Noise correction of turbulent spectra obtained from Acoustic Doppler Velocimeters

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Abstract

Turbulent Kinetic Energy (TKE) frequency spectra are essential in characterizing turbulent flows. The Acoustic Doppler Velocimeter (ADV) provides three-dimensional time series data at a single point in space which are used for calculating velocity spectra. However, ADV data are susceptible to contamination from various sources, including instrument noise, which is the intrinsic limit to the accuracy of acoustic Doppler processing. This contamination results in a flattening of the velocity spectra at high frequencies ($\mathcal{O}(10)$ Hz). This paper demonstrates two elementary methods for attenuating instrument noise and improving velocity spectra. First, a "Noise Auto-Correlation" (NAC) approach utilizes the correlation and spectral properties of instrument noise to identify and attenuate the noise in the spectra. Second, a Proper Orthogonal Decomposition (POD) approach utilizes a modal decomposition of the data and attenuates the instrument noise by neglecting the higher-order modes in a time-series reconstruction. The methods are applied to ADV data collected in a tidal channel with maximum horizontal mean currents up to 2 m/s. The spectra estimated using both approaches exhibit an $f^{-5/3}$ slope, consistent with a turbulent inertial sub-range, over a wider frequency range than the raw spectra. In contrast, a Gaussian filter approach yields spectra with a sharp decrease at high frequencies. In an example application, the extended inertial sub-range from the NAC method increased the confidence in estimating the turbulent dissipation rate, which requires fitting the amplitude of the $f^{-5/3}$ region. The resulting dissipation rates have smaller uncertainties and are more consistent with an assumed local balance to shear production, especially for mean horizontal currents less than 0.8 m/s.

Keywords: Marine-Hydro Kinetic (MHK) devices, Turbulent flow, Turbulent Kinetic Energy (TKE) Spectra, ADV, Doppler /instrument Noise

1 1. Introduction

Acoustic Doppler Velocimeter (ADV) data are commonly used for performing field measurements in rivers and oceans [1, 2, 3, 4, 5]. The ADV measures fluid velocity by comparing the Doppler phase shift

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of coherent acoustic pulses along three axes, which are then transformed to horizontal and vertical compo-4

nents. In contrast to an an Acoustic Doppler Current Profiler (ADCP), the ADV samples rapidly ($\mathcal{O}(10)$) 5 Hz) from a single small sampling volume ($\mathcal{O}(10^{-2})$ m diameter). The rapid sampling is useful for estimating

the turbulent intensity, Reynolds stresses, and velocity spectra. Velocity spectra are useful in characterizing 7

uid flow and are also used as an input specification for synthetic turbulence generators (e.g., TurbSim [6]

and computational fluid dynamics (CFD) simulations (viz. TrubSim). These simulations require inflow turbulence conditions for calculations of dynamic forces acting on Marine and Hydro-Kinetic (MHK) en-10

ergy conversion devices [see 7]. This study focuses on accurate estimation of velocity spectra from ADV 11 measurements that are contaminated with noise, for application in CFD simulations for MHK devices.

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ADV measurements are contaminated by Doppler noise, which is the intrinsic limit in determining a 13 unique Doppler shift from finite length pulses [8, 9, 10]. Doppler noise, also called "instrument noise", can 14 introduce significant error in the calculated statistical parameters and spectra. Several previous papers have 15 addressed Doppler noise and its effect on the calculated spectra and statistical parameters [5, 8, 9, 10]. These 16 studies have shown that the Doppler noise has properties similar to that of white noise and is associated 17 with a spurious flattening of ADV spectra at high frequencies [8, 9]. In the absence of noise, velocity 18 spectra in the range of 1 to 100 Hz are expected to exhibit an $f^{-5/3}$ slope, termed the inertial sub-range 19 [11, 12, 13]. Nikora et.al. [8] showed that the spurious flattening at high frequencies is significantly greater 20 for the horizontal u and v components of velocity as compared to the vertical w component of velocity, and 21 is a result of the ADV beam geometry. Motivated by the many applications of velocity spectra, this study 22 examines the effectiveness of two elementary techniques to minimize the contamination by noise in velocity 23 spectra calculated from ADV data. 24

ADV measurements are also contaminated by spikes, which are random outliers that can occur due to 25 interference of previous pulses reflected from the flow boundaries or due to the presence of bubbles, sediments, 26 etc in the flow. Several previous papers have demonstrated methods to identify, remove and replace spikes 27 in ADV data [14, 15, 16, 17, 18]. For example, Elgar and Raubenheimer[14], and Elgar et. al. [16] have 28 used the backscattered acoustic signal strength and correlation of successive pings to identify spikes. Once 29 the spike has been identified, it can be replaced with the running average without significantly influencing 30 statistical quantities [18]. Another technique that is commonly used to de-spike ADV data is Phase-Space-31 Thresholding (PST) [19]. This technique is based on the premise that the first and second derivatives of the 32 turbulent velocity component form an ellipsoid in 3D phase space. This ellipsoid is projected into 2D space 33 and data points located outside a previously determined threshold are identified as spikes and eliminated. 34 The PST approach is an iterative procedure wherein iterations are stopped when no new spikes can be 35 identified. There are several variations of this approach, such as 3D-PST and PST-L, detailed descriptions 36 of which are given in [15, 17]. In the present study, an existing method for despiking from [16] is applied, 37 and we restrict our investigation to Doppler noise. 38

One existing technique to remove Doppler noise from ADV data is a low-pass Gaussian digital filter [10, 20, 21, 22, 23]. Although this technique is capable of eliminating Doppler noise from the total variance, the spectra calculated from filtered data exhibit a sharp decrease at high frequencies. In contrast, Hurther and Lemmin [24], using a four beam Doppler system, estimated the noise spectrum from cross-spectra evaluations of two independent and simultaneous measurements of the same vertical velocity component. After the correction, spectra obtained by Hurther and Lemmin [24] exhibit an $f^{-5/3}$ slope out to the highest frequency (Nyquist frequency).

The present study explores two different approaches for attenuating noise and thereby improving velocity spectra at high frequencies. The first approach, termed the "Noise Auto-Correlation" (NAC) approach, 47 utilizes assumed spectral and correlation properties of the noise to subtract noise from the velocity spectra. 48 The NAC approach is analogous to the Hurther and Lemmin [24] approach, but differs in that they estimate 49 the noise variance using the difference between two independent measures of vertical velocity, whereas in this 50 study the noise variance is estimated from the flattening of the raw velocity spectra. The second approach 51 uses Proper Orthogonal Decomposition (POD) to decompose the velocity data in a series of modes. In 52 POD, the maximum possible fraction of TKE is captured for a projection onto a given number of modes. 53 Combinations of POD modes identify the energetic structures in turbulent data fields [25, 26, 27, 28, 29]. 54 Low-order reconstructions of the ADV data are performed using a reduced number of POD modes which 55 are associated only with the energetic structures in the turbulent flows. This eliminates the random and 56 less energetic fluctuations associated with instrument noise. 57

The field measurements and raw velocity spectra are described in §2 and the methods to attenuate noise 58 from velocity spectra follow in §3. Before detailing the NAC and POD approaches (§3.1 & §3.2, respectively), 59 the assumptions implicit to both methods are described in §32.1. Results, in the form of noise-corrected 60 spectra from both methods, are presented in §4. The noise-corrected spectra are compared with spectra 61 from a Gaussian filter approach in §4.3 and evaluated for theoretical isotropy in §4.4. Finally, an example 62 application is given in §5, where the NAC method is used to reduce uncertainties in estimating the turbulent 63 dissipation rates from the field dataset, especially during weak tidal flows. The NAC method estimates of 64 dissipation rates are also more consistent with an assumed TKE budget, wherein shear production balances 65 dissipation. Conclusions are stated in §6. 66

⁶⁷ 2. Field measurements

⁶⁶ ADV measurements were collected in Puget Sound, WA (USA) using a 6-MHz Nortek Vector ADV. The ⁶⁷ site is near Nodule Point on Marrowstone Island at 48° 01'55.154" N 122°39'40.326" W and 22 m water ⁷⁰ depth, as shown in Fig. 1. The ADV was mounted on a tripod that was 4.6 m above the sea bed (the ⁷¹ intended hub height for a tidal energy turbine), and it acquired continuous data at a sampling frequency f_s



Figure 1: Regional map, bathymetry, and location of ADV measurements at Marrowstone Island site in Puget Sound, northwest of Seattle, WA.

of 32 Hz for four and a-half days during spring tide in February 2011. The mean horizontal currents ranged 72 from 0 to 2 m/s. The measurement location was sufficiently deep (17 m below the water surface at mean 73 lower low water) where the influence of wave orbital velocities may be neglected. The measurement location 74 is in close proximity to headlands, which can cause flow separation and produce large eddies, depending on 75 the balance of tidal advection, bottom friction, and local acceleration due to the headland geometry. In a 76 prior deployment at the same location, the tripod was instrumented with a HOBO Pendant-G for collecting 77 acceleration data. Results indicate that tripod motion (e.g., strumming at the natural frequency) is unlikely 78 to bias measurements. For further details about the measurement site location and data, see [5, 30]. 79

The raw data acquired from the ADV are shown in Fig. 2(a), where a few spikes are obvious in the raw data. The flow velocity did not exceed the preset velocity range of the ADV [see 5, 30], and there was no contamination from the flow boundary (ADV was positioned facing upward). Thus, these are

treated as spikes and removed according to Elgar and Raubenheimer [14], and Elgar et al. [16]. The spikes 83 constitute less than 1% of all data, thus a more advanced algorithm was not necessary. Before performing 84 this Quality Control (QC), the continuous data are broken into sets of 300 s (five minutes) data records, each 85 containing 9600 data points, which yields 1256 independent data records. This ensures that the velocity 86 measurements are stationary (i.e., stable mean and variance) for each set, which is essential for implementing 87 de-spiking approach, calculating statistical quantities, and calculating velocity spectra [31]. Furthermore, а 88 two-sample Kolmogorov-Smirnov test is performed to validate that the samples for a given record have 89 the same distribution with a 5% significance level. The QC routine removes data with low pulse-to-pulse 90 correlations, which are associated with spikes in the ADV data. A low correlation cut-off c value [14, 16] is 91 determined using the equation $c = 30 + 40\sqrt{f_s/f_{max}}$ where f_s is the actual sampling frequency and f_{max} 92 is the maximum possible sampling frequency. The average acoustic correlations for the ADV measurements 93 performed for this investigation are 93.35, 96.70 and 96.72 for beam-1, beam-2, and beam-3 respectively, 94 while the minimum values of the average acoustic correlations are 88.85, 93.62 and 93.42 for beam-1, beam-95 and beam-3 respectively. The number of spurious points is less than 1% of the total points, and these 96 spurious data points are replaced with the running mean. It has been shown that interpolation of data along 97 the small gaps between data points that have been replaced by the running mean does not significantly alter 98 the spectra or the second order moments, provided only a few data points are replaced [14, 16, 18]. The 99 approach used here successfully eliminates the obvious spikes from the entire raw data, as shown in Fig. 2(b). 100 The ADV data set from which spikes have been removed will be referred to as QC ADV data in the remainder 101 of the paper. 102

103 2.1. Flow Scales

The ADV data were collected in an energetic tidal channel with a well-developed bottom boundary 104 layer (BBL). In such a boundary layer, the canonical expectation is for a turbulent cascade to occur which 105 transfers energy from the large scale eddies (limited by the depth or the stratification) to the small scale 106 eddies (limited by viscosity). In frequency, this cascade occurs in the $f^{-5/3}$ inertial sub-range, assuming 107 advection of a frozen field (i.e., Taylor's hypothesis $f = \langle u \rangle /L$). The extent of this frequency range can 108 be estimated from the energetics of the flow. Independent estimates of the turbulent dissipation rates ϵ 109 (using the structure function of collocated ADCP data, see [5, 32, 33]) range from 10^{-6} to 10^{-4} m²/s³. The 110 Kolmovgorov scale, at which viscosity ν acts and limits the inertial sub-range, is given by $L_k = (\nu^3/\epsilon)^{1/4}$, 111 and thus ranges from 10^{-3} to 10^{-4} m. Converting this length scale to frequency by advection of a mean 112 flow of $\mathcal{O}(1)$ m/s, we expect the inertial sub-range will extend to a frequency of 10^3 to 10^4 Hz. This is well 113 beyond the 16 Hz maximum (i.e., Nyquist frequency) of the following analysis, and thus we expect the true 114 spectra to follow a $f^{-5/3}$ slope throughout the higher frequencies. 115

Another consideration for the high frequency spectra is the sampling volume of the measurement. Using

the 0.014 m diameter sampling volume setting in the Nortek configuration software, the corresponding maximum frequency for accurate measurements is $f = \langle u \rangle / L = 1/0.014 = 71$ Hz, which is again greater than the 16 Hz maximum (i.e., Nyquist frequency) of the following analysis. At lower speeds this frequency will decrease (and vice-versa), and at 0.22 m/s the frequency becomes equal to the 16 Hz Nyquist frequency of our data. Thus, the sampling volume is sufficiently small for accurate high-frequency measurements in all but the weakest tidal conditions (horizontal mean currents less than 0.22 m/s occur for only 6% of the dataset).

The lowest frequency of the inertial sub-range is set by the size of the large energy-containing eddies, and for isotropy, these must be smaller than the distance to the boundary (4.6 m) or the Ozimdov length. Since the site is well-mixed, the distance to the boundary is the limiting scale, and, again using Taylor's frozen turbulence hypothesis, suggests that the lower bound for the inertial sub-range is ~0.2 Hz. Thus, we expect, from dynamical arguments alone, to observe isotropic $f^{-5/3}$ spectra from approximately 10^{-1} to 10^4 Hz, and deviations in the spectra from the $f^{-5/3}$ slope in this range suggest noise contamination in the ADV data.

131 2.2. Spectra

The observed TKE varied significantly during each tidal cycle, and the 1256 records of QC ADV data are divided into two groups: slack and non-slack tidal conditions. The slack tidal and non-slack tidal conditions are the time periods when the mean horizontal velocity magnitudes for a record are less than and greater than 0.8 m/s respectively [5, 30]. This cutoff is chosen primarily for relevance to tidal energy turbines, which typically begin to extract power at $\mathcal{O}(1)$ m/s. However, the 0.8 m/s criterion is also relevant to the conditions for which noise creates uncertainty in the turbulent dissipation rate (see §5).

There are 525 data records of slack tidal condition and 731 data records of non-slack tidal condition, with 138 each record containing 300 s of data and 9600 data points. The energy spectra of the u, v, and w velocity 139 components are calculated for each ADV data record using the Fast Fourier Transform (FFT) algorithm on 140 Hamming-tapered windows of 1024-points each with 50% overlap. This yields approximately 47 equivalent 141 Degrees of Freedom (DOF) [34]. The mean velocity spectra for the non-slack and slack tidal conditions are 142 shown in Figs. 3(a) and (b) respectively. The energy in the spectra decreases with increasing frequency, with 143 flat noise-floor at high frequencies. The mean spectra for all components of velocity are similar, suggesting \mathbf{a} 144 a quasi-isotropic turbulence, except at high frequencies, where the noise-floor is lower in the vertical velocity 145 spectra than in the horizontal velocity spectra. This difference in noise is a well-known consequence of the 146 ADV beam alignment (30 deg from vertical, 60 deg from horizontal) [9, 35]. 147

As shown in Figs. 4(a)-(c) for slack and non-slack tidal conditions, the grey lines represent the spectra associated with each QC ADV data record, and the solid and dash red, green and blue lines represent the ensemble-averaged spectra for u, v and w components of velocity for slack and non-slack tidal conditions



Figure 2: Data from ADV: (a) raw velocity data, and (b) velocity data after QC step.

respectively. The spectra for the individual records exhibit significant fluctuations from one record to 151 the next, suggesting that there is a significant change in TKE even for the non-slack tidal condition. The 152 ensemble-averaged spectra shown in these figures have a $f^{-5/3}$ slope in the inertial sub-range [11, 12, 13, 36]. 153 which is typical for turbulent flows, and indicative of classic Kolmogorov cascade of energies from the larger 154 to smaller scale eddies. As discussed in §2.1, inertial sub-range should extend from the frequency range of 155 $\mathcal{O}(10^{-1})$ Hz to $\mathcal{O}(10^4)$ Hz. However, it is observed from these figures that the ensemble-averaged spectra 156 for u and v components of velocity display a flattening at frequencies greater than 1 Hz for horizontal 157 components (i.e., a deviation from $f^{-5/3}$ slope in inertial sub-range). This is consistent with the effect of 158 instrument noise observed by Nikora and Goring [8], and Voulgaris and Trowbridge [9]. Nikora and Goring 159 [8] defined a characteristic frequency (f_b) , which separates two regions in the spectra: 1) the region where 160 TKE is much larger than the instrument noise energy (i.e., for $f \leq f_b$) and 2) the region where TKE is 161 comparable to the instrument noise energy (i.e., for $f \ge f_b$). The flattening of the spectra is always observed 162 in the region of comparable turbulence and instrument noise energies (i.e., for the region in spectra with 163 $\geq f_b$). For this study, the characteristic frequencies for non-slack and slack tidal conditions, for both u f 164 and v spectra, are observed to be approximately 2.5 Hz and 1.0 Hz, respectively. For vertical spectra, the 165 flattening associated with noise is only evident during slack conditions; however, this is still sufficient to 166

 $_{167}$ degrade estimates of the turbulent dissipation (see §5).



Figure 3: Mean velocity spectra of QC ADV data for u, v, and w components:(a) non-slack tidal condition and (b) slack tidal condition.



Figure 4: Ensemble-averaged spectra for the non-slack (solid colors) and slack (dashed colors) tidal conditions: (a)-(c), u, v, and w components of velocity respectively. Grey lines represent the spectra calculated from individual data records of 300 s each.

¹⁶⁸ 3. Methods

169 3.1. "Noise Auto-Correlation" (NAC)

Studies by Nikora and Goring [8], Voulgaris and Trowbridge [9], and Garcia et al. (2005) [10] have shown 170 that ADV noise is well approximated as Gaussian white noise. They have also shown that the presence of 171 instrument noise in the spectra is associated with flattening of spectra at higher frequencies. The following 172 "Noise Auto-Correlation" (NAC) approach exploits the properties of white noise to identify and attenuate 173 the contribution of instrument noise from the spectra. Although elementary in theory, this classic treatment 174 of noise is appealing because it is simple, direct, and computationally efficient. More advanced techniques, 175 which might treat any nonlinear effects and relax the assumptions on the noise, may be required for other 176 applications. 177

First, the time series (x(t)) is assumed to be contaminated with white noise, and is expressed as the summation of the true signal $(x_s(t))$ and white noise (wn(t)),

$$x(t) = x_s(t) + wn(t), \tag{1}$$

where t is time. The auto-correlation $(R_{x,x}(\tau))$ calculated of the data is

$$R_{x,x}(\tau) = E[x(t)x(t+\tau)],\tag{2}$$

where E represents the expected value, t is time, and τ represents the time-lag associated with autocorrelation. The auto-correlation given by Eq. 2 can also be expressed as the summation of auto-correlations (i.e., R_{x_s,x_s} and $R_{wn,wn}$) and cross-correlations (i.e., $R_{x_s,wn}$ and R_{wn,x_s}) of the true signal and white noise [37, 38],

$$R_{x,x}(\tau) = R_{x_s,x_s}(\tau) + R_{wn,wn}(\tau) + \underbrace{R_{x_s,wn}(\tau)}_{0} + \underbrace{R_{wn,x_s}(\tau)}_{0}.$$
(3)

In Eq. 3, it should be noted that the cross-correlation between true signal and white noise will approach zero for long time series [37, 38]. Therefore, $R_{x,x}$ is expressed as the summation of auto-correlation of true signal and white noise only, as shown in Eq. 3. The auto-correlation function of white noise is a delta function with magnitude equal to the total variance of the white noise (i.e., B) at zero time-lag. Therefore, it is expected that the auto-correlation function of a signal contaminated with white noise would exhibit a spike at zero time-lag, since $R_{x,x}(\tau)$ is the summation of the auto-correlation of clean signal and white noise, schematic of which is shown in the Figs. 5(a)-(c).

Similarly, the spectrum $(S_{x,x}(f))$ calculated from the contaminated data can also be expressed as the summation of the true spectrum $(S_{x_s,x_s}(f))$ and the noise spectrum $(S_{wn,wn}(f))$,

$$S_{x,x}(f) = S_{x_s,x_s}(f) + S_{wn,wn}(f),$$
(4)



Figure 5: Schematic showing the effect of white noise contamination in the auto-correlation function: (a) schematic of autocorrelation function of clean signal, (b) schematic of auto-correlation function of white noise, and (c) schematic of autocorrelation function of clean signal with white noise.



Figure 6: Schematic showing the effect of white noise contamination in the auto-spectral density function: (a) schematic of auto-spectral density function of clean signal, (b) schematic of auto-spectral density function of white noise, and (c) schematic of auto-spectral density function of clean signal with white noise.

where f is the frequency in Hz. The spectrum of the white noise acquires a constant value at all frequencies 194 and the total energy in the white noise (i.e., B) is the area under the spectrum, as shown in Fig. 6 (b). At 195 higher frequencies, where the spectrum of clean signal has energy comparable to the spectrum of white noise, 196 the spectrum of contaminated signal is expected to flatten out, as schematically shown in Figs. 6(a)-(c). 197 Nikora and Goring [8] in their study have suggested that the flattening of the spectra is always observed in 198 the frequency with comparable spectral energies of clean signal and instrument noise. Furthermore, they 199 have also estimated the energy contribution of instrument noise (i.e., B) by calculating the area of the 200 rectangular region extending over all frequencies, with energy levels equal to those of the flattened portion 201 of the spectrum [8, 10]. 202

If the energy contribution from the white noise (i.e., B) is known, the auto-correlation function of the

clean signal (i.e., $R_{x_s,x_s}(\tau)$) can be estimated using the following sets of equations

$$R_{wn,wn}(\tau) = \begin{cases} B & \text{if } \tau = 0; \\ 0 & \text{otherwise.} \end{cases}$$
(5)

$$R_{x_s,x_s}(\tau) = \tilde{R}_{x,x}(\tau) - R_{wn,wn}(\tau).$$
(6)

Finally, the spectra $(S_{x_s x_s}(f))$ of the clean data can be estimated by Fourier transforming the autocorrelation of the true signal determined using Eq. 6, given as

$$S_{x_s x_s}(f) = \int_{-\infty}^{\infty} R_{x_s, x_s}(\tau) e^{-i2\pi f \tau} d\tau.$$
(7)

Here, the NAC approach requires estimating the energy contribution of instrument noise (i.e., B) from 207 the raw spectra, and then using Eqs. 5 and 6 to obtain the auto-correlation function of the noise-removed 208 data. An independent a priori estimate of the noise variance would be preferable; however, that is not 209 possible for a pulse coherent Doppler system, because the noise depends on the correlations of all the pulse 210 pairs (i.e., it is not expected to be constant across all conditions or data records). After determining B, one 211 can calculate the Fourier transform of the noise-removed auto-correlation function to estimate the noise-212 corrected spectra. Again, it should be noted that the NAC approach is only capable of attenuating the 213 instrument noise from the spectra because instrument noise is assumed to be white noise. Unlike the POD 214 method in the following section, the NAC approach can only estimate noise-corrected frequency spectra, 215 and not noise-corrected time series data. 216

217 3.2. Proper Orthogonal Decomposition (POD)

Proper Orthogonal Decomposition (POD) has been used in fluid dynamics for at least 40 years (Lumley 218 [25]). Singular System Analysis, Karhunen-Loeve decomposition, Principle Component Analysis [39], and 219 Singular Value Decomposition (SVD), are names of POD implementations in other disciplines [see 26]. 220 POD is a robust, unambiguous technique, and when applied to a turbulent flow field data set, it can identify 221 dominant features or structures in the data set. Decomposition of the turbulent flow field data by this 222 technique provides a set of modes, and the combination of these modes can be used to represent flow 223 structures containing most of the energy. Moreover, these POD modes are orthogonal and optimal, thus, 224 they provide a compact representation of structures in the flow. POD has been used to study axisymmetric 225 jets [27, 28], shear layer flows [40], axisymmetric wakes [41], coherent structures in turbulent flows [42], and, 226 in the field of wind energy by [43]. Here, POD is used to identify and attenuate noise from the ADV data 227 by performing a low-order reconstruction of the ADV data using only selective, low-order POD modes. 228

When applied to the turbulent velocity data set, the POD technique yields a set of optimal basis functions or POD modes (ϕ 's). These POD modes are optimal in the sense that they maximize the projection of the turbulent data sets on to the POD modes in a mean square sense, expressed as [see 25, 26]

$$\frac{\langle |(u,\phi)|^2 \rangle}{\|\phi\|^2},\tag{8}$$

where $\langle . \rangle$ is the average operator, (.,.) represents the inner product, |.| represents the modulus, and ||.|| is the L^2 -norm. Maximization of $\langle |(u,\phi)|^2 \rangle$ when subjected to the constraint $||\phi||^2 = 1$, leads to an integral eigenvalue problem given as [for detailed derivation see 25, 26]

$$\int_{\Omega} \langle \mathbf{u}(t) \otimes \mathbf{u}(t') \rangle \phi dt = \lambda \phi(t), \tag{9}$$

where Ω is the domain of interest, u is the velocity field (can be either vector or scalar quantities), \otimes is the tensor product, $\langle u(t) \otimes u(t') \rangle$ is the ensemble-averaged autocorrelation tensor of the velocity records forming the kernel of the POD, and λ is the energy associated with each POD mode.

After discretization of Eq. 9, the matrix formulation of the POD implementation for a turbulent data field [see 44, 45, 46] is given by

$$[\mathbb{R}_{uu}]\{\phi\} = \lambda\{\phi\},\tag{10}$$

where \mathbb{R}_{uu} is the ensemble-averaged correlation tensor matrix, ϕ is the POD mode, and λ is the energy 240 captured by each POD mode. The correlation matrix calculated from the turbulent data set is also referred 241 to as the POD kernel. For the POD implementation used in this study, ADV data were broken into 64 242 records each containing 2048 data points, which yielded 2478 and 3410 data records for the slack and \mathbf{S} 243 non-slack tidal conditions respectively. This is in contrast to the 300 s records used for the NAC method, and is necessary to constrain the size of the kernel matrix and thus the computational time. The resulting 245 POD kernel matrix for each record is 2048×2048 , yielding 2048 ϕ 's and λ 's. The slack and non-slack tidal 246 conditions are defined as less than or greater than a horizontal mean flow of 0.8 m/s respectively. 247

248 Once determined, these POD modes can be used to reconstruct each velocity component as

$$\mathbf{u}^{n}(t) = \sum_{p=1}^{N} a_{p}^{n} \phi_{p},\tag{11}$$

where $u^n(t)$ is the n^{th} velocity data record, a_p^n is the time-varying coefficient for the *p*th POD mode and 249 the n^{th} velocity data record, and N represents number of modes used for reconstructions. If all the POD 25 modes (i.e., N = 2048 for this study) are used in the velocity field reconstruction, it should yield the original 251 velocity data set or record. However, when a limited number of POD modes are used (i.e., N < 2048), the 252 reconstructed velocity field is referred to as a low-order reconstruction. The time-varying POD coefficients 253 (a_n) are obtained by projecting the velocity data field from each record onto the POD modes. For this 254 study, there are 3140 and 2478 time varying coefficients associated with each POD mode for non-slack and 255 slack tidal conditions respectively. The relevance of these POD modes (ϕ_p) in representing the coherent or 256 energetic structures can be ascertained by analyzing the energy captured by each of these modes (i.e., λ_p) 257 and also by analyzing the time-varying coefficients associated with these modes.

²⁵⁹ Since these POD modes are optimal and orthogonal,

$$(\phi_i, \phi_j) = \delta_{ij}, \tag{12}$$

$$\langle a_i a_j^* \rangle = \delta_{ij} \lambda_i, \tag{13}$$

where δ_{ij} is the Kronecker delta, a_j^* is the conjugate of a_j , $\langle \rangle$ ensemble-averaging, and (.) represents the inner product. These relationships are used for the verification of POD results.

When applied to a turbulent data set, the POD modes can be analyzed to identify the modes that are 262 associated with non-coherent, low-energy, high frequency fluctuations in the flow field. Since the instrument 263 noise is assumed to be white noise, it is expected that the contribution from the instrument noise will be 264 non-coherent and will have low energy. Therefore, in a low-order reconstruction, the modes associated with 265 noise are excluded. Similarly, Singular Spectrum Analysis (SSA) [47] is used to obtain information about 266 the signal to noise separation when the noise is uncorrelated in time (i.e., white noise) in analysis of climatic 267 time series. Durgesh et al. [42] demonstrated the ability of POD to filter small scale fluctuations in a swirling 268 jet and turbulent wake, and capture coherent structures by performing low-order reconstructions. 269

270 4. Results

271 4.1. NAC implementation

The NAC method described in section 3 is implemented on the QC ADV data to correct for instrument noise. The results presented here will focus on the non-slack tidal condition (i.e., data records with the mean horizontal velocity magnitude greater than 0.8 m/s), since these are of greater operational interest for tidal energy turbines. However, the application in §5 emphasizes the slack conditions.

The first step in this approach is to estimate the noise variance, B, from the raw spectra [8]. At 276 frequencies greater than a characteristic frequency (f_b) , flattening of the spectra is observed, as shown in 277 Figs. 4(a) and (b). At these frequencies, the spectra are dominated by instrument noise; therefore, the 278 flattened portion of the spectra represents the energy level (or variance) contributed by instrument noise 279 [8, 10]. The area of the rectangular region extending over all frequencies, with energy levels equal to those of 280 the flattened portion of the spectra, can provide an estimate of total energy from instrument noise, since it 281 exhibits behavior similar to that of Gaussian white noise [8]. A schematic representing the total contribution 282 from instrument noise for a single component of velocity is shown in Fig. 6, the same approach is also used 283 to calculate instrument noise contribution for v and w components of velocity. This approach has also been 284 used by Nikora and Goring [8], Garcia et al. [10], Romagnoli et. al. [48] to estimate the contribution of 285 instrument noise (Doppler noise) in ADV data. Here, to obtain an accurate estimate of the energy in the 286 instrument noise, the mean energy value of the spectra from 12-16 Hz is used. 287



Figure 7: Estimated along-beam noise $n = \cos(55^\circ)\sqrt{B_{uu} + B_{vv}}$ (black dots) and a priori noise value as n = 1% of the horizontal mean flow (red).

The average noise energies (variances) obtained are $B_{uu} \sim 0.0017 m^2/s^2$ and $B_{vv} \sim 0.0010 m^2/s^2$ for the *u* and *v* horizontal components of velocity, respectively. The corresponding horizontal error velocity is $\sqrt{B_{uu} + B_{vv}}$, which is converted to along beam error with $\cos(55^\circ)$ and shown in Fig. 7 with the *a priori* 0.1% error velocity. The values and qualitative dependence on the mean flow speed are similar to [8].

The second step in the NAC approach is to calculate the auto-correlation of the true signal (i.e., $R_{uu,NAC}$ and $R_{vv,NAC}$) by subtracting the contribution of instrument noise from the auto-correlation values (i.e., R_{uu} , and R_{vv}),

$$R_{uu,NAC}(\tau) = \begin{cases} R_{uu}(\tau) - B, & \text{if } \tau = 0; \\ R_{uu}(\tau), & \text{otherwise,} \end{cases}$$
(14)

where B is the total energy or variance from the instrument noise.

The ensemble-averaged R_{uu} , R_{vv} , and R_{ww} as a function of time-lag (τ), for non-slack tidal condition, are shown in Fig. 8. As observed in the figure, the auto-correlation values approach zero with increase in τ , which is as expected for turbulent flows. Figures 9(a) and (b) show the mean R_{uu} and R_{vv} close to zero τ . As observed in the figures, the auto-correlations (i.e., R_{uu} and R_{vv}) show a spike or jump in value at zero τ , while R_{ww} shows a correlation curve without presence of a spike, as observed in Fig. 9(c). A spike in auto-correlation at zero τ is consistent with contamination by Gaussian white noise (see Eq. 3, 6, and Fig. 5).

 $R_{uu,NAC}$ and $R_{vv,NAC}$ are estimated using Eq. 14, and are shown in Figs. 9(a) and (b) respectively. As observed in the figures, the spike in auto-correlation at zero time-lag is reduced after removing the estimated contribution of instrument noise (B). These corrected auto-correlation values are then used to calculate spectra (i.e., $S_{uu,NAC}$ and $S_{vv,NAC}$) using Eq. 7. The ensemble-averaged NAC spectra for u and vcomponents of velocity, for the non-slack tidal condition, are shown in Figs. 10(a) and (b) respectively. As observed in these figures, there is more than an order of magnitude reduction in instrument noise level for both components of horizontal velocity at frequencies above f_b . Furthermore, the spectra exhibit an extended



Figure 8: Ensemble-averaged auto-correlation for non-slack tidal condition from QC ADV data for all components of velocity R_{uu} , R_{vv} , and R_{ww} .

 $f^{-5/3}$ inertial sub-range. The mean square error (MSE) of the corrected spectra from the expected $f^{-5/3}$ slope is calculated, and is shown in Fig. 11. As observed in the figure, there is significant decrease in the MSE value for NAC spectra compared with the MSE value obtained for raw spectra. A similar behavior is also observed for the slack tidal condition, as shown in Fig. 12. It should also be noted that NAC spectra from each 300 s record still exhibit significant variability, similar to the raw spectra, and ensemble averaging of several spectra is required to obtain smooth spectra.

A recent study done by Romagnoli et. al. [48] used a similar approach to estimate Doppler noise, and then used the energy in the Doppler noise to obtain corrected auto-correlation function and accurately estimate integral time length scales. However, the focus of this study is to obtain an accurate estimate of the velocity spectra for the purpose of CFD simulations. Therefore, in this work, the estimated energy in the Doppler noise was used to correct the auto-correlation function, and then the Fourier transform of the corrected auto-correlation function was used to obtain an accurate estimation of the velocity spectra.

322 4.2. POD implementation

The POD method is used to identify and attenuate the contribution of instrument noise from the QC ADV data and provide a comparison with the results obtained by NAC method since no direct observations of the true spectra at higher frequencies are available. The POD analysis is performed separately for uand v components of velocity during non-slack and slack tidal conditions. The detailed implementation and results for the non-slack condition, and certain relevant results for the slack tidal condition, are presented here.

For both components of horizontal velocity, POD modes and the energy in them are determined using the discretized POD equation, given in Eq. 10. The first six POD modes (dimensionless basis functions) obtained



Figure 9: Section of auto-correlation plot highlighting ensemble-averaged auto-correlation close to zero τ for non-slack tidal condition, showing the spike in correlation due to contribution from instrument noise (i.e., B): (a) for the *u* component of velocity, R_{uu} and $R_{uu,NAC}$, (b) for the *v* component of velocity, R_{vv} and $R_{vv,NAC}$, and (c) for *w* component of velocity, R_{ww} without presence of spikes.

for u component of velocity, which are optimized for the velocity fluctuations, are shown in Fig. 13(a)-(f) (a 331 similar result is obtained for v component of velocity, not shown). As observed from these figures, the modes 332 have a definitive structure to them and they show an increase in number of peaks and valleys with increase 333 in mode number, as well as a shift in the location of peaks and valleys. This suggests that the combination of 334 modes may identify coherent structures present in the turbulent flow data and may also represent advection 335 of coherent structures. The cumulative energy captured by the POD modes for u component of velocity is 336 shown in Fig. 14. As observed in the figure, the higher order modes have captured significantly lower energy 337 as compared to lower order POD modes. This suggests that the higher order POD modes may be associated 338 with non-coherent structures or noise which is not energetic. A similar behavior is also observed for the v339 component of velocity (not shown here). 340

A low-order reconstruction is performed as shown in Fig. 13(g). As observed in the figure, a low-order reconstruction using first six POD modes is able to accurately capture the low frequency fluctuations. However, when the 359 POD modes which capture ~ 80 percent of total energy (as can be seen from the Fig. 14) are used for the low-order reconstruction, the reconstructed velocity data almost exactly follow the original ADV data trend, while suppressing the high frequency fluctuations in the data.

In the following paragraphs, two versions of POD noise-correction, implemented for the u component of velocity, during non-slack tidal condition, are discussed in detail. These are implemented for v component of velocity as well (both non-slack and slack tidal conditions), however the implementation is not discussed in detail here because the results are similar.



Figure 10: Ensemble-averaged spectra obtained from QC ADV data, NAC, POD and Gaussian filter approaches: (a) for u component of velocity during non-slack tidal condition, and (b) for v component of velocity during non-slack tidal condition.



Figure 11: MSE of the spectra from the expected $f^{-5/3}$ slope for QC ADV data, Gaussian filter, NAC and POD approaches.



Figure 12: Ensemble-averaged spectra obtained from QC ADV data, NAC, POD and Gaussian filter approaches: (a) for u component of velocity during slack tidal condition, (b) for v component of velocity during slack tidal condition, and (c) for w component of velocity during slack tidal condition.

The first version assumes that the spectra for the energetic tidal flow follow a $f^{-5/3}$ slope in the inertial 350 sub-range of the spectra. Several low-order reconstructions are calculated using Eq. 11, where N varies from 351 1 to 2048, which yield 3410 low-order-reconstructed velocity data records (i.e., total number of records in non-352 slack tidal condition) for each value of N. Spectra are then estimated from these low-order-reconstructed 353 velocity data records for each value of N, and an ensemble-averaged spectrum is calculated from these 35 spectra. Then, the Mean Square Error (MSE) of the ensemble-averaged spectrum from the expected $f^{-5/3}$ 355 slope in the inertial sub-range (here, the frequency in the range of 1 Hz to 8 Hz) is calculated. The MSE as a 356 function of mode number (N) used for the reconstruction is shown in Fig. 15. As observed in the figure, the 357 MSE shows a significant variation with change in the mode number used for the low-order reconstruction. 358 A physical explanation for the MSE is that initially, each additional mode captures additional information 359 about coherent turbulence, but, above a certain number of POD modes (i.e., $N_{optimal}$), they are dominated 360 by noise. The ensemble-averaged spectrum (i.e., $S_{uu,POD}$) calculated from these low-order reconstructions 361 is shown in Fig. 10(a). As observed in the figure, low-order reconstruction using $N_{optimal} = 359$ modes 362 is able to accurately capture the behavior of the spectra by attenuating instrument noise, and exhibits an 363 $f^{-5/3}$ slope in the inertial sub-range. 364

The second version estimates the $N_{optimal}$ modes a priori, without assuming an $f^{-5/3}$ slope. In this approach, the λ 's are related to the TKE (or variance $\langle u'^2 \rangle$) by

$$\langle u'^2 \rangle = \frac{1}{2048} \sum_{i=1}^{2048} \lambda i.$$
 (15)

The variances for the u and v components of velocity for slack and non-slack tidal conditions are calculated directly from QC-ADV data and λ s. The variances obtained from both these approaches have identical values. This suggests that the λ s can be used to represent the total TKE from the ADV data. Now in a low-order reconstruction, if only a certain number of POD modes are used such that the cumulative TKE from the excluded POD modes is exactly equal to contribution from instrument noise i.e., B, this will yield ADV data with reduced instrument noise. The relationship between the cumulative TKE of the excluded modes (i.e., B) and $N_{optimal}$ can mathematically be defined as

$$\langle u'^2 \rangle - B = \frac{1}{2048} \sum_{i=1}^{N_{optimal}} \lambda i.$$
(16)

If the contribution from instrument noise i.e., B is known, the above equation can be used to estimate $N_{optimal}$. Using the B values from the NAC implementation results in $N_{optimal}$ values similar to the $N_{optimal}$ obtained by assuming an $f^{-5/3}$ slope. This self-consistency in the two versions of POD suggests an effective removal of noise, given a priori assumptions about either the noise or the true signal. Although POD requires significant assumptions, it has the advantage of retaining time domain information.

The ensemble-averaged spectrum (i.e., $S_{uu,POD}$) calculated from the low-order reconstructions using N_{optimal} modes is shown in Fig. 10(a). There is an order of magnitude decrease in the noise floor level



Figure 13: POD modes for non-slack tidal condition and low-order reconstruction: (a)-(f) first six POD modes for u component of velocity, and (g) u-component of velocity from ADV data record-1 along with low-order reconstruction using first 6 and 359 POD modes.

compared to the ensemble-averaged raw spectrum (i.e., S_{uu}). The POD spectrum extends the $f^{-5/3}$ inertial sub-range, and there is a decrease in the MSE error from the expected $f^{-5/3}$ slope (see Fig. 11).

A similar analysis for the v component of velocity (not presented here) shows that $N_{optimal} = 397$ POD modes. The ensemble-averaged spectrum for v component of velocity (for non-slack tidal condition) calculated from low-order reconstructions using 397 POD modes, is shown in Fig. 10(b), and exhibits a result similar to that of u component of velocity. The POD technique is also implemented for the slack tidal condition, and the resulting spectra for the slack tidal condition are shown in Fig. 12. These spectra exhibit a trend similar to that of the non-slack condition, suggesting that this approach can also be implemented in the case where turbulent flows are less energetic.

Even though the NAC and POD approaches are inherently different, they yield similar noise-corrected spectral results, corroborating the effective attenuation of instrument noise from QC ADV data. A separate comparison of the results for each of these approaches with theoretical isotropy follows in §4.4.

393 4.3. Gaussian filter implementation

The results obtained using the NAC and POD approaches are compared to results obtained using a conventional low-pass Gaussian filter, which is commonly used to remove high frequency noise [see 10, 21,



Figure 14: Cumulative energy in POD modes during non-slack tidal condition for u component of velocity.



Figure 15: Mean Square Error (MSE) for u component of velocity for non-slack tidal condition as a function of the mode number (N) used for low-order reconstructions.

 $_{236}$ 22, 23]. For this purpose, a filter with a smoothing function (w(t)) [20], given as

$$w(t) = (2\pi\sigma^2)^{-0.5} \exp^{-t^2/2\sigma^2},$$

$$\sigma = \left(\frac{\ln(0.5)^{0.5}}{-2\pi f_{50}^2}\right)^{0.5},$$
(17)

where, t is time, $f_{50} = f_D/6$, and $f_D=32$ Hz is the sampling frequency, is used. The QC ADV data are 397 filtered and used to calculate the spectra for horizontal velocity components (i.e., $S_{uu,Gauss}$ and $S_{vv,Gauss}$) 398 for non-slack tidal condition. The ensemble-averaged spectra obtained after filtering the QC ADV data are 399 shown in Fig. 10. As observed in the figure, the instrument noise in the filtered data is eliminated at higher 400 frequencies. However, spectra show a bump at a frequency of 8 Hz and shift away from the expected $f^{-5/3}$ 401 slope in the inertial sub-range. Thus, although the Gaussian low-pass filter is capable of correcting for the 402 instrument noise present at higher frequencies, it may not be able to do so at lower frequencies, resulting 403 in a bump in the spectra and a deviation from the expected $f^{-5/3}$ slope. Figure 11 shows that there is a 404 decrease in the MSE of the spectra from the expected $f^{-5/3}$ slope as compared to MSE of spectra obtained 405 from QC ADV data, but the NAC and POD methods have significant reduction in MSE. A similar result is 406 also observed for the slack tidal condition QC ADV data, as shown in Fig. 12. 407

408 4.4. Evaluation of isotropy

To evaluate the effectiveness of NAC and POD approaches in removing instrument noise from ADV data, the relationship between the horizontal and vertical spectra provided by Lumley and Terray [49] is utilized. The model spectra provided by Lumley and Terray [49] for a frozen inertial-range turbulence advecting past a fixed sensor is used to determine the ratio of spectra (R) for horizontal and vertical components. This quasi-isotropic ratio,

$$\mathbf{R} = \frac{(12/21)(S_{uu}(f) + S_{vv}(f))}{S_{ww}(f)},$$
(18)

is predicted to be $\simeq 1.0$ in the inertial sub-range for the flow near the seabed (neglecting wave motions). See 414 articles by Lumley and Terray [49], Trowbridge and Elgar [50], and Feddersen [18] for detailed derivation and 415 analyses. Figure 16 shows the R values as a function of frequency, calculated from the QC ADV data, and 416 noise removal approaches used in this study i.e., NAC, POD, and Gaussian filter techniques. As observed 417 from the figure, the spectra obtained from QC ADV data and Gaussian low-pass filtered data acquire R 418 values significantly higher than unity in the inertial sub-range of the spectra (i.e., for frequency higher than 419 2 Hz). However, for the NAC and POD techniques, R values stay close to unity for most of the inertial 420 sub-range of the spectra (i.e., for frequencies from 1-8 Hz). The spectra obtained from NAC and POD 421 approaches are consistent with the isotropic spectra suggested by [49]. In spite of the noise correction, at 422 higher frequencies (i.e., frequencies higher that 8 Hz), R value deviates significantly from its theoretical unit 423 value. This is because at these frequencies, the energy content of Doppler noise is significantly higher (even 424



Figure 16: Variation of R as a function of frequency. The horizontal dashed line represents R values of 0.8 and 2.0.

after NAC or POD technique) compared to energy content of u and v components of velocity spectra. The w component of spectra will have significantly lower energy compared to the noise contaminated spectra of the horizontal velocity components at these frequencies. Therefore, the ratio of $S_{uu} + S_{vv}/S_{ww}$ will show a significant deviation from the expected result.

429 5. Application of NAC to improve estimates of the turbulent dissipation rate

One common use of ADV spectra is to estimate the dissipation rate of TKE. In this section, we apply the NAC method to the field data and demonstrate improved estimates of the dissipation rate, especially during less energetic (i.e., slack) tidal conditions. The improvement is primarily in the confidence (reduced uncertainty) of each dissipation estimate, however the NAC method also gives dissipation estimates more consistent with an expected local TKE budget. This application is restricted to the spectra of vertical velocity; other applications might benefit from applying the NAC method to horizontal velocities as well.

The dissipation rate ϵ is estimated from the ADV vertical velocity spectra $S_{ww}(f)$ shown in Fig. 12(c)

$$S_{ww}(f) = a\epsilon^{2/3} f^{-5/3},\tag{19}$$

where f is frequency and a is the Kolmogorov constant taken to be 0.69 for the vertical component [51]. The vertical component is used because it has the lowest intrinsic Doppler noise (a result of ADV geometry). This approach utilizes Taylor's 'frozen field' hypothesis, which infers a wavenumber k spectrum as a frequency fspectrum advected past the ADV at a speed $\langle u \rangle$, such that $f = \langle u \rangle k$.

First, the raw spectra S_{ww} and NAC spectra $S_{ww,NAC}$ are calculated using five-minute bursts of the 32 Hz sampled ADV field data, which have stationary mean and variance over the burst. Next, an $f^{-5/3}$ slope is fit to the spectra in the range of 1 < f < 10 Hz. The fitting is forced to $f^{-5/3}$ using MATLAB's *roubustfit* algorithm, and the intercept is set to zero. The standard error of the fit is retained and is propagated through Eq. 19 as a measure of the uncertainty σ_{ϵ} in the resulting ϵ values. The standard error is defined as the rms error between the fit and the spectra, normalized by the number of frequency bands used in the fitting.

The dissipation rates and uncertainties from all bursts are shown in Fig. 17 as a function of the burst 448 mean horizontal tidal current $\langle u \rangle$. The dissipation rates are elevated during strong tidal flows and are 449 similar order of magnitude to estimates from other energetic tidal channels [33]. The dissipation rates from 450 the raw spectra are consistently higher than the dissipation rates from the NAC spectra. The reduction in 451 dissipation is expected owing to the reduction of velocity variance by the NAC method. The uncertainties 452 in dissipation rates from the raw spectra also are consistently higher than the uncertainties from the NAC 453 spectra. The reduction in uncertainties is a result of better fits, over a wider range of frequencies, to the 454 $f^{-5/3}$ inertial sub-range. For either method, the 16 Hz maximum frequency is still expected to be well 455 within the inertial sub-range, which should extend to $\mathcal{O}(10^2)$ Hz during slack conditions and $\mathcal{O}(10^4)$ Hz 456 during strong tidal flows (see scaling discussion in $\S32.1$). 457

The difference between methods is most pronounced during slack conditions ($\langle u \rangle < 0.8 \text{ m/s}$), which is when Doppler noise is mostly likely to contaminate the ADV measurements (because the velocity signal is small compared with the noise). Under slack conditions, the uncertainties in raw dissipation rates are almost a factor of ten larger than the corresponding uncertainties in NAC dissipation rates. During more energetic tidal conditions, the vertical velocity spectra are elevated above the noise floor at most or all frequencies, and thus there is less disparity between the methods (although an overall bias is persistent).

Lacking independent measurements for validation of the dissipation results, a reasonable requirement is for the uncertainty of each dissipation rate to be small compared with the estimate itself (i.e., $\sigma_{\epsilon} \ll \epsilon$). For the raw estimates of dissipation, this condition is only met during strong tidal flows ($\langle u \rangle > 0.8$ m/s in Fig. 17). For the NAC estimates of dissipation, this condition is met during all except the weakest tidal flows ($\langle u \rangle > 0.1$ m/s in Fig. 17). Thus, the NAC method extends the range of conditions in which the turbulent dissipation rate can be estimated with high confidence.

470 Another approach to evaluate the dissipation results is to assess the TKE budget,

$$\frac{D}{Dt}\left(TKE\right) + \nabla \cdot \mathcal{T} = \mathcal{P} - \epsilon, \tag{20}$$

where $\frac{D}{Dt}$ is the material derivative (of the mean flow), \mathcal{T} is the turbulent transport, \mathcal{P} is production (via shear and buoyancy) and ϵ is dissipation rate (loss to heat and sound). In a well-developed turbulent boundary layer, a balance between production and dissipation is expected. Furthermore, in a well-mixed environment, the production term will be dominated by Reynolds stresses acting on the mean shear $\mathcal{P} =$ $-\langle u'w' \rangle \frac{d\overline{u}}{dz}$, and buoyancy production can be neglected. (This assumption is corroborated by measurements



Figure 17: Dissipation rates (top) and uncertainties (bottom) versus mean horizontal speed obtained from raw spectra (red symbols) and NAC spectra (blue symbols).

of salinity stratification, using CTDs mounted at 1.85 and 2.55 m above the seabed on the ADV tripod, which showed < 0.05 PSU difference over all tidal conditions.) Here, Reynolds stresses are calculated directly from the ADV data, after rotation to principal axes, and the shear is calculated from collocated ADCP data with 0.5 m vertical resolution [see 30]. There is, of course, noise contamination in the estimation of Reynolds stresses $\langle u'w' \rangle$ from ADV, because u' and w' share noise from the same acoustic beams. However, this has a limited affect on the estimates because of the high frequency nature of the noise [9]. (This is in contrast to estimating the dissipation rate, which requires fidelity at high frequencies.)

The shear production and dissipation rates are compared in Fig. 18. The raw estimates of dissipation 483 exceed shear production consistently. The NAC estimates of dissipation, by contrast, are scattered above 484 and below the production. The rms error of an assumed $P - \epsilon$ balance during all tidal conditions is 4.7×10^{-5} 485 for raw estimates and 1.6×10^{-5} for NAC estimates. As in the comparison of uncertainty, the difference in 486 methods is most pronounced during less energetic conditions (i.e., $\epsilon < 10^{-5}$ in Fig. 18). The rms error of an 487 assumed $P - \epsilon$ balance during slack tidal conditions is 2.0×10^{-5} for the raw estimates and 0.6×10^{-5} for the 488 NAC estimates. Thus, results from the NAC method are more consistent, over a wider range of conditions, 489 with the expected dynamics of a turbulent bottom boundary layer. 490

491 6. Conclusions

ADV measurements were collected from a proposed tidal energy site and used to evaluate two methods for 492 noise-correction of velocity spectra. The raw spectra were flat at higher frequencies, consistent with previous 493 studies on Doppler instrument noise. Both NAC and POD approaches were effective in decreasing the noise 494 contamination of spectra, especially for high frequencies. The attenuation of instrument noise extends 495 observations of the $f^{-5/3}$ inertial sub-range to more frequencies, and thus gives a better fit (i.e., more 496 points) when estimating the dissipation rate. Moreover, a wider subrange obtained from these approaches 497 may also be helpful in providing an accurate estimation of the dissipation rate when ADV data are further 498 contaminated by waves and platform vibrations at select frequencies. 499

In comparison, the NAC and POD techniques show better agreement with an expected $f^{-5/3}$ slope than a conventional low-pass Gaussian filter approach. In the later approach, instrument noise is only removed above the cut-off frequency of the filter, and hence, the spectra may not be accurate just below the cut-off frequency.

The NAC approach provides a straightforward method for attenuating instrument noise in velocity spectra and does not require prior knowledge of the spectral shape. However, the NAC approach does not provide the noise-corrected data in the temporal domain as all the operations required for NAC approach are performed in the frequency domain. It should also be noted that the NAC approach is implemented on the assumption that the instrument noise has unlimited bandwidth, which needs to be investigated further. The



Figure 18: Shear production versus dissipation obtained from raw spectra (red symbols) and NAC spectra (blue symbols). All tidal conditions shown, processed in five-minute bursts. The dashed line indicates a 1:1 balance.

⁵⁰⁹ POD approach is capable of reducing instrument noise in spectra and in the temporal domain. However,

the POD approach is more computationally intensive, requires prior knowledge of the noise level or spectral

shape, and may not work in flows without dominant large scale coherent structures.

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