

## Part 1.

$$y_i = \sum_{k=1}^n a_{ik} x_k$$

- Given the matrix-vector product  
 $\mathbf{y} = \mathbf{A}\mathbf{x}$   
where  $\mathbf{y}$  is an  $(r \times 1)$  column vector,  
 $\mathbf{x}$  is an  $(n \times 1)$  and  $\mathbf{A}$  is an  $(r \times n)$  matrix, write pseudo code for a suitable algorithm.
- Estimate in terms of  $r$  and  $n$  the number of floating point operations (multiplies, additions and subtractions) in this algorithm.

## Part II

Given the algorithm for the row-ordered matrix vector product:

```
%compute the Ax product
y = zeros(m,1);
for i = 1:m
    y(i) = 0;
    for j = 1:n
        y(i) = y(i) + A(i,j)*x(j);
    end
end
```

$$\begin{pmatrix} a_{11} & a_{12} & a_{13} & a_{14} & a_{15} & a_{16} \\ 0 & a_{22} & a_{23} & a_{24} & a_{25} & a_{26} \\ 0 & 0 & a_{33} & a_{34} & a_{35} & a_{36} \\ 0 & 0 & 0 & a_{44} & a_{45} & a_{46} \\ 0 & 0 & 0 & 0 & a_{55} & a_{56} \\ 0 & 0 & 0 & 0 & 0 & a_{66} \end{pmatrix}$$

Modify as needed for the case where  $\mathbf{A}$  is *upper triangular*

See reverse side

### Part III

$$C_{kj} = \sum_{i=1}^r A_{ki} B_{ij}$$

- Given the matrix-matrix product  
 $\mathbf{C}=\mathbf{A}\mathbf{B}$   
where  $\mathbf{A}$  is an  $(m \times r)$  matrix,  $\mathbf{B}$  is an  $(r \times n)$  matrix and  $\mathbf{C}$  is an  $(m \times n)$  matrix write pseudo code for a suitable algorithm.
- Estimate in terms of  $m$ ,  $n$ , and  $r$  the number of floating point operations (multiplies, additions and subtractions) in this algorithm.

See reverse side