

Statistics 394, Problem Set 5

Wellner; 2/2/2000

- Reading:** Kelly, Chapter 3, Sections 1.1 - 3.4.
Optional Web Reading: Section I.C.4 & 5, Distributions & Conditional distributions at <http://www.math.uah.edu/stat/dist/index.html> .
Due: Wednesday, February 9, 2000.
Reminder: Mid-Term Exam: Monday, February 7.

1. K 3.1, # 7 (page 155). (Look at, but don't turn in, # 8.)
2. K 3.2, # 1 (page 167).
3. K 3.2, # 4 (page 167).
4. K 3.2, # 5 (page 167).
5. Suppose that two fair dice are rolled and the sequence of scores (X_1, X_2) are recorded. Let $T = X_1 + X_2$ and $D = X_1 - X_2$ denote the sum and difference of the scores, respectively.
 - (a) Find the joint mass function of (T, D) ; call it $p_{T,D}$.
 - (b) Find the marginal probability mass function of D ; call it p_D .
 - (c) Find the marginal probability mass function of T ; call it p_T .
 - (d) Are T and D independent? (Justify your answer.)
6. Suppose the same setup as in the previous problem.
 - (a) Find the conditional probability mass function of T given $D = d \in \{-5, -4, \dots, 5\}$.
 - (b) Find the conditional probability mass function of D given $T = t \in \{2, 3, \dots, 12\}$.