Sequence comparison: Score matrices
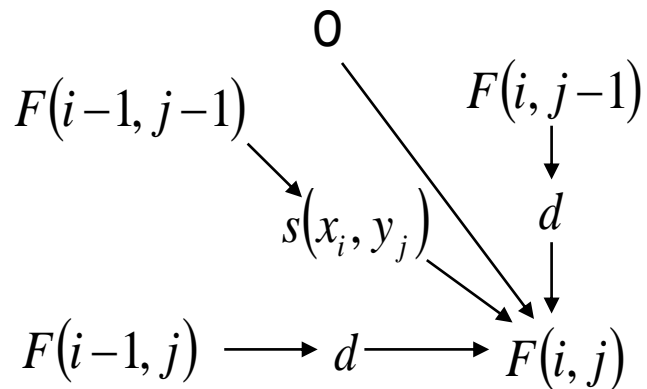
Genome 559: Introduction to Statistical and Computational Genomics

Prof. James H. Thomas

Local alignment - review

	A	C	G	T
A	2	-7	-5	-7
C	-7	2	-7	-5
G	-5	-7	2	-7
T	-7	-5	-7	2

d = -5

$$F(i-1,j-1)$$
$$0$$
$$F(i,j-1)$$
$$s(x_i, y_j)$$
$$d$$
$$F(i-1,j) \longrightarrow d \longrightarrow F(i,j)$$

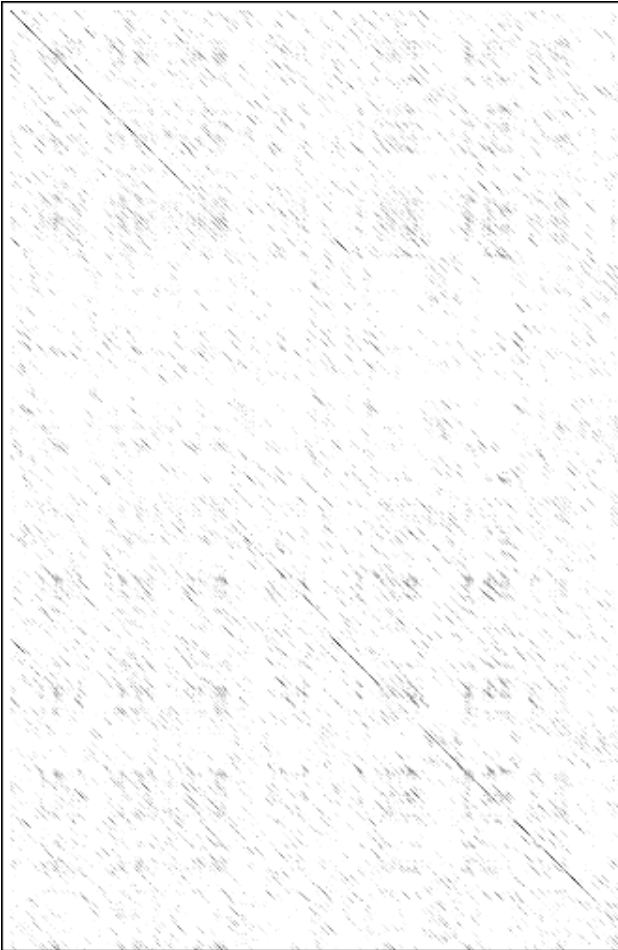|		A	A	G
	0	0	0	0
A	0	2	2	0
G	0	0	0	4
C	0	0	0	0

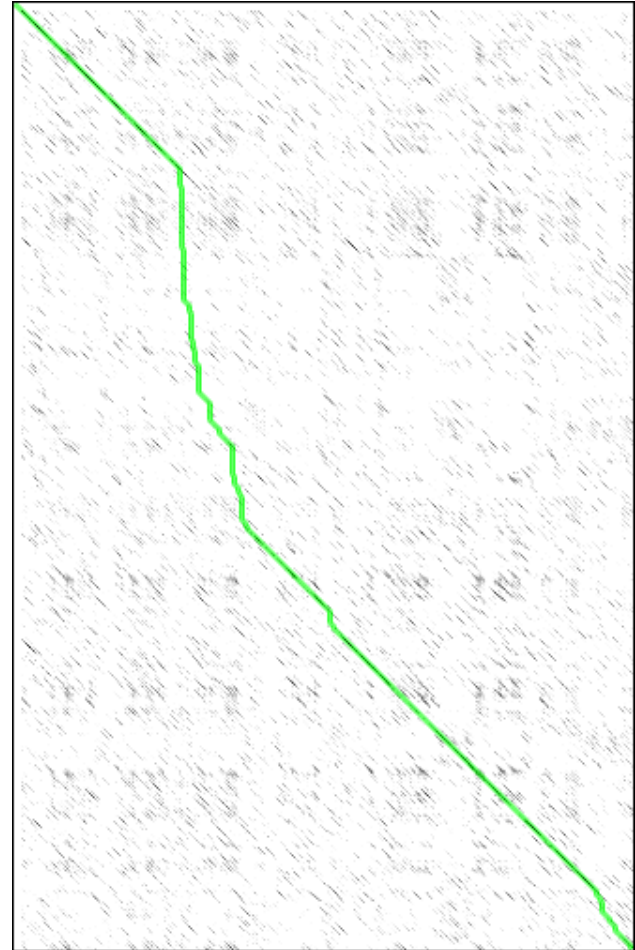(no arrow means no preceding alignment)

Local alignment - review

- Two differences from global alignment:

  - If a score is negative, replace with 0.

  - Traceback from the highest score in the matrix and continue until you reach 0.

dot plot of two DNA sequences

overlay of the global DP alignment path

What would the best <u>local</u> alignment (probably) look like?

Score Matrices

Where do all those numbers come from?

	A	C	G	T
A	2	-7	-5	-7
C	-7	2	-7	-5
G	-5	-7	2	-7
T	-7	-5	-7	2

Protein score matrices

• Quantitatively represent the degree of conservation of typical amino acid residues over evolutionary time.

• All possible amino acid changes are represented (matrix of size at least 20 x 20).

• Most commonly used are several different BLOSUM matrices derived for different degrees of evolutionary divergence.

• DNA score matrices are conceptually similar.
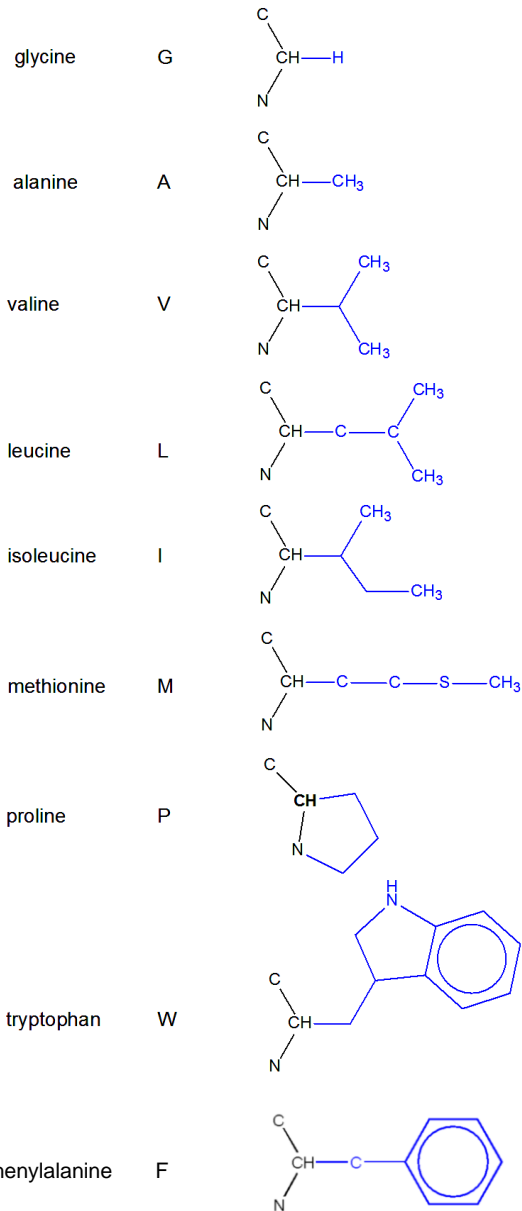
BLOSUM62 Score Matrix

regular 20 amino acids

BLOSUM Clustered Scoring Matrix in 1/2 Bit Units
Cluster Percentage: >= 62

	A	R	N	D	C	Q	E	G	H	I	L	K	M	F	P	S	T	W	Y	V	B	Z	X	*
A	4	-1	-2	-2	0	-1	-1	0	-2	-1	-1	-1	-1	-2	-1	1	0	-3	-2	0	-2	-1	0	-4
R	-1	5	0	-2	-3	1	0	-2	0	-3	-2	2	-1	-3	-2	-1	-1	-3	-2	-3	-1	0	-1	-4
N	-2	0	6	1	-3	0	0	0	1	-3	-3	0	-2	-3	-2	1	0	-4	-2	-3	3	0	-1	-4
D	-2	-2	1	6	-3	0	2	-1	-1	-3	-4	-1	-3	-3	-1	0	-1	-4	-3	-3	4	1	-1	-4
C	0	-3	-3	-3	9	-3	-4	-3	-3	-1	-1	-3	-1	-2	-3	-1	-1	-2	-2	-1	-3	-3	-2	-4
Q	-1	1	0	0	-3	5	2	-2	0	-3	-2	1	0	-3	-1	0	-1	-2	-1	-2	0	3	-1	-4
E	-1	0	0	2	-4	2	5	-2	0	-3	-3	1	-2	-3	-1	0	-1	-3	-2	-2	1	4	-1	-4
G	0	-2	0	-1	-3	-2	-2	6	-2	-4	-4	-2	-3	-3	-2	0	-2	-2	-3	-3	-1	-2	-1	-4
H	-2	0	1	-1	-3	0	0	-2	8	-3	-3	-1	-2	-1	-2	-1	-2	-2	2	-3	0	0	-1	-4
I	-1	-3	-3	-3	-1	-3	-3	-4	-3	4	2	-3	1	0	-3	-2	-1	-3	-1	3	-3	-3	-1	-4
L	-1	-2	-3	-4	-1	-2	-3	-4	-3	2	4	-2	2	0	-3	-2	-1	-2	-1	1	-4	-3	-1	-4
K	-1	2	0	-1	-3	1	1	-2	-1	-3	-2	5	-1	-3	-1	0	-1	-3	-2	-2	0	1	-1	-4
M	-1	-1	-2	-3	-1	0	-2	-3	-2	1	2	-1	5	0	-2	-1	-1	-1	-1	1	-3	-1	-1	-4
F	-2	-3	-3	-3	-2	-3	-3	-3	-1	0	0	-3	0	6	-4	-2	-2	1	3	-1	-3	-3	-1	-4
P	-1	-2	-2	-1	-3	-1	-1	-2	-2	-3	-3	-1	-2	-4	7	-1	-1	-4	-3	-2	-2	-1	-2	-4
S	1	-1	1	0	-1	0	0	0	-1	-2	-2	0	-1	-2	-1	4	1	-3	-2	-2	0	0	0	-4
T	0	-1	0	-1	-1	-1	-1	-2	-2	-1	-1	-1	-1	-2	-1	1	5	-2	-2	0	-1	-1	0	-4
W	-3	-3	-4	-4	-2	-2	-3	-2	-2	-3	-2	-3	-1	1	-4	-3	-2	11	2	-3	-4	-3	-2	-4
Y	-2	-2	-2	-3	-2	-1	-2	-3	2	-1	-1	-2	-1	3	-3	-2	-2	2	7	-1	-3	-2	-1	-4
V	0	-3	-3	-3	-1	-2	-2	-3	-3	3	1	-2	1	-1	-2	-2	0	-3	-1	4	-3	-2	-1	-4
B	-2	-1	3	4	-3	0	1	-1	0	-3	-4	0	-3	-3	-2	0	-1	-4	-3	-3	4	1	-1	-4
Z	-1	0	0	1	-3	3	4	-2	0	-3	-3	1	-1	-3	-1	0	-1	-3	-2	-2	1	4	-1	-4
X	0	-1	-1	-1	-2	-1	-1	-1	-1	-1	-1	-1	-1	-1	-2	0	0	-2	-1	-1	-1	-1	-1	-4
*	-4	-4	-4	-4	-4	-4	-4	-4	-4	-4	-4	-4	-4	-4	-4	-4	-4	-4	-4	-4	-4	-4	-4	1

ambiguity codes and stop (B and Z are historical)

Amino acid structures

Hydrophobic

glycine	G	
alanine	A	
valine	V	
leucine	L	
isoleucine	I	
methionine	M	
proline	P	
tryptophan	W	
phenylalanine	F	

Polar

cysteine	C	
serine	S	
threonine	T	
tyrosine	Y	
asparagine	N	
glutamine	Q	

Charged

histidine	H	
lysine	K	
arginine	R	
aspartate	D	
glutamate	E	
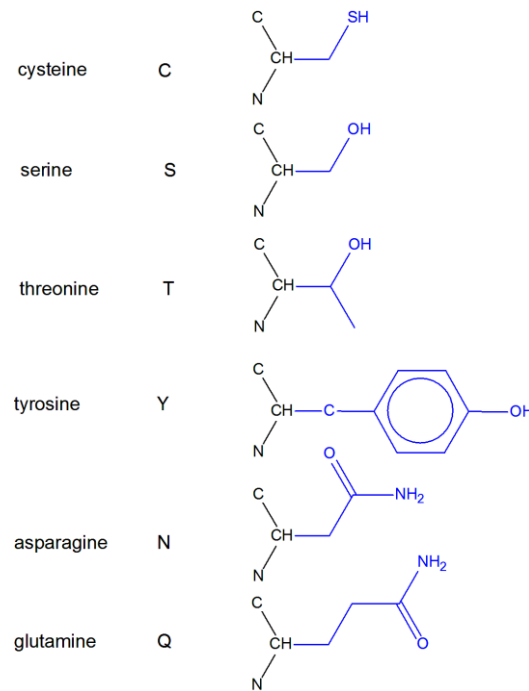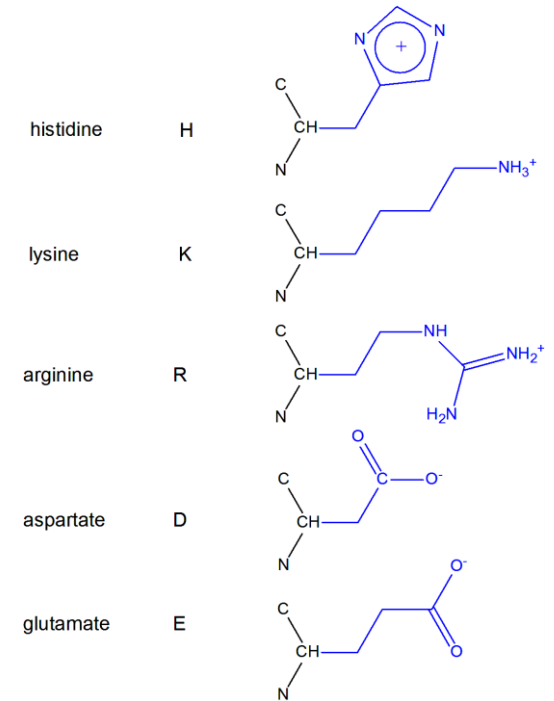
BLOSUM62 Score Matrix

	A	R	N	D	C	Q	E	G	H	I	L	K	M	F	P	S	T	W	Y	V
A	4	-1	-2	-2	0	-1	-1	0	-2	-1	-1	-1	-1	-2	-1	1	0	-3	-2	0
R	-1	5	0	-2	-3	1	0	-2	0	-3	-2	2	-1	-3	-2	-1	-1	-3	-2	-3
N	-2	0	6	1	-3	0	0	0	1	-3	-3	0	-2	-3	-2	1	0	-4	-2	-3
D	-2	-2	1	6	-3	0	2	-1	-1	-3	-4	-1	-3	-3	-1	0	-1	-4	-3	-3
C	0	-3	-3	-3	9	-3	-4	-3	-3	-1	-1	-3	-1	-2	-3	-1	-1	-2	-2	-1
Q	-1	1	0	0	-3	5	2	-2	0	-3	-2	1	0	-3	-1	0	-1	-2	-1	-2
E	-1	0	0	2	-4	2	5	-2	0	-3	-3	1	-2	-3	-1	0	-1	-3	-2	-2
G	0	-2	0	-1	-3	-2	-2	6	-2	-4	-4	-2	-3	-3	-2	0	-2	-2	-3	-3
H	-2	0	1	-1	-3	0	0	-2	8	-3	-3	-1	-2	-1	-2	-1	-2	-2	2	-3
I	-1	-3	-3	-3	-1	-3	-3	-4	-3	4	2	-3	1	0	-3	-2	-1	-3	-1	3
L	-1	-2	-3	-4	-1	-2	-3	-4	-3	2	4	-2	2	0	-3	-2	-1	-2	-1	1
K	-1	2	0	-1	-3	1	1	-2	-1	-3	-2	5	-1	-3	-1	0	-1	-3	-2	-2
M	-1	-1	-2	-3	-1	0	-2	-3	-2	1	2	-1	5	0	-2	-1	-1	-1	-1	1
F	-2	-3	-3	-3	-2	-3	-3	-3	-1	0	0	-3	0	6	-4	-2	-2	1	3	-1
P	-1	-2	-2	-1	-3	-1	-1	-2	-2	-3	-3	-1	-2	-4	7	-1	-1	-4	-3	-2
S	1	-1	1	0	-1	0	0	0	-1	-2	-2	0	-1	-2	-1	4	1	-3	-2	-2
T	0	-1	0	-1	-1	-1	-1	-2	-2	-1	-1	-1	-1	-2	-1	1	5	-2	-2	0
W	-3	-3	-4	-4	-2	-2	-3	-2	-2	-3	-2	-3	-1	1	-4	-3	-2	11	2	-3
Y	-2	-2	-2	-3	-2	-1	-2	-3	2	-1	-1	-2	-1	3	-3	-2	-2	2	7	-1
V	0	-3	-3	-3	-1	-2	-2	-3	-3	3	1	-2	1	-1	-2	-2	0	-3	-1	4

Good scores – chemically similar

Bad scores – chemically dissimilar

Amino acid structures

Hydrophobic

glycine	G	
alanine	A	
valine	V	
leucine	L	
isoleucine	I	
methionine	M	
proline	P	
tryptophan	W	

Polar

cysteine	C
serine	S
threonine	T
tyrosine	Y
asparagine	N
glutamine	Q

Charged

histidine	H
lysine	K
arginine	R
aspartate	D
glutamate	E
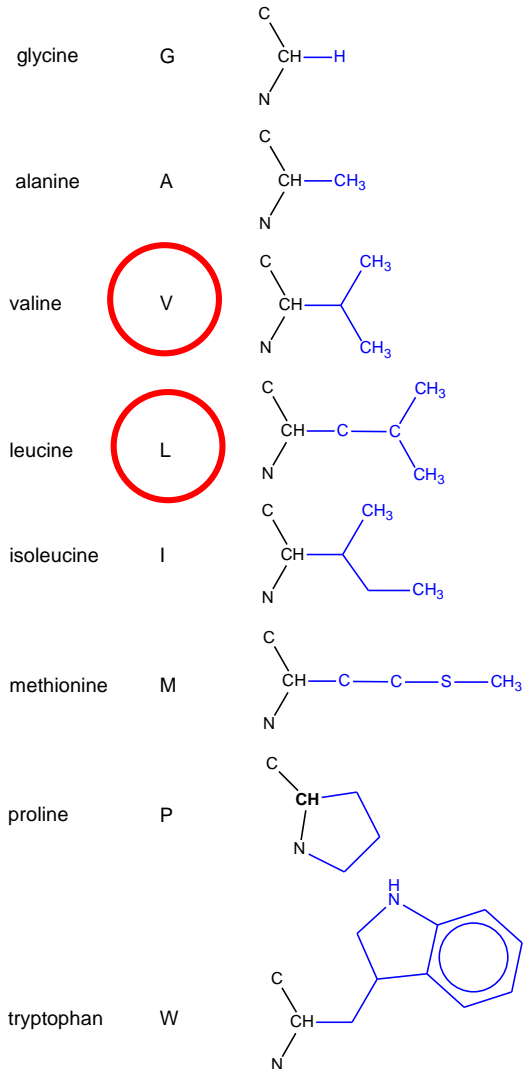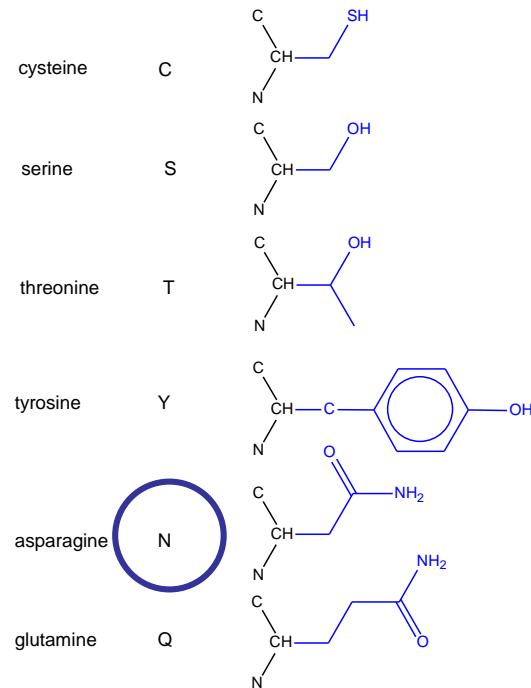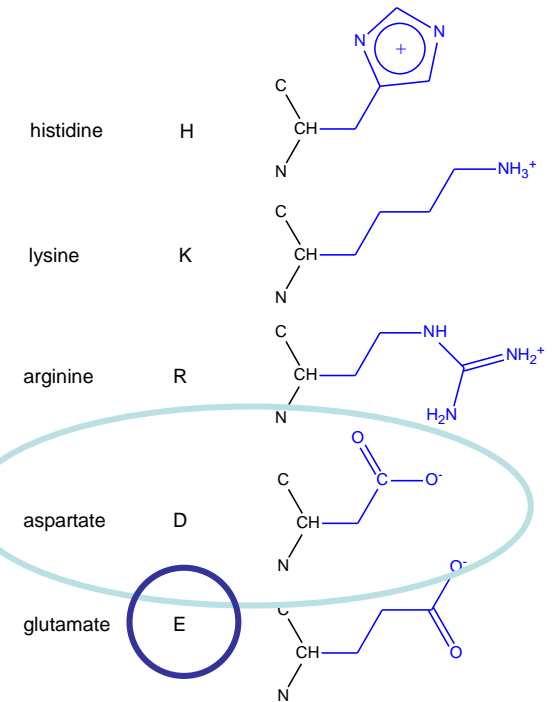
Deriving BLOSUM scores

- Find sets of sequences whose alignment is thought to be correct (this is partly circular - requires alignment).

- Measure how often various amino acid pairs occur in the alignments.

- Normalize to the expected frequency of amino acid pairs <u>randomly</u> in the same set of alignments.

- Derive a log-odds score for aligned vs. random.

Example of alignment <u>block</u> (the BLO part of BLOSUM)

31 positions (columns)
61 sequences (rows)

• Thousands of such blocks go into computing a single BLOSUM matrix.

• Represent full diversity of sequences.

• Results are summed over all columns of all blocks.
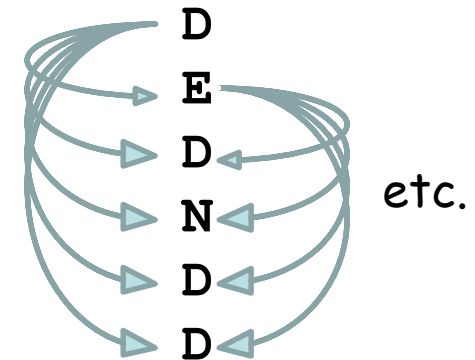
Pair frequency *vs.* expectation

Actual aligned pair frequency:

$$q_{ij} = \frac{1}{T} \sum c_{ij}$$

this is called the sum of pairs (the SUM part of BLOSUM)

where c_{ij} is the count of ij pairs and T is the total pair count.

Sample column from an alignment block:

D
E
D
N
D
D

etc.

6 D-D pairs
4 D-E pairs
4 D-N pairs
1 E-N pair

Randomly expected pair frequency:

$$e_{aa} = p_a p_a$$

$$e_{ab} = p_a p_b + p_b p_a = 2 p_a p_b$$

where p_a and p_b are the overall probabilities (frequencies) of specific residues a and b.

(a multiple alignment of N sequences is the equivalent of all the pairwise alignments, which number (N)(N-1)/2.)

Log-odds score calculation (so adding scores == multiplying probabilities)

$$s_{ij} = \log_2 \frac{q_{ij}}{e_{ij}}$$

counted pair frequency

expected random pair frequency

For computational speed often rounded to nearest integer and (to reduce round-off error) they are often multiplied by 2 (or more) first, giving a "half-bit" score:

$$\text{matrixScore} = (\text{rounded}) \; 2\log_2 \frac{q_{ij}}{e_{ij}}$$

(computers can add integers faster than floats)

	A	R	N	D	C	Q	E	G	H	I	L	K	M	F	P	S	T	W	Y	V
A	4	-1	-2	-2	0	-1	-1	0	-2	-1	-1	-1	-1	-2	-1	1	0	-3	-2	0
R	-1	5	0	-2	-3	1	0	-2	0	-3	-2	2	-1	-3	-2	-1	-1	-3	-2	-3
N	-2	0	6	1	-3	0	0	0	1	-3	-3	0	-2	-3	-2	1	0	-4	-2	-3
D	-2	-2	1	6	-3	0	2	-1	-1	-3	-4	-1	-3	-3	-1	0	-1	-4	-3	-3
C	0	-3	-3	-3	9	-3	-4	-3	-3	-1	-1	-3	-1	-2	-3	-1	-1	-2	-2	-1
Q	-1	1	0	0	-3	5	2	-2	0	-3	-2	1	0	-3	-1	0	-1	-2	-1	-2
E	-1	0	0	2	-4	2	5	-2	0	-3	-3	1	-2	-3	-1	0	-1	-3	-2	-2
G	0	-2	0	-1	-3	-2	-2	6	-2	-4	-4	-2	-3	-3	-2	0	-2	-2	-3	-3
H	-2	0	1	-1	-3	0	0	-2	8	-3	-3	-1	-2	-1	-2	-1	-2	-2	2	-3
I	-1	-3	-3	-3	-1	-3	-3	-4	-3	4	2	-3	1	0	-3	-2	-1	-3	-1	3
L	-1	-2	-3	-4	-1	-2	-3	-4	-3	2	4	-2	2	0	-3	-2	-1	-2	-1	1
K	-1	2	0	-1	-3	1	1	-2	-1	-3	-2	5	-1	-3	-1	0	-1	-3	-2	-2
M	-1	-1	-2	-3	-1	0	-2	-3	-2	1	2	-1	5	0	-2	-1	-1	-1	-1	1
F	-2	-3	-3	-3	-2	-3	-3	-3	-1	0	0	-3	0	6	-4	-2	-2	1	3	-1
P	-1	-2	-2	-1	-3	-1	-1	-2	-2	-3	-3	-1	-2	-4	7	-1	-1	-4	-3	-2
S	1	-1	1	0	-1	0	0	0	-1	-2	-2	0	-1	-2	-1	4	1	-3	-2	-2
T	0	-1	0	-1	-1	-1	-1	-2	-2	-1	-1	-1	-1	-2	-1	1	5	-2	-2	0
W	-3	-3	-4	-4	-2	-2	-3	-2	-2	-3	-2	-3	-1	1	-4	-3	-2	11	2	-3
Y	-2	-2	-2	-3	-2	-1	-2	-3	2	-1	-1	-2	-1	3	-3	-2	-2	2	7	-1
V	0	-3	-3	-3	-1	-2	-2	-3	-3	3	1	-2	1	-1	-2	-2	0	-3	-1	4

BLOSUM62 matrix
(half-bit scores)

(9 half-bits = 4.5 bits)

Frequency of C residue
over all proteins: 0.0162
(you have to look this up)

Reverse calculation of aligned C–C pair frequency in BLOSUM data set:

C–C $\quad \dfrac{q_{cc}}{e_{cc}} = 2^{(4.5)} = 22.63 \qquad e_{cc} = 0.0162 * 0.0162 = 0.000262$

thus $\quad q_{cc} = 22.63 * 0.000262 = 0.00594$

(in words, C-C pairs are 22.6 times more frequent than you would expect by chance)

Constructing Blocks

- Blocks are ungapped alignments of multiple sequences, usually 20 to 100 amino acids long.

- Cluster the members of each block according to their percent identity.

- Make pair counts and score matrix from a large collection of similarly clustered blocks.

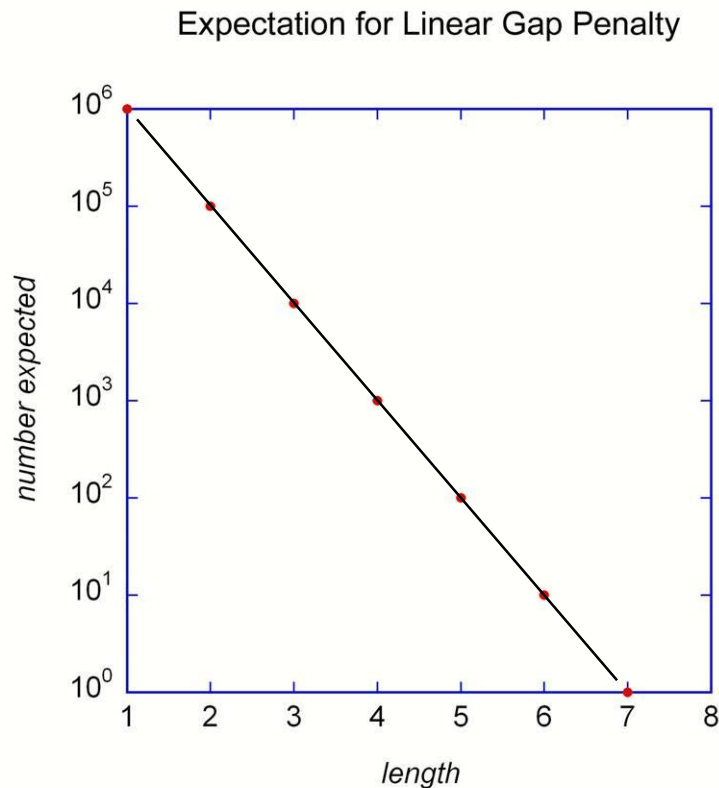- Each BLOSUM matrix is named for the <u>percent identity</u> cutoff in step 2 (e.g. BLOSUM70 for 70% identity).

Gap (indel) scores

Randomly Distributed Gaps

if $p_g = k$ (probability of a gap at each position in the sequence)

then $P(g_1) = k, P(g_2) = k^2, ..., P(g_n) = k^n$

Expectation for Linear Gap Penalty

[note - the <u>slope</u> of the line in this plot will vary according to the frequency of gaps, but it will always be linear]

Distribution of real alignment gap lengths in a large set of X-ray structure-aligned proteins
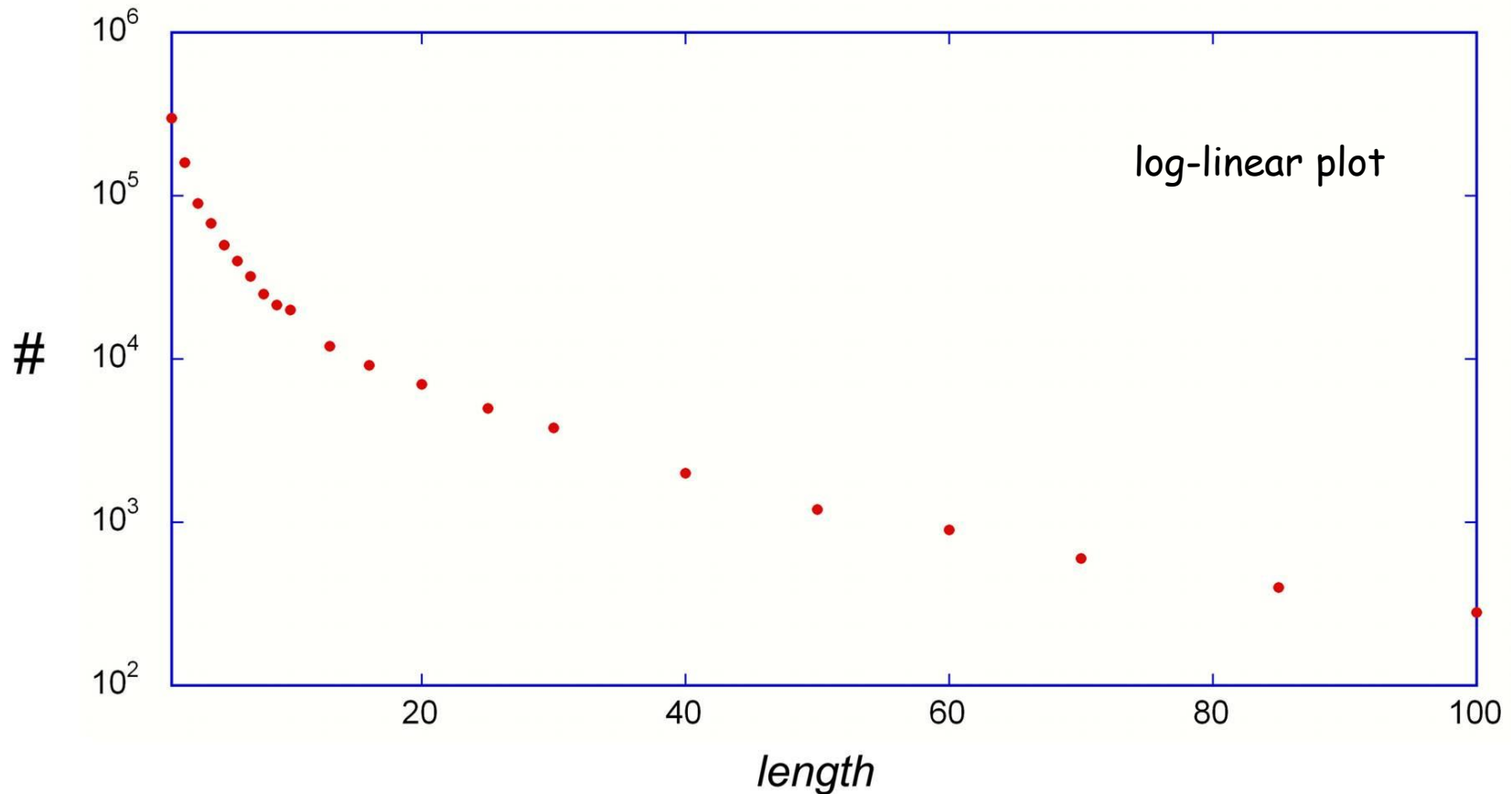
Nowhere near linear - hence the use of affine gap penalties (there ideally would be several levels of decreasing affine penalties)

What you should know

- How a score matrix is derived

- What the scores mean probabilistically

- Why gap penalties should be affine