

Names (must be present):

In class and on the exam, you considered the N-term Taylor series approximation ($k=0:N-1$) for $\exp(x)$ (e^x).

For $x=4$, the result for the error bound is:

N	8	9	10
f(4) exact	54.598	54.598	54.598
Rel Error %	5.95%	2.38%	0.88%

With 8 terms, the series result has a relative error upper bound of 5.95%. By increasing to 10 terms, the error bound drops to 0.88%.

Download the demo m-file *ExpTaylorTerm.m* from “set 4” to use here with Matlab. When called as $y = \text{ExpTaylorTerm}(x, n)$, y is the n -term approximation to $\exp(x)$.

1. To be sure that you know how to invoke this function, use Matlab: to calculate the 8-term approximation to $\exp(4)$, to calculate the exact answer $\exp(4)$, and to report the relative error $\text{abs}((\text{exact}-\text{approx})/(\text{exact}))$.
Your relative percentage error should be less than the bound above but greater than 5%..
Write it down:
2. Calculate the 8-term approx to $\exp(2)$ with the function provided. What is the relative (in percentage) error of this result:
3. Directly from this result for $\exp(2)$, obtain an estimate of $\exp(4)$ and calculate its relative (in percentage) error. (*Do not call ExpTaylorTerm for $x=4$ here.*)
4. Calculate the 8-term approx to $\exp(1)$ with the function provided. What is the relative (in percentage) error of this result:
5. Directly from this result for $\exp(1)$, obtain an estimate of $\exp(4)$ and calculate its relative (in percentage) error. (*Do not call ExpTaylorTerm for $x=4$ here.*)

See reverse side