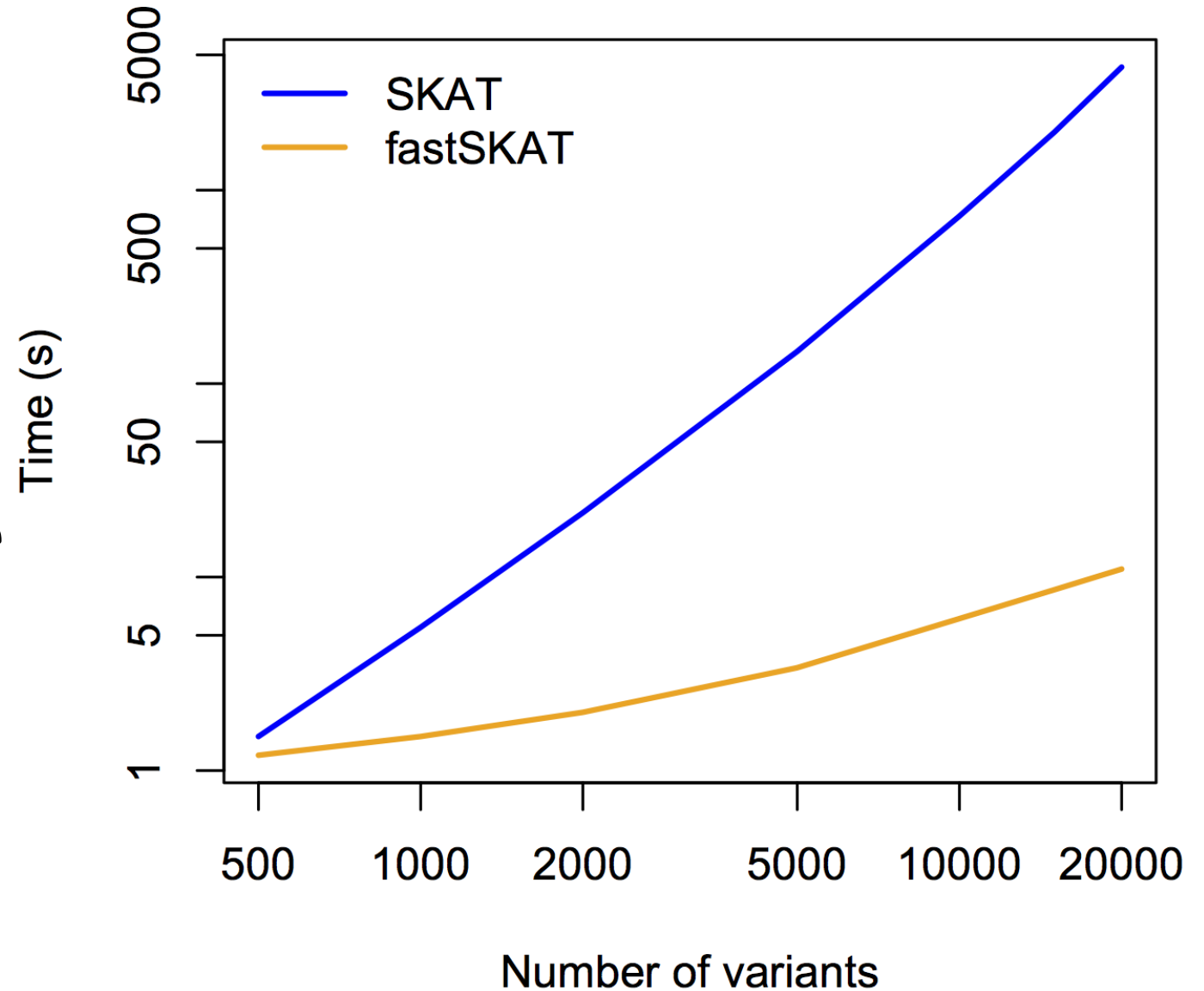
LDL-C; 17259 gene regions  
with 1k-7k variants within  
 $\pm 50$  kb





# How much faster?

- For  $N=5000$ ;
- Exploits sparse genotypes, here
- 3 orders of magnitude faster, for large  $M$





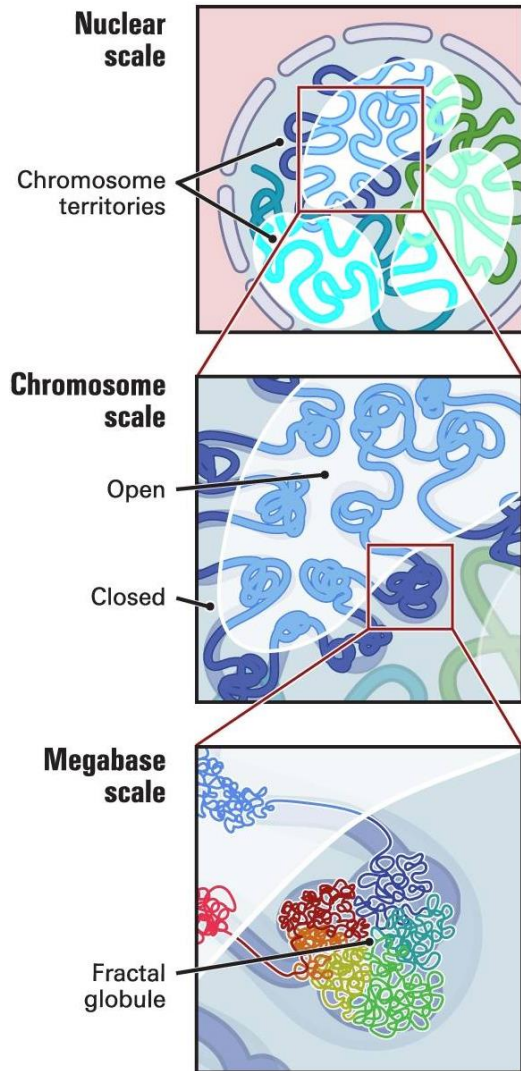
# What new stuff can it do?

Investigate large variant sets (10k-100k) defined by structural or functional criteria

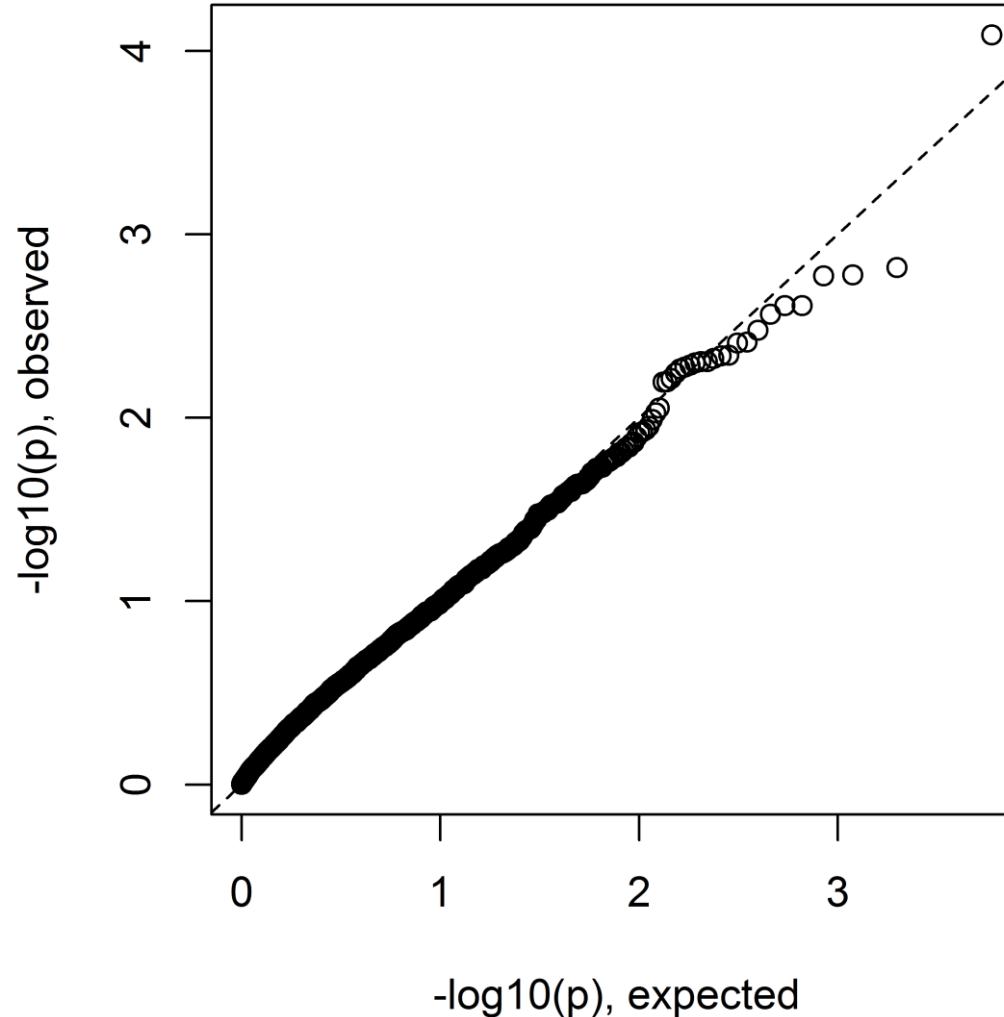
- Topologically Associating Domains
- Histone marks



# Topologically Associating Domains



Lieberman-Aiden et al (2005, Science)

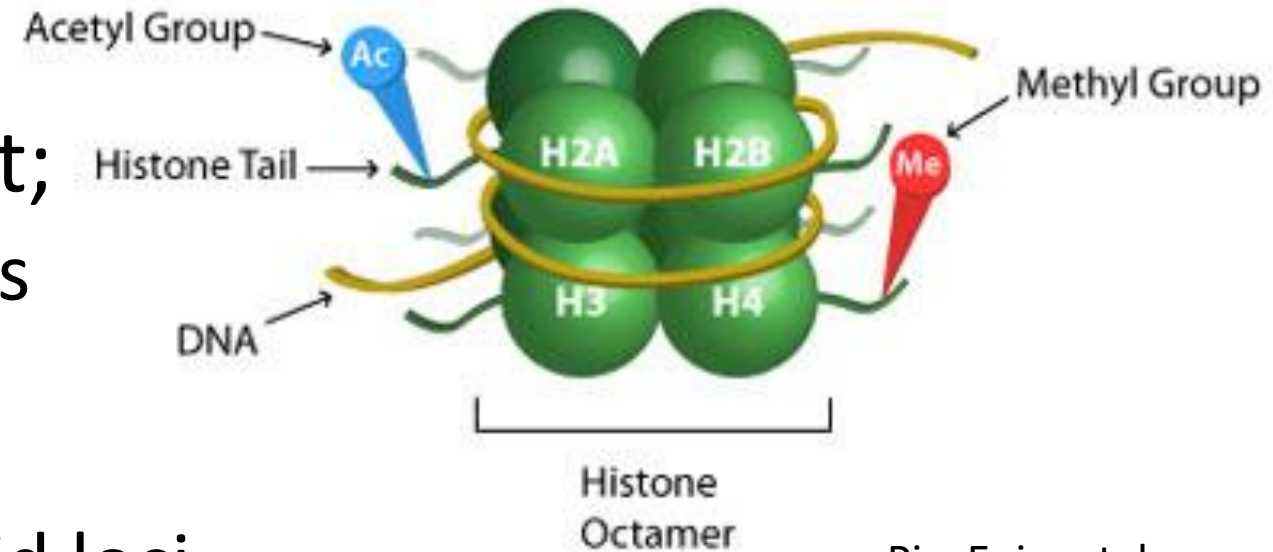


- average 1Mb, 10k-20k variants
- top hit contains APOE, not quite significant
- **fastSKAT** is 2400 times faster



# Histone marks

- Analyzed rare variants that;
  - fall within regulatory marks of six different histones annotated in adult liver
  - within 500Kb of known lipid loci
  - **aggregated over a whole chromosome** (up to M=100k)
- Control: random variants in same regions
- Two signals ( $p=10^{-5}$ ) on chromosome 19 (likely APOE)



Pic: Epigentek.com



# Can **fastSKAT** handle...

- Binary data? Yes
- Survival data? Not yet
- Parallel processing? Will be straightforward
- Family data from pedigrees? Yes with mixed models (GMMAT)
- Empirical kinship matrices? Not yet
  
- Software: [github.com/tslumley/bigQF](https://github.com/tslumley/bigQF)
- Manuscript: [read it on the plane home!](#)
- Underlying math: Halko et al (ArXiv) *Finding structure with randomness*



# Any questions?

Thanks to:

- Thomas Lumley, Jen Brody, Gina Peloso
- CHARGE Lipids Working Group
- TOPMed Analysis group and Data Coordinating Center
- Analysis Commons on DNAnexus
- University of Washington Genetic Analysis Center

We are recruiting research scientists –  
email Cathy Laurie: [cclaurie@uw.edu](mailto:cclaurie@uw.edu)... **fast!**