

Econ 582
Midterm Exam

This is an open book exam. You have 1 hour and 30 minutes to complete the exam.
Please write short answers to each question.

Time Series Models

1. Consider the following model for observed real GDP, y_t , as a function of consumption, c_t , and saving, s_t :

$$y_t = c_t + s_t$$

$$c_t = \mu + c_{t-1} + v_t, \quad c_0 \text{ is a fixed constant}$$

$$s_t = u_t$$

$$\begin{pmatrix} v_t \\ u_t \end{pmatrix} \sim iid N \left(\begin{pmatrix} 0 \\ 0 \end{pmatrix}, \begin{pmatrix} \sigma_v^2 & 0 \\ 0 & \sigma_u^2 \end{pmatrix} \right)$$

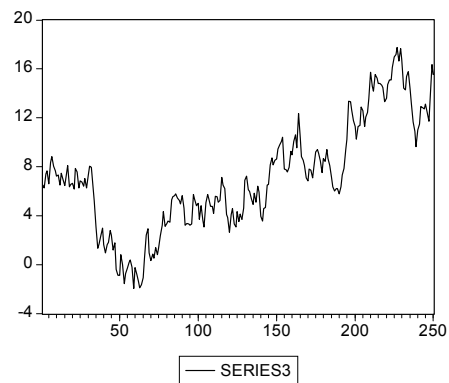
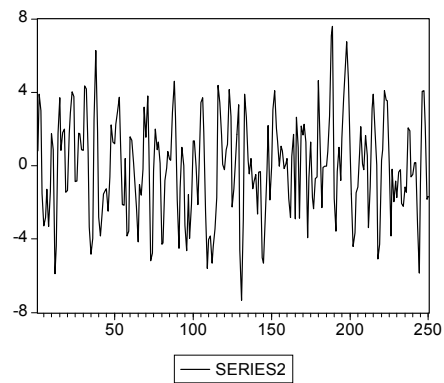
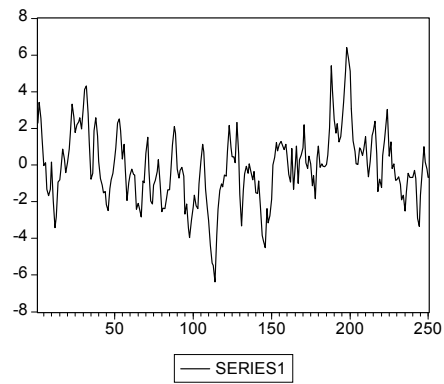
- a. Is y_t covariance stationary? Justify your answer.

Consider the first difference of y_t :

$$\Delta y_t = \Delta c_t + \Delta s_t = (\mu + v_t) + (u_t - u_{t-1}).$$

- b. Compute $E[\Delta y_t]$, $\text{var}(\Delta y_t)$ and $\text{cov}(\Delta y_t, \Delta y_{t-j})$ for $j = 1, 2, \dots$. Based on your computations, is Δy_t covariance stationary?
- c. Based on your computations above, what $\text{ARMA}(p, q)$ model describes the behavior of Δy_t ?

2. Below are plots of some simulated time series and the corresponding sample autocovariance functions.



- a. What ARMA(p, q) models would you choose to describe the above 3 series? Justify your answers.

Panel Data

Consider the following gasoline demand equation:

$$\ln\left(\frac{Gas}{Car}\right)_{it} = \beta_0 + \beta_1 \ln\left(\frac{Y}{N}\right)_{it} + \beta_2 \ln\left(\frac{P_{MG}}{P_{GDP}}\right)_{it} + \beta_3 \ln\left(\frac{Car}{N}\right)_{it} + \varepsilon_{it}$$

where Gas/Car is motor gasoline consumption per auto, Y/N is real per capita income, P_{MG}/P_{GDP} is real motor gasoline price and Car/N denotes the stock of cars per capita. The panel data set consists of annual observations across 18 OECD countries ($i = 1, \dots, 18$) covering the period 1960 – 1978 ($t = 1, \dots, 19$).

- Under what conditions is the random effects (RE) estimator appropriate?
- Briefly describe how you would compute the RE estimator. (Hint: You can give an analytic answer or you can describe how you would compute the estimator in Eviews)
- Under what conditions is the fixed effects (FE) estimator appropriate?
- Briefly describe how you would compute the FE estimator. (Hint: You can give an analytic answer or you can describe how you would compute the estimator in Eviews)
- For the above application, which estimator would you use? Justify your answer.

Multi-Equation GMM

Consider the multi-equation investment model

$$\begin{aligned} y_{it} &= \delta_{i0} + \delta_{i1}F_{it} + \delta_{i2}C_{it} + \varepsilon_{it} \\ &= \mathbf{z}_{it}'\boldsymbol{\delta}_i + \varepsilon_{it}, \quad (i = 1, \dots, N; t = 1, \dots, T) \end{aligned}$$

where

y_{it} = gross investment of firm i in year t

F_{it} = denotes market value of firm i at the end of the previous year t

C_{it} = value of the stock of plant and equipment for firm i at the end of the previous year t .

- a. Write the system of equations as a “big giant regression” of the form

$$\mathbf{y} = \mathbf{Z}\boldsymbol{\delta} + \boldsymbol{\varepsilon}$$

Suppose that z_{im} is predetermined for every equation ($E[z_{it}\varepsilon_{js}] = 0 \forall i, j, t, s$) and that the errors are contemporaneously correlated across equations.

- b. What estimator would you use if you think that the errors are not conditionally homoskedastic? Briefly describe how you would compute this estimator. (Hint: You can give an analytic answer or you can describe how you would compute the estimator in Eviews)
- c. What estimator would you use if you think that the errors are conditionally homoskedastic? Briefly describe how you would compute this estimator. (Hint: You can give an analytic answer or you can describe how you would compute the estimator in Eviews)
- d. Suppose the errors are conditionally homoskedastic. Consider testing the hypothesis that the coefficients are the same across equations:

$$H_0 : \delta_1 = \dots = \delta_M$$

Describe how you would test this hypothesis. (Hint: You can give an analytic answer or you can describe how you would compute the test in Eviews)