** Modified and added to by Eric Shea-Brown for AMATH 422/522: errors and other unpleasantries may have been introduced, unless you’re in this class refer to www.cam.cornell.edu/~dmb/DMBsupplements.html for the original!! With additional material from Prof. Mark Goldman, UC Davis

Introduction

These notes for computer labs accompany our textbook *Dynamic Models in Biology* (Princeton University Press 2006). They are based in part on course materials by former TAs Colleen Webb, Jonathan Rowell and Daniel Fink at Cornell, Professors Lou Gross (University of Tennessee) and Paul Fackler (NC State University), and on the book *Getting Started with Matlab* by Rudra Pratap (Oxford University Press). So far as we know, the exercises here and in the textbook can all be done using the Student Edition of Matlab, or a regular base license without additional Toolboxes.

Thinking about MATLAB

- Very sophisticated “graphing calculator”
- High-level programming language for scientific computing
- vs. c or FORTRAN, many built-in commands, less-complex syntax
- vs. c or FORTRAN, Interpreted language (code translated during run), with some pre-compiled functions
- IF used carefully, good balance of speed and ease of use
1 Interactive calculations

The MATLAB interface is a set of interacting windows. In some of these you “talk” to MATLAB, and in others MATLAB “talks” to you. Windows can be closed (the × button) or detached to become free-floating (curved arrow button). To restore the original layout, use View/Desktop Layout/Default in the main menu bar.

Two important windows are Help window and Command. Launch Pad is the online Help system. To open this, type doc in the command window and hit enter. The Command window is for interactive commands, meaning that the command is executed and the result is displayed as soon as you hit the Enter key.

1.1 Graphing calculator mode – working in the command window

For example, at the command prompt >>, type in 2+2 and hit Enter; you will see

```matlab
>> 2+2
ans =
   4
```

**Suppressing output:** Now type in 2+2; (including the semicolon) – what happens? A semicolon at the end of a line tells MATLAB not to display the results of the calculation. This lets you do a long calculation (e.g. solve a model with a large number of intermediate results) and then display only the final result.

1.1.1 Variables

To do anything complicated, the results have to be stored in variables. For example, type a=2+2 in the Command window and you see

```matlab
>> a=2+2
a =
   4
```

The variable a has been created, and assigned the value 4. By default, a variable in MATLAB is a matrix (a rectangular array of numbers); in this case a is a matrix of size $1 \times 1$ (one row, one column), which acts just like a number.

Variable names must begin with a letter, and followed by up to 30 letters, numbers, or underscore characters. Matlab is case sensitive: Abc and abc are not the same variable. In contrast to some other languages, a period (.) cannot be part of a variable name.

```matlab
>> a1=2
>> my_favorite_variable_number_2=4
```
VALID: Letter followed by letters, numbers, underscore character.

NOTE! capitalization matters. $A \neq a$ !!

NOT VALID:

```matlab
>> my_favorite_variable#2=4
??? my_favorite_variable#2=1
>> 2a=1
Error: Unexpected MATLAB expression.
>> my.favorite.variable.name=1
my =
    favorite: [1x1 struct]
```

Exercise 1.1 Here are some variable names that cannot be used in Matlab; explain why:
cell.maximum.size; 4min; site#7 .

1.1.2 FUNDAMENTAL PROGRAMMING SYNTAX: Assigning VALUES to VARIABLES

- LHS = RHS
- value RHS assigned to LHS, NOT other way around

```matlab
>> c=2
c =
    2

>> 2=c
??? 2=c
Error: The expression to the left of the equals sign is not a valid target for an assignment.
```

Another example:

```matlab
>> a=2;b=4;
>> a=b;
>> a,b
```

Exercise 1.2 What values do you get for a and b in the above? Explain why.

```matlab
>> a=2;b=4;
>> b=a;
>> a,b
```

Exercise 1.3 What values do you get for a and b in the above? Explain why.
Calculations

Calculations are done with variables as if they were numbers

+  
-  
/  (divide)  
*  (multiply)  
^  (exponent)  
abs(x)  (absolute value)  
\cos(x), \sin(x), \tan(x) \quad \text{IMPORTANT: ANGLE } x \text{ IS INTERPRETED IN RADIANS}  
\exp(x)  \text{ exponential function } e^x  
\log(x)  \text{ log to base } e  
\log10(x)  \text{ log to base } 10  
sqrt(x)  \text{ square root}  

The latter are built-in functions

```matlab
>> a = sqrt(2)  
a = 1.4142  
>> a=2 ; b=4 ; c=a^b  
c = 16  
```

For example enter

```matlab
>> x=5; y=2; z1=x*y, z2=x/y, z3=x^y  
```

and you should see

```matlab
z1 =  
10  
z2 =  
2.5000  
z3 =  
25  
```

Notice that several commands can go on the same line. The first two were followed by semicolons, so the results were not displayed. The rest were followed by commas, and the results were displayed. A comma after the last statement on the line isn’t necessary.

You can do several operations in one calculation, such as

```matlab
>> A=3; C=(A+2*sqrt(A))/(A+5*sqrt(A))  
C =  
0.5544  
```
The parentheses are specifying the order of operations. The command

\[
\text{>> C}=A+2*\sqrt{A}/A+5*\sqrt{A}
\]

gets a different result – the same as

\[
\text{>> C}=A + 2*(\sqrt{A}/A) + 5*\sqrt{A}.
\]

The default order of operations is:

PEMDAS

parenthesis
exponentiation
multiplication
division
addition
subtraction

Say we want: \( a = 2 \), \( b = 4 \), \( c = \frac{a}{a+b} \)

\[
\text{>> a}=1 \ ; \ b=4 \ ; \ c=a/(a+b)
\]
\[
c = 5 \ \ldots \ \text{WRONG OR RIGHT?}
\]

\[
\text{>> a}=1 \ ; \ b=4 \ ; \ c=a/(a+b)
\]
\[
c = 0.2000 \ \ldots \ \text{WRONG OR RIGHT?}
\]

Operations of equal priority are performed left to right.

\[
\text{>> b} = 12-4/2^3 \quad \text{gives} \quad 12 - 4/8 = 12 - 0.5 = 11.5
\]
\[
\text{>> b} = (12-4)/2^3 \quad \text{gives} \quad 8/8 = 1
\]

**Exercise 1.4** Compute the values of \( b \) below, and explain the results you get.

\[
\text{>> b} = -1^2
\]
\[
\text{>> b} = (-1)^2
\]

In complicated expressions it’s best to use parentheses to specify explicitly what you want, such as \( \text{>> b} = 12 - (4/2^3) \) or at least \( \text{>> b} = 12 - 4/(2^3) \). **Use lots of parentheses** instead of trusting the computer to figure out what you meant.

**Exercise 1.5**: Have MATLAB compute the values of

1. \( \frac{2^5}{2^{(-1)}} \) and compare it with \((1 - \frac{1}{2})^{-1} \) [answer: 1.0323]

2. \( \sin(30), \sin(\pi/6), \cos^2(\pi/8) \) [answers for last two: 0.5, 0.8536. The constant \( \pi \) is a pre-defined variable \( \text{pi} \) in Matlab. So typing \( \cos(\text{pi}/8) \) works in Matlab, but note that \( \cos(\text{pi}^2)/\text{8} \) won’t work!]

3. \( \frac{2^5}{2^{(-1)}} + 4\sin(\pi/6) \) [answer: 3.0323].
1.2 Storing + viewing variables and their values

Even though x and y were not displayed, MATLAB automatically “remembers” their values. This is a blessing and a curse. First, three ways to see what values are stored:

(1) Type

```
>> x, y
```

and MATLAB displays the values of x and y.

(2) Variables defined in a session are displayed in the Workspace window. Click on the tab to activate it and then double-click on x to launch a window summarizing x’s properties and entries. Since x is a 1×1 matrix, there’s only one value. Getting a bit ahead of ourselves, create a 3×2 matrix of 1’s with the command

```
>> X=ones(3,2)
```

and then look at what X is using the Workspace window. Clicking on the matrix icon opens a window that displays its values.

(3) Use the whos command (MATLAB)

```
>> whos
```

<table>
<thead>
<tr>
<th>Name</th>
<th>Size</th>
<th>Bytes</th>
<th>Class</th>
<th>Attributes</th>
</tr>
</thead>
<tbody>
<tr>
<td>a</td>
<td>1x1</td>
<td>8</td>
<td>double</td>
<td></td>
</tr>
<tr>
<td>b</td>
<td>1x1</td>
<td>8</td>
<td>double</td>
<td></td>
</tr>
<tr>
<td>c</td>
<td>1x1</td>
<td>8</td>
<td>double</td>
<td></td>
</tr>
</tbody>
</table>

Now to the curse: stored values can come back to haunt you, giving unintended output. Thus:

GOOD PRACTICE: clear variables before starting to program.

```
>> clear all
>> whos
```

COMMANDS stored in memory

Commands can be edited, instead of starting again from scratch. There are two ways to do this. In the Command window, the ↑ key recalls previous commands. For example, you can bring back the next-to-last command and edit it to

```
>> x=5  y=2  z1=x*y  z2=x/y  z3=x^y
```
so that commands are not separated by either a comma or semicolon. Then press Enter, and you will get an error message. *Multiple commands on a line have to be separated by a comma or a semicolon (no display).*

The other way is to use the **Command History** window, which holds a running history of your commands. You can re-run a command by double-clicking on it.

### 1.3 Help !!!

MATLAB also has many **built-in mathematical functions** that operate on variables (see Table above). You can get help on any function by entering

```
help functionname
```
in the console window (e.g., try `help sqrt`).

```
>> help sqrt
SQRT   Square root.
    SQRT(X) is the square root of the elements of X. Complex results are produced if X is not positive.

    See also sqrtm, realsqrt, hypot.

    Reference page in Help browser
    doc sqrt
```

**Even better** – a more extensive help browser appears when you type `doc` – try this for `sin (doc sin)` and `sqrt`.

Thanks anyway, but what SHOULD I be looking up? the `lookfor` command

```
>> lookfor exponent
EXP    Exponential.
EXPINT Exponential integral function.
EXPM   Matrix exponential.
...
```

**Representation of numbers in scientific computing: finite precision**

Standard: IEEE floating point arithmetic.

Important feature – finite precision: approx 16 significant digits

Display more digits:

```
>> a=0.1
```
a =
    0.1000
>> format long
>> a
a =    0.100000000000000

Roundoff error:

>> a=4/3 ; b=a-1 ; c = (3*b)-1

Exercise 1.6 What value does MATLAB return for c above? Does this make sense?

OVERFLOW AND UNDERFLOW:
Maximum number: \( \approx 10^{308} \)
Minimum number: \( \approx 10^{-308} \)
Overflow:

>> a=10^400
a =     Inf

Underflow

>> a=10^-400
a =     0

Another special number: not defined

>> 0/0
ans =
     NaN
2 Vectors

MATLAB uses vectors and matrices (1- and 2-dimensional rectangular arrays of numbers) as its primary data types. Starting with the former, a vector value is just a list of scalar values.

Arranged horizontally into a row vector:

\[ \vec{x} = (6 \ 12 \ 5). \]  
(1)

Or vertically into a column vector:

\[ \vec{x} = \begin{pmatrix} 6 \\ 12 \\ 5 \end{pmatrix}. \]  
(2)

In MATLAB, row vectors are entered with brackets and spaces or commas:

\[
\begin{align*}
\text{>> } & x=[6 \ 12 \ 5] \\
& x = 6 \quad 12 \quad 5
\end{align*}
\]

OR

\[
\begin{align*}
\text{>> } & x=[6 , 12 , 5] \\
& x = 6 \quad 12 \quad 5
\end{align*}
\]

In MATLAB, column vectors are entered via semicolons:

\[
\begin{align*}
\text{>> } & x=[6 ; 12 ; 5] \\
& x =
\begin{array}{c}
6 \\
12 \\
5
\end{array}
\end{align*}
\]

The transpose operation switches between row and column vectors. This is given by dot prime in MATLAB. That is, in MATLAB:

\[
\text{>> } y=x.'. 
\]
2.1 Computing with vectors

TWO BASIC OPERATIONS ON VECTORS:

**Multiplication by scalar**

\[
\mathbf{c} \mathbf{x} = \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix} = \begin{pmatrix} cx_1 \\ cx_2 \\ cx_3 \end{pmatrix}; \text{ that is, } x_j \rightarrow cx_j
\]

Matlab does this via *

\[
\text{>> } \mathbf{x}=[1;2;3] \text{ ; } 3*\mathbf{x}
\]

ans =

3
6
9

**Addition of two vectors**

\[
\mathbf{x} + \mathbf{y} = \begin{pmatrix} x_1 + y_1 \\ x_2 + y_2 \\ x_3 + y_3 \end{pmatrix}
\]

Subtraction is similar, and this works the same for row and column vectors. Matlab implements this via + and - operations:

\[
\text{>> } \mathbf{x}=[1;2] \text{ ; } \mathbf{y}=[0;-2]; \mathbf{z}=\mathbf{x}+\mathbf{y}
\]

\[
\mathbf{z} =
\begin{pmatrix}
1 \\
0
\end{pmatrix}
\]

Matrix dimensions must agree: add row + row or col + col. Here is what happens if this rule is violated:

\[
\text{>> } \mathbf{z}+ [2 \ 2]
\]

??? Error using ==> plus

Overall, once a vector has been created it can be used in calculations as if it were a number (more or less).

\[
\text{>> } \text{initialsize}=[1,3,5,7,9,11]
\]
>> finalsize=initialsize+1
finalsize =
    2 4 6 8 10 12
>> newsize=sqrt(initialsize)
newsize =
    1.0000 1.7321 2.2361 2.6458 3.0000 3.3166

Notice that the operations were applied to every entry in the vector. Similarly,
    initialsize-5, 2*initialsize, initialsize/10
apply subtraction, multiplication, and division to each element of the vector. But now try
    >> initialsize^2
and MATLAB responds with

??? Error using ==> ^
Matrix must be square.

Why? Because initialsize^2 is interpreted as initialsize*initialsize, and * indicates
matrix multiplication. It was OK to compute 2*initialsize because Matlab interprets mul-
tiplication with a 1 x 1 matrix as scalar multiplication. But matrix multiplication of A*A is
only possible if A is a square matrix (number of rows equal to the number of columns).

Entry-by-entry operations are indicated by a period before the operation symbol:

    >> nextsize=initialsize.^2
    >> x=initialsize.*newsize
    >> x=initialsize./finalsize

Note that addition and subtraction are always term-by-term.

**Functions for vector construction**

A set of regularly spaced values can be constructed by
    x=start:increment:end

    >> x=0:1:10
    x =
      0 1 2 3 4 5 6 7 8 9 10

The increment can be positive or negative. If you omit the increment it is assumed to be
1, hence x=0:10 gives the same result as x=0:1:10.

x=linspace(start, end, length) lets you specify the number of steps rather than
the increment.
Note that `linspace` requires commas as the separators, instead of colons.

**Exercise 2.1** Create a vector \( v=[1 \ 5 \ 9 \ 13] \), first using the \( v=a:b:c \) construction, and then using \( v=linspace(a,b,c) \).

**Vector addressing**

Often it is necessary to extract a specific entry or other part of a vector. This is done using subscripts, for example:

```
>> initialsize(3)
an =
5
```

This extracts the third element in the vector. You can also access a block of elements using the functions for vector construction

```
c=initialsize(2:5)
c =
   3 5 7 9
```

This has extracted the 2\textsuperscript{nd} through 5\textsuperscript{th} elements in the vector. If you type in

```
>> c=initialsize(4:2:6)
```

the values in parentheses are interpreted as in vector creation \( x=(a:b:c) \). So what do you think this command will do? Try it and see.

Extracted parts don’t have to be regularly spaced. For example

```
>> c=initialsize([1 2 5])
c =
   1 3 9
```

extracts the 1\textsuperscript{st}, 2\textsuperscript{nd}, and 5\textsuperscript{th} elements.

Addressing is also used to set specific values within a vector. For example,

```
>> initialsize(1)=12
```
changes the value of the first entry in `initialsize` while leaving the rest alone, and

```
>> initialsize([1 3 5])=[22 33 44]
```
changes the 1\textsuperscript{st}, 3\textsuperscript{rd}, and 5\textsuperscript{th} values.

Illustrating a common error:
Moreover: remember (especially if you code in C or Python!) that indexing in MATLAB starts with 1; x(0) does not work.

**Exercise 2.2** Write a **one-line** command to extract the the second, first, and third elements of initialsize **in that order**.

**Exercise 2.3** : Have MATLAB compute the values of

1. Make a list numbers spaced by 0.2, between a minimum value of 1 and a maximum value of 20. Assign that list to the variable name `myvector`.
2. repeat the previous command using `linspace`
3. pick out the 4th value of `myvector` and assign it to the variable name `fourthelement`

### 3 Time to code! Writing script (.m) files

Small tasks can be done interactively, but modeling or complicated data analysis are done using **programs** – sets of commands stored in a file. MATLAB uses the extension `.m` for program files and refers to them as **M-files**.

- Type `edit` at command line
- Put a few of your favorite commands in the editor
- Make sure `clear all` is the first line in your program
- save it as `myprogram.m` Remember the folder where you saved it.
- You’ve made a .m file — that is, a MATLAB program!
- Navigate (click on the ..., or use the `cd` command) in the command window to the location where you stored the program
- To run it, type `myprogram` at the command line

Most programs for working with models or analyzing data follow a simple pattern:

1. “Setup” statements.
2. Input some data from a file or the keyboard.
3. Carry out the calculations that you want.

4. Print the results, graph them, or save them to a file.

**Exercise 3.1** Write a program `integrator_1.m`. First define the discrete vector `signal_vector=sin(t)` where `t=[1:10]` represents time. Write code that computes `I_vector` as the cumulative sum of `signal_vector`. (Hint: use `doc` and `help`). Make a plot of `I_vector` vs. `t` using `*` markers for the data. Have your .m file automatically label the axes. (Hint: use `doc plot` to learn all about plotting). Is it clear that `I_vector` represents a “discrete” integral of the signal?

**The for loop**

Loops make it easy to do the same operation over and over again, for example:

- make population forecasts 1 year ahead, then 2 years ahead, then 3, ...
- update the state of every neuron based on the inputs it received in the last time interval.

The basic structure can be understood via this MATLAB code.

```matlab
for n= 1:9
    disp(n)
end
```

Use `edit` to code this into a program `myloop.m`, save it and run it!

**COMPONENTS OF THE FOR LOOP:**

- `n` loop variable
- `1:9` loop vector
- `disp(n)` or `print(n)` command
HOW IT WORKS:

- Code starts with n equal to first element in loop vector
- runs command
- advances n to next element
- repeats
- quits when have covered all elements of loop vector

In more detail:

- in any for loop, we define a list of numbers, here 1 through 9. think of this as the "loop vector." The loop vector can be any list of numbers – it does not have to be “integers counting up.”
- the loop variable, n, starts at the first number in the list. it is set equal to that value
- the commands (here, just printing the value of n to the screen) are run
- then when end is reached, n is reset to the NEXT number in the list, the commands are run, and the process is repeated
- it terminates when all entries of the loop vector have been used.

Please type in, and make sure you understand what happens, for these example as well:

```matlab
for p=[4 6 67 -1]
    disp(p)
end

sum=0
for k=1:5
    sum=sum+k
end
```
Table 1: Comparison and logical operators in Matlab.

<table>
<thead>
<tr>
<th>Operator</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>==</td>
<td>Equal to</td>
</tr>
<tr>
<td>~=</td>
<td>Not equal to</td>
</tr>
<tr>
<td>&lt;</td>
<td>Less than</td>
</tr>
<tr>
<td>&lt;=</td>
<td>Less than or equal to</td>
</tr>
<tr>
<td>&gt;</td>
<td>Greater than</td>
</tr>
<tr>
<td>&gt;=</td>
<td>Greater than or equal to</td>
</tr>
<tr>
<td>&amp;</td>
<td>AND</td>
</tr>
<tr>
<td></td>
<td></td>
</tr>
<tr>
<td>~</td>
<td>NOT</td>
</tr>
</tbody>
</table>

4 IF STATEMENTS

Logical conditions also allow the rules for "what happens next" in a model to be affected by the current values of state variables. The if statement lets us do this; the basic format is

```matlab
if(condition);
    commands
else;
    other commands
end;
```

Here's a simple example or two. Code this into MATLAB:

```matlab
x=2
if (x==2);
    disp('OK, x is 2')
else;
    disp('umm, x is not 2')
end;

x=3
if (x<2);
    disp('OK, x is less than 2')
else;
    disp('umm, x is not less than 2')
end;
```

You get the picture: the condition is ANYTHING you want that is true or false. Of course, for this to make sense, we need MATLAB operations that return true or false values after doing a logical test. We've seen two of these above, but and a complete list is in Table 1.

If the "else" is to do nothing, you can leave it out:
As in

```matlab
x=3
if (x<2);
    disp('OK, x is less than 2')
end;
```

**Exercise 4.1 INTEGRATOR STAGE 2:** Write a code `integrator_function.m` which

- defines a signal `signal_vector` (a vector of signal values at different timepoints).
- defines a threshold `thresh`

and computes as its answer the first time that the cumulative sum of the signal crosses the threshold.
More complicated decisions can be built up using `elseif`. The basic format for that is

```matlab
if(condition);
    commands
elseif(condition);
    other commands
else;
    other commands
end;
```

5 Creating new functions

M-files can be used to create new functions, which then can be used in the same way as Matlab’s built-in functions. Function m-files are often `useful` because they let you break a big program into a series of steps that can be written and tested one at a time. They are also sometimes `necessary`. For example, to solve a system of differential equations in Matlab, you have to write a function m-file that calculates the rate of change for each state variable.

5.1 Simple functions

Function m-files have a special format. Here is an example, `mysum.m` that calculates the sum of the entries in a matrix [the `sum` function applied to a matrix calculates the sum of each column, and then a second application of `sum` gives the sum of all column sums].

```matlab
function f=mysum(A);
    f=sum(sum(A));
return;
```

It works like this:

```matlab
>> mysum([1 2])
an =
3
```

This example illustrates the rules for writing function m-files:

1. The first line must begin with the word `function`, followed by an expression of the form: `variable_name = function_name(function arguments)`
2. The function name `must` be the same as the name of the m-file.
3. The last line of the file is `return;` (this is not required in the current version of Matlab, but is useful for compatibility with older versions).

4. In between are commands that calculate the function value, and assign it to the variable `variable_name` that appeared in the first line of the function.

### 5.2 Functions with multiple arguments or returns

Matlab functions can have more than one argument, and can return more than one calculated variable. The function `eulot.m` is an example with multiple arguments. It computes the Euler-Lotka sum

\[
\sum_{a=0}^{n} \lambda^{-(a+1)} l_a f_a - 1
\]

as a function of \(\lambda\), and vectors containing the values of \(l_a\) and \(f_a\).

```matlab
function f=eulot(lambda,la,fa);
age=0:(length(la)-1);
y=lambda.^(-(age+1));
f=sum(y.*la.*fa)-1;
return;
```

We have seen that (given the values of \(l_a\) and \(f_a\)) the dominant eigenvalue \(\lambda\) of the age-structured model results in this expression equaling 0. Type in

```
>> la=[0.9 0.8 0.7 0.5 0.2]; fa=[0 0 2 3 5];
eulot(1.4,la,fa) and eulot(1.5,la,fa) have opposite signs, indicating that \(\lambda\) is between 1.4 and 1.5.
```

To have more than one returned value, the first line in the m-file is slightly different: the various quantities to be returned are enclosed in `[ ]`. An example is `stats.m`:

```matlab
function [mean_x,var_x,median_x,min_x,max_x]=stats(x);
mean_x=mean(x); var_x=var(x);
median_x=median(x);
min_x=min(x); max_x=max(x);
return;
```

Function m-files can contain `subfunctions`, which are functions called by the main function (the one whose name appears in the m-file name). Subfunctions are “visible” only within the m-file where they are defined. In particular, you cannot call a subfunction at the Command line, or in another m-file. For example, create an m-file `Sumgeseries.m` with the following commands:

```matlab
function f=Sumgseries(r,n);
u=gseries(r,n); f=sum(u);
return;
```
function f=gseries(r,n);
    f=r.^(0:n);
    return;

Only the first of the two functions – the one with the same name as the m-file will be 'visible' to Matlab. That is:

>> Sumgseries(0.1,500)
an =
    1.1111
>> gseries(0.1,500)
?? Undefined command/function 'gseries'.

Exercise 5.1. Write a function m-file rmatrix.m which takes as arguments 3 matrices A,S,Z, and returns the matrix B = A + S.* Z. When it's working you should be able to do:

>> A=ones(2,2); S=0.5*eye(2); Z=ones(2,2); B=rmatrix(A,S,Z)
B =
     1.5000    1.0000
     1.0000    1.5000