

**$10^{11}$  neurons**

**$(10^5 \text{ per mm}^3)$**

**$10^{15}$  synapses**

from *Neuroscience: Exploring the Brain* by M.F. Bear, B.W. Connors, and M.A. Paradiso, 2001

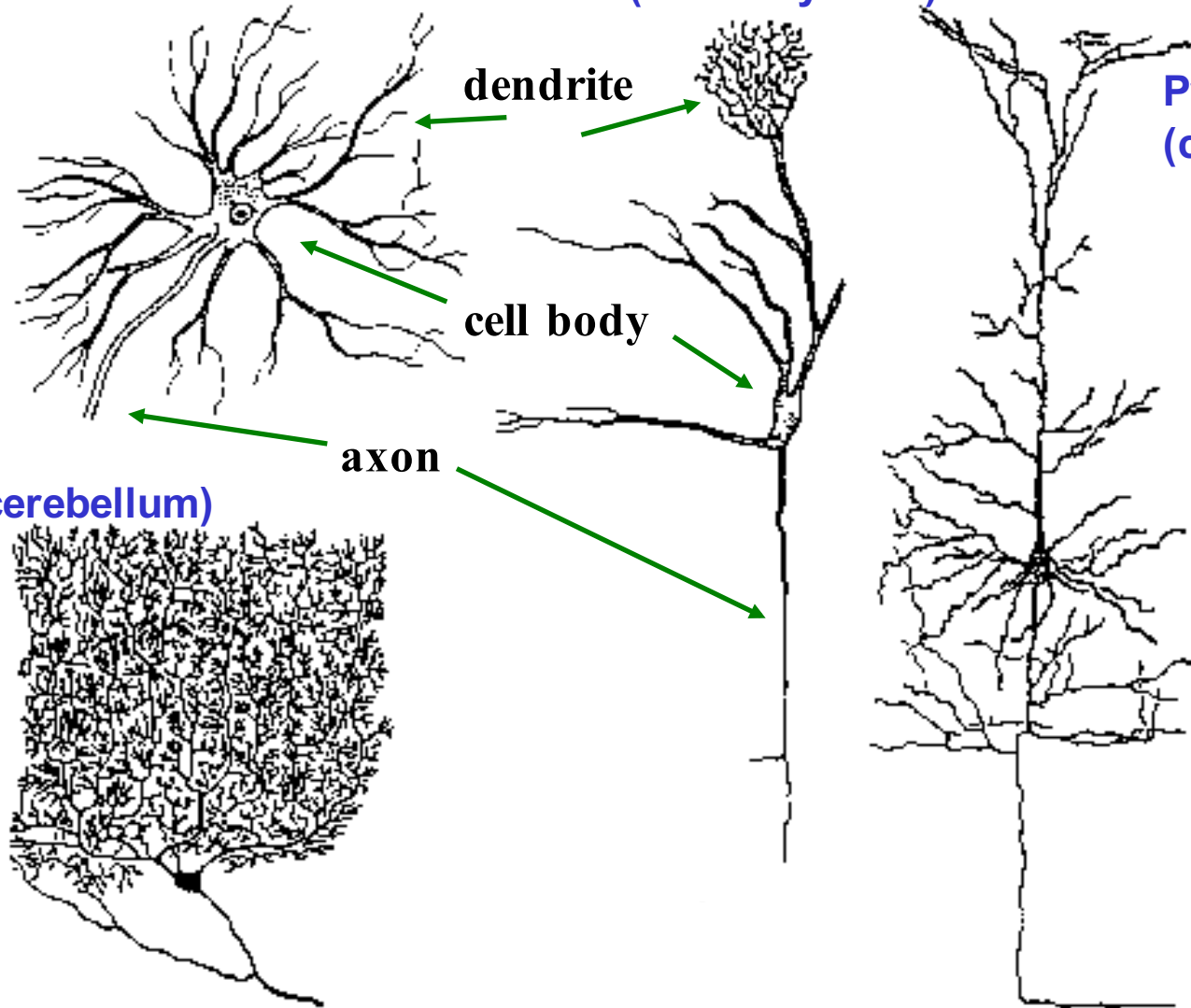
**Electrical signals come IN to dendrites, are “integrated” in cell body, result goes OUT axon**

**motor neuron (spinal cord)**

**mitral cell  
(olfactory bulb)**

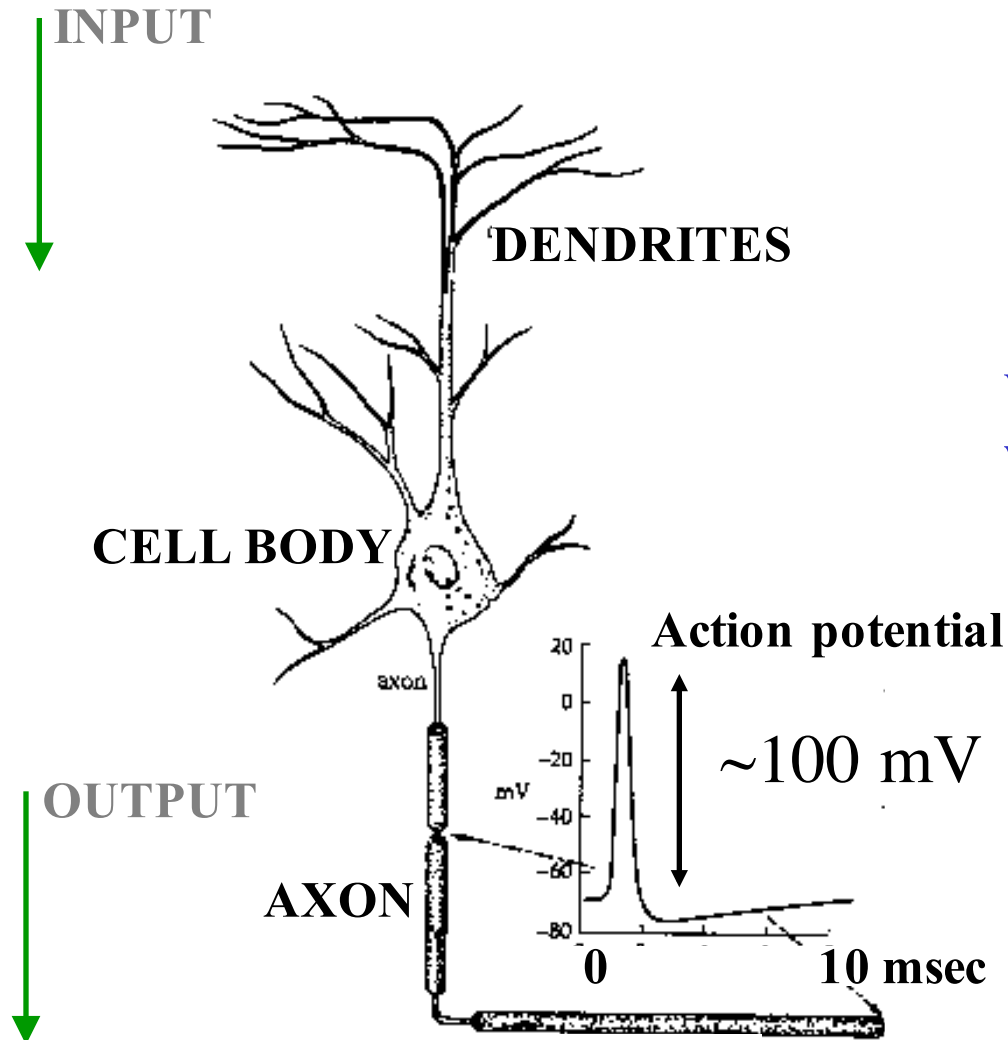
**Pyramidal cell  
(cortex)**

**Purkinje cell (cerebellum)**



**From Nicholls et al, 1992, Fisher and Boycott, 1974, Johnston and Wu, 1997**

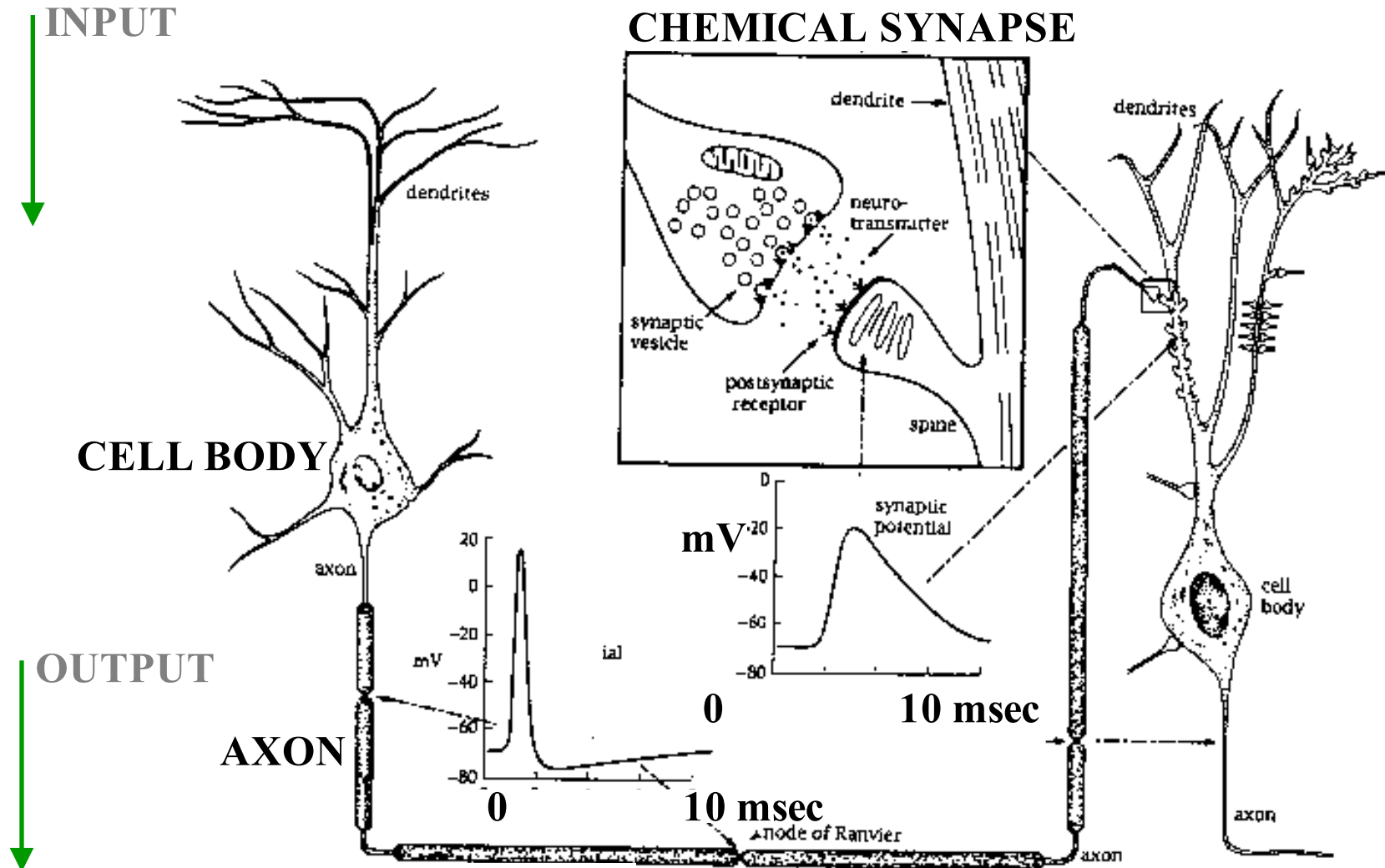
Given sufficient input, neurons “fire action potentials” – fast voltage transients



Voltage  $V$ : set by "excess charge" inside vs outside membrane (more later)

Given sufficient input, neurons “fire action potentials” – fast voltage transients

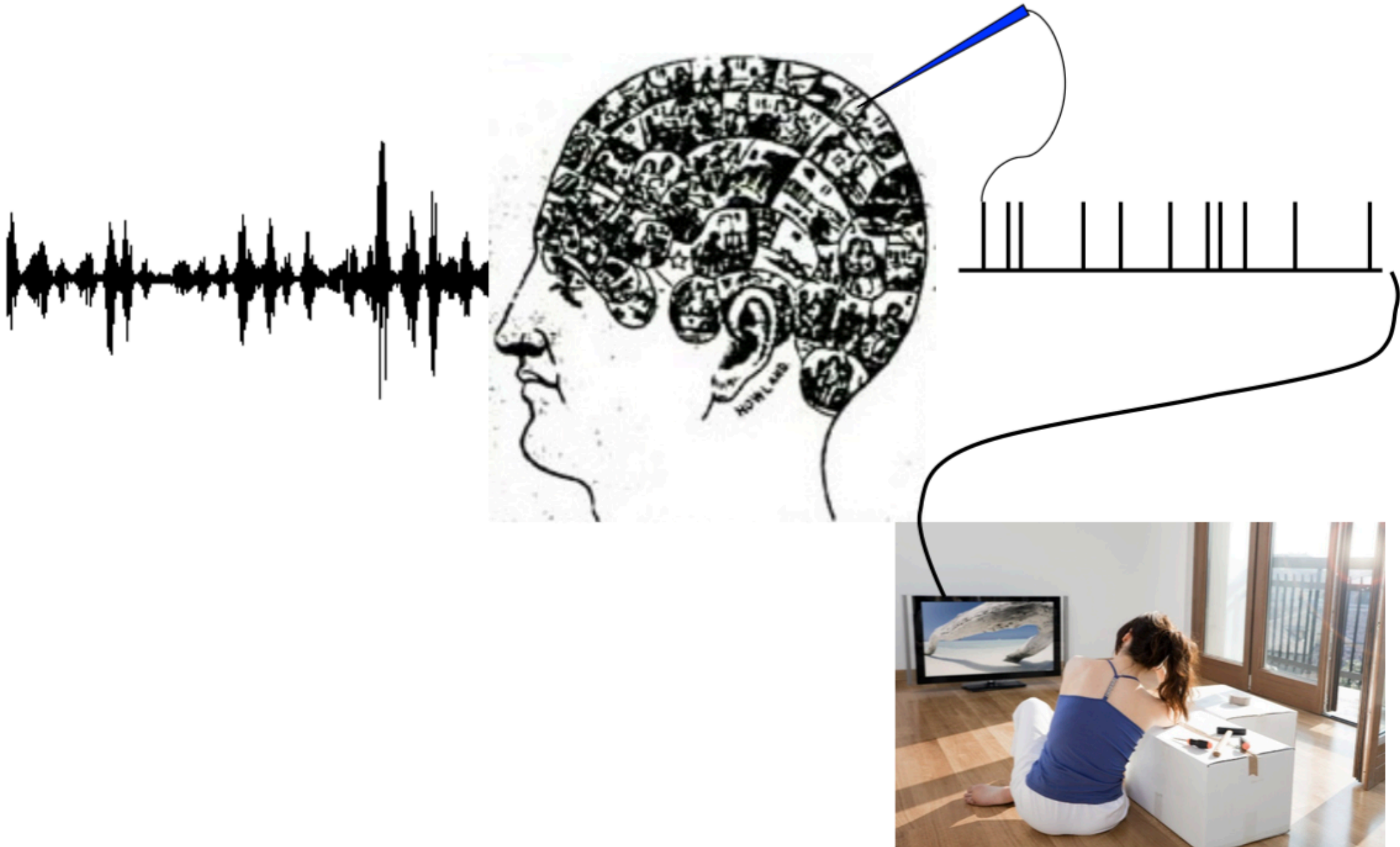
...which are communicated to downstream neurons via synapses



- Overview (blackboard)

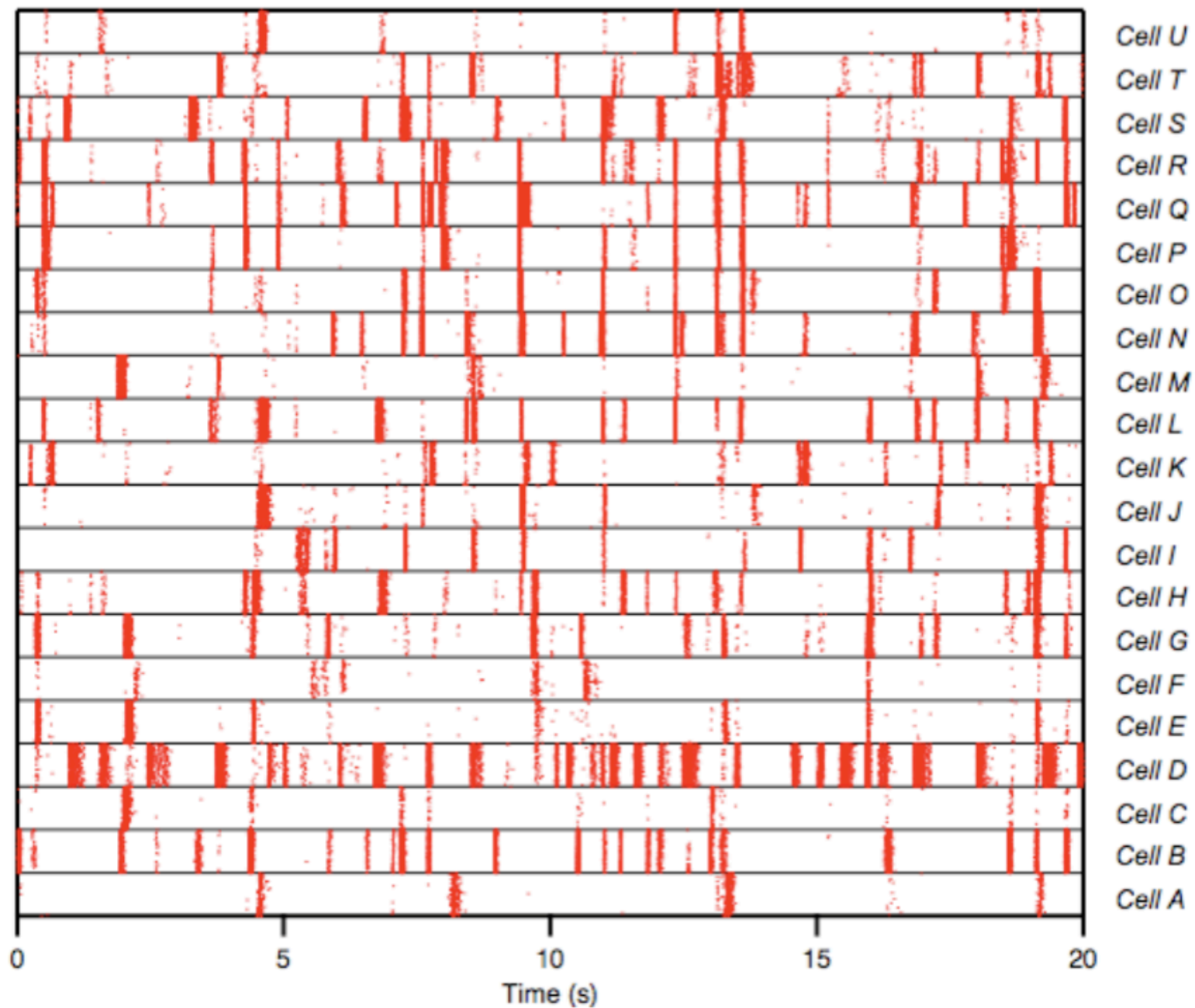
- Thanks to Prof. Adrienne Fairhall for many slides, materials, and ideas!

# Neural coding



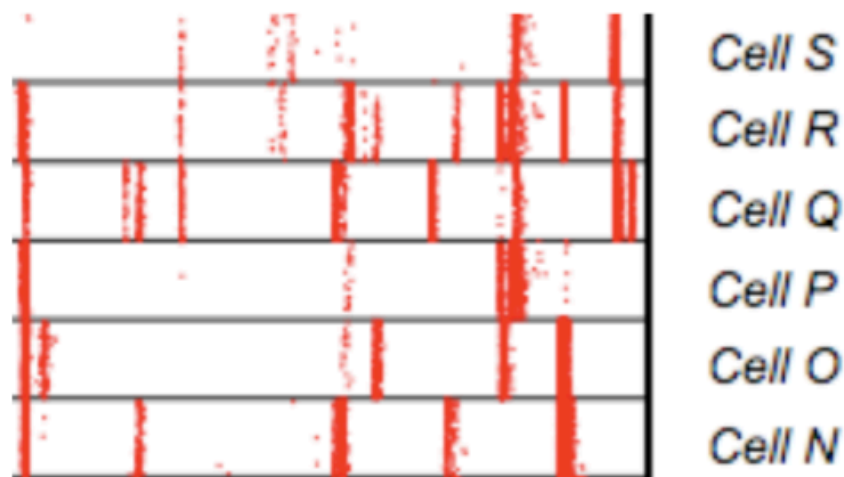
# What is the neural code?

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# What is the neural code?

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*Encoding:* how does a stimulus cause a pattern of responses?

- what are “responses” and what are their characteristics?
- how much is deterministic and how much stochastic?
- neural models:
  - what takes us from stimulus to response;
  - descriptive and mechanistic models, and the relation between them.

*Decoding:* what do these responses tell us about the stimulus?

- Implies some kind of decoding algorithm
- How do we evaluate how good our algorithm is?

# Neural coding

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More generally, we are interested in determining the relationship:

$$P(\text{response} \mid \text{stimulus})$$

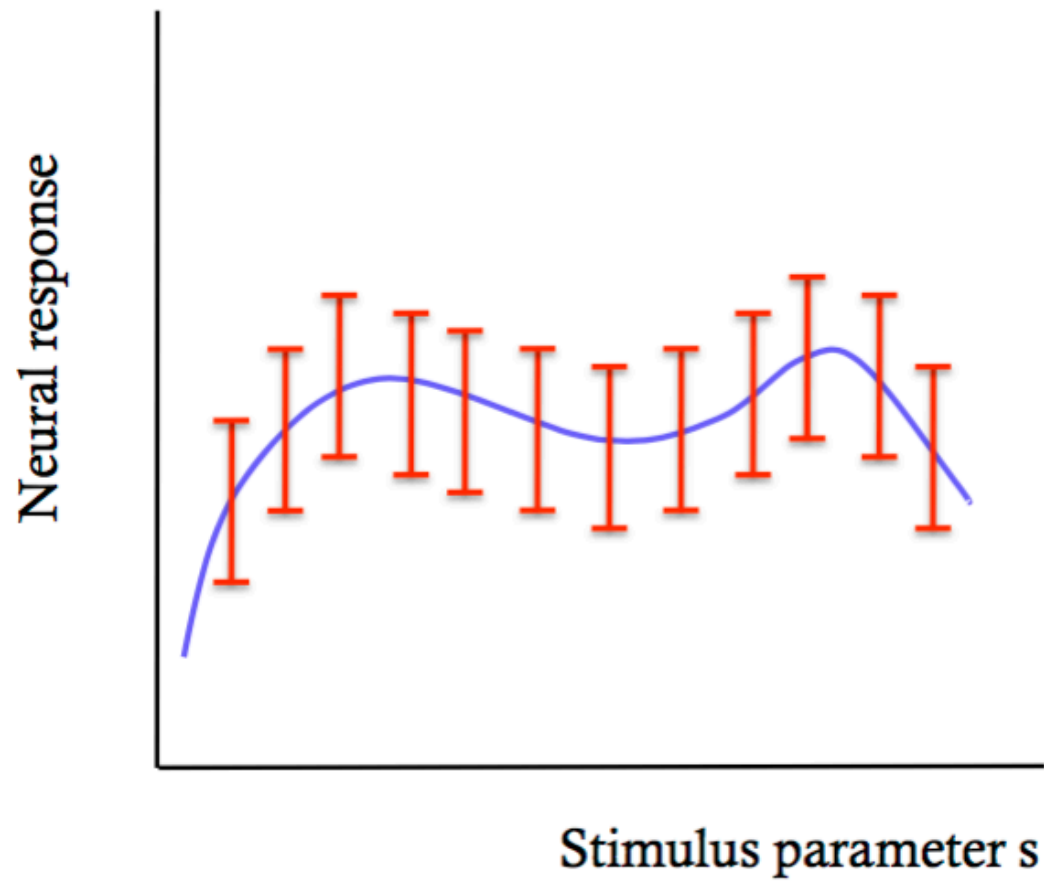
*encoding*

$$P(\text{stimulus} \mid \text{response})$$

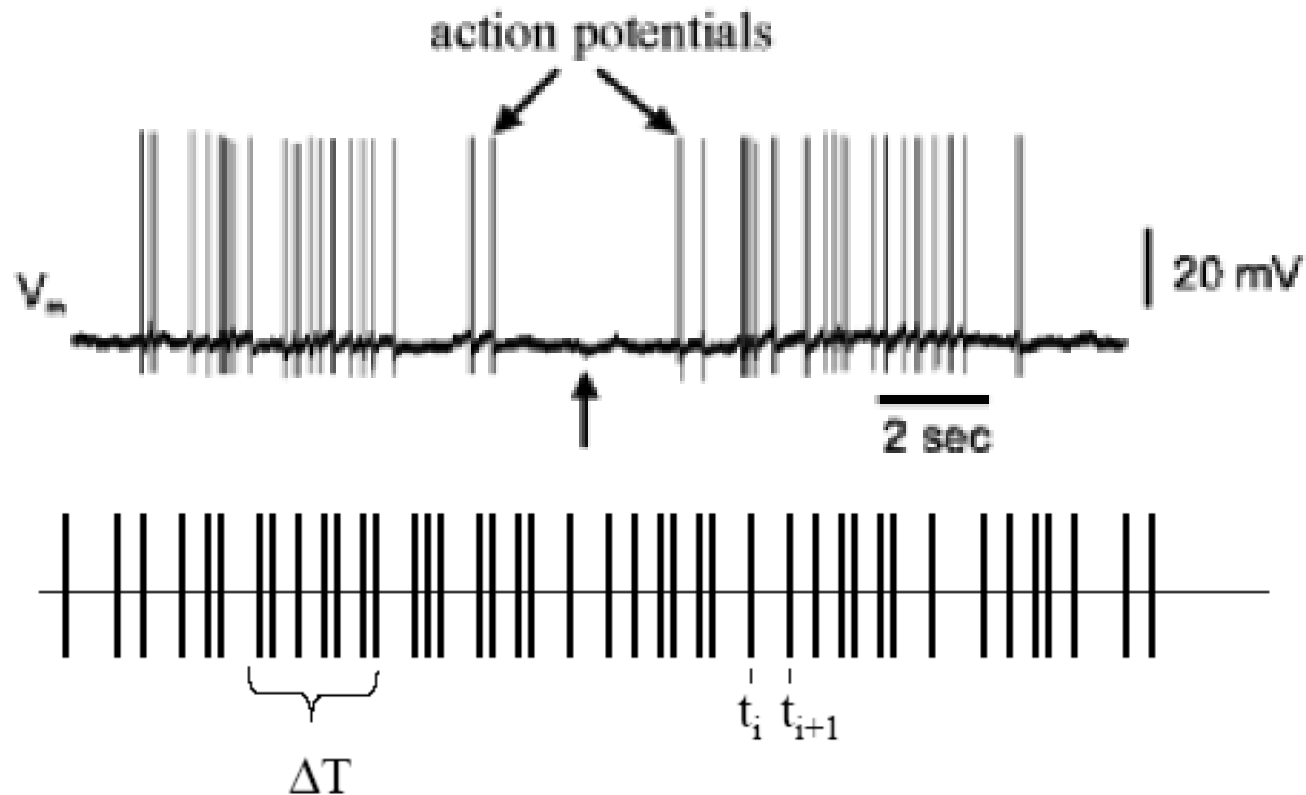
*decoding*

# Neuronal representation of information

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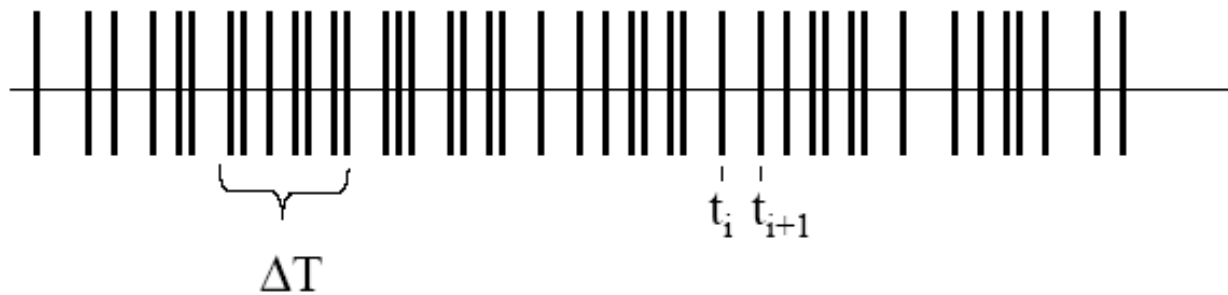
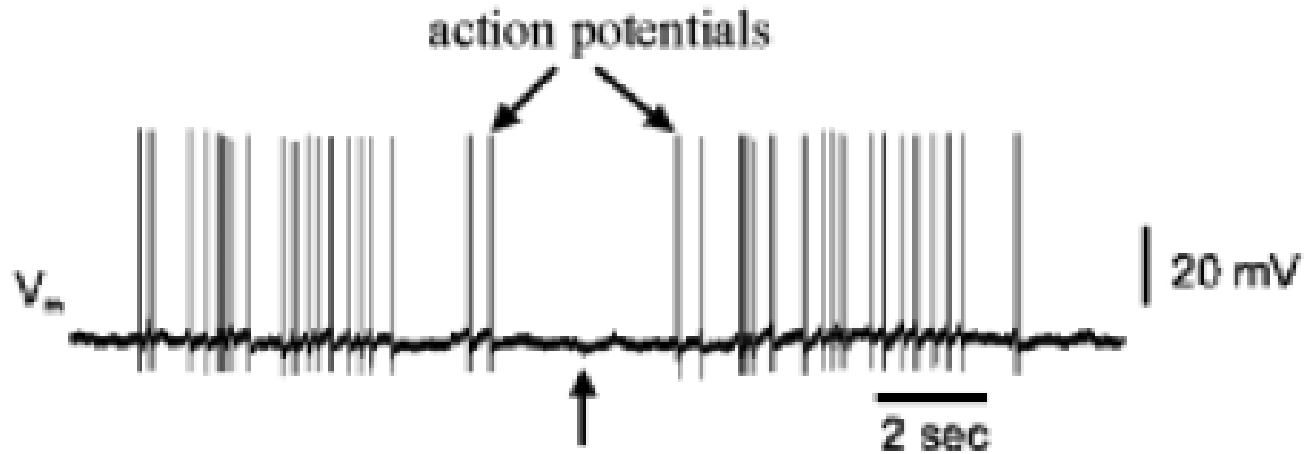
Simplest definition of neural response: *firing rates*



$$\text{Firing rate} = (\# \text{ spikes}) / (\Delta T)$$

(Other possibilities: spike timing, synchrony among multiple spikes, ...)

(Board ... definition of delta function)



David Tank

SPIKE TRAIN

$$\rho(t) = \sum_{t_i} \delta(t - t_i)$$

FIRING RATE

$$r(t) = \frac{1}{\Delta T} \int_t^{t+\Delta T} \rho(t) dt$$

Starting “simple:”

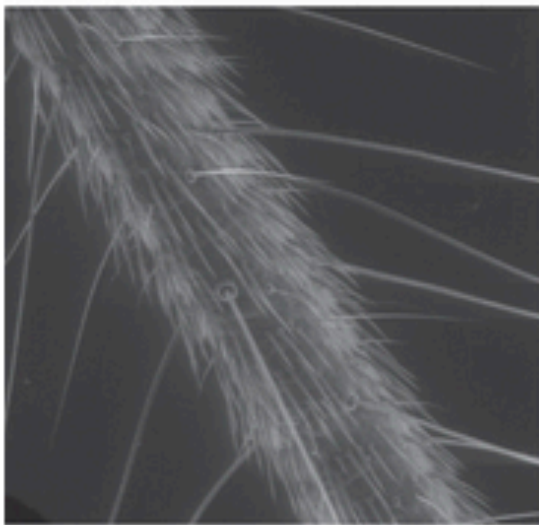
Stimulus ENcoding in the cricket cercal system

Response = firing rate

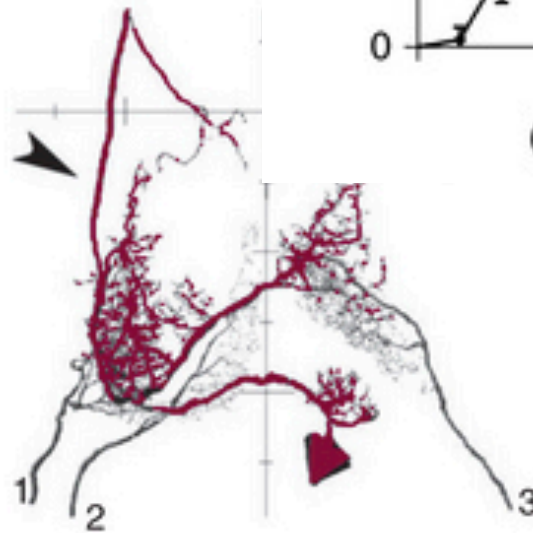
Stimulus = wind direction



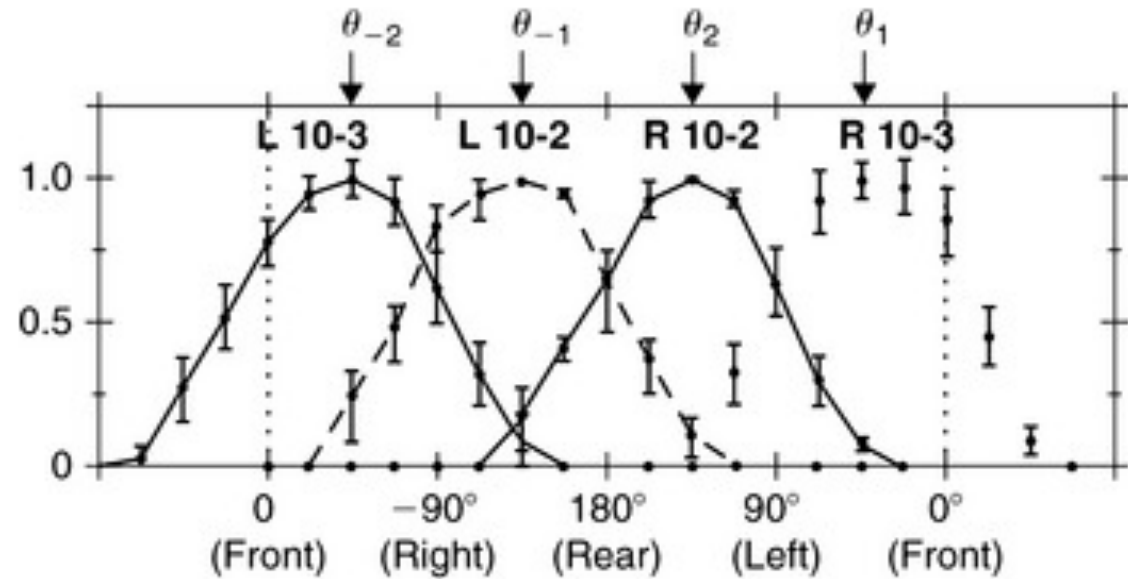
(A)



(B)

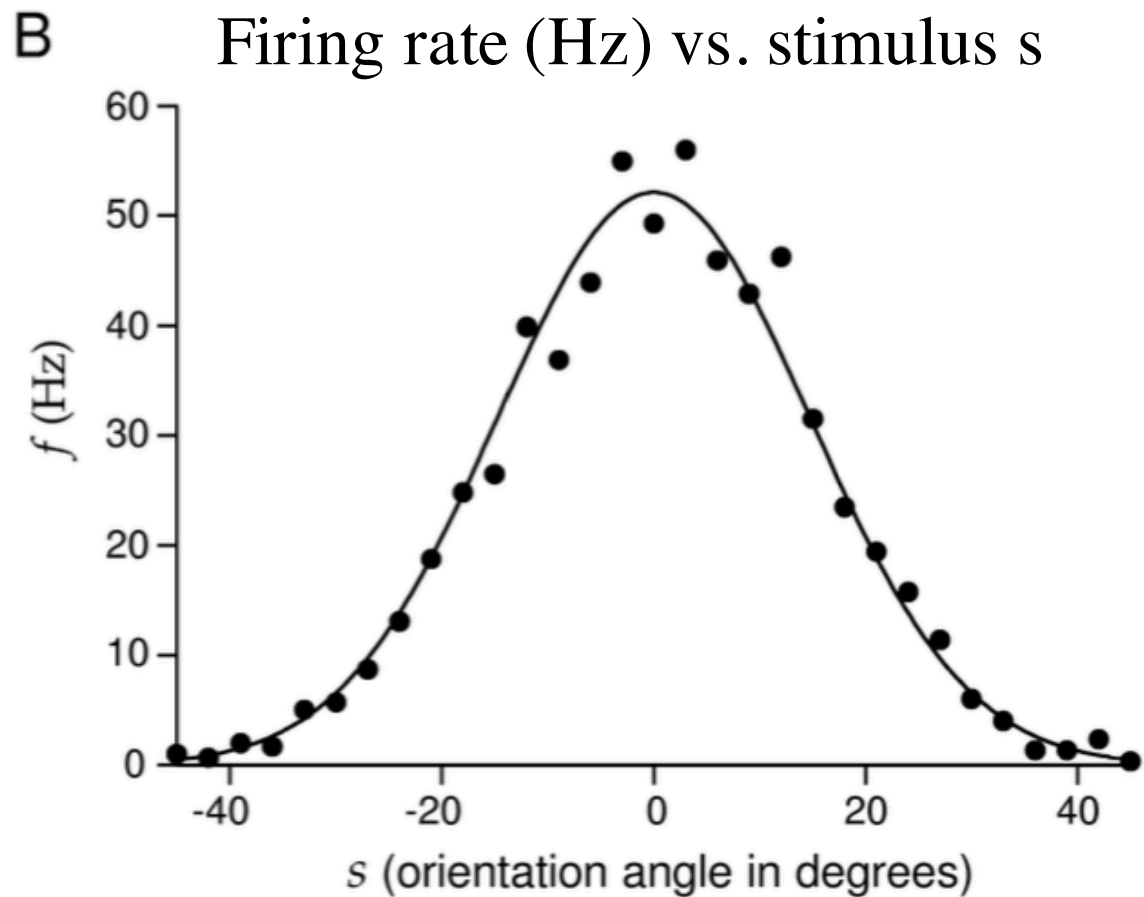
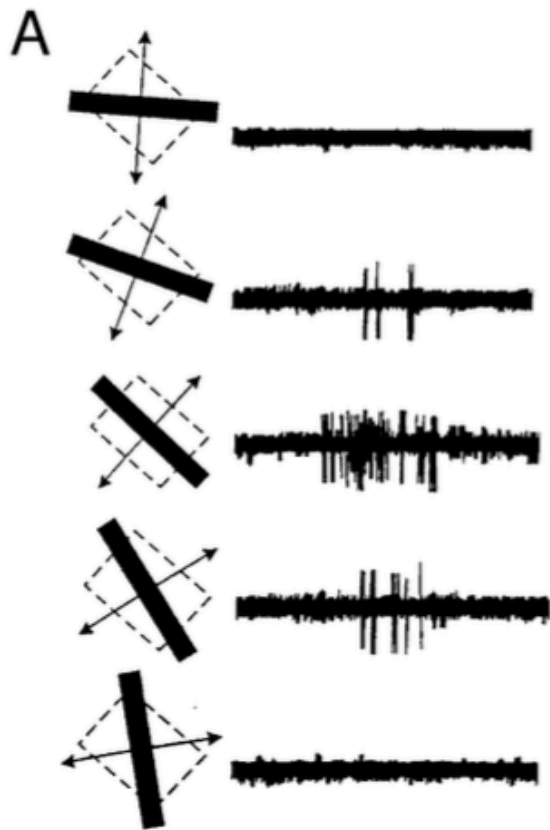


(C)



# Receptive fields and tuning curves

Tuning curve:  $r = f(s)$



**Gaussian tuning curve of a cortical (V1) neuron**

(Board –

Modeling spike trains and the Poisson process

Random variables

Generating spike trains in MATLAB)

## Code 1: generate\_simple\_spiketrain.m

```
%Generate single spiketrain

rand( 'state',sum(100*clock) );

nsec=1 ;
T=1;
deltat=0.001;
r=100;
p=r*deltat;
numbins=round(T/deltat);
spiketrain=round(rand(1,numbins) + (p-1/2))

figure;
imagesc(spiketrain)
...
```

(Board – Mean, variance, std dev)

## Code 1, continued: Generating and analyzing multiple trials of a spike train

```
%Generate many "trials" of spiketrains
numtrials=10;
spiketrain=round(rand(numtrials,numbins) +
(p-1/2));

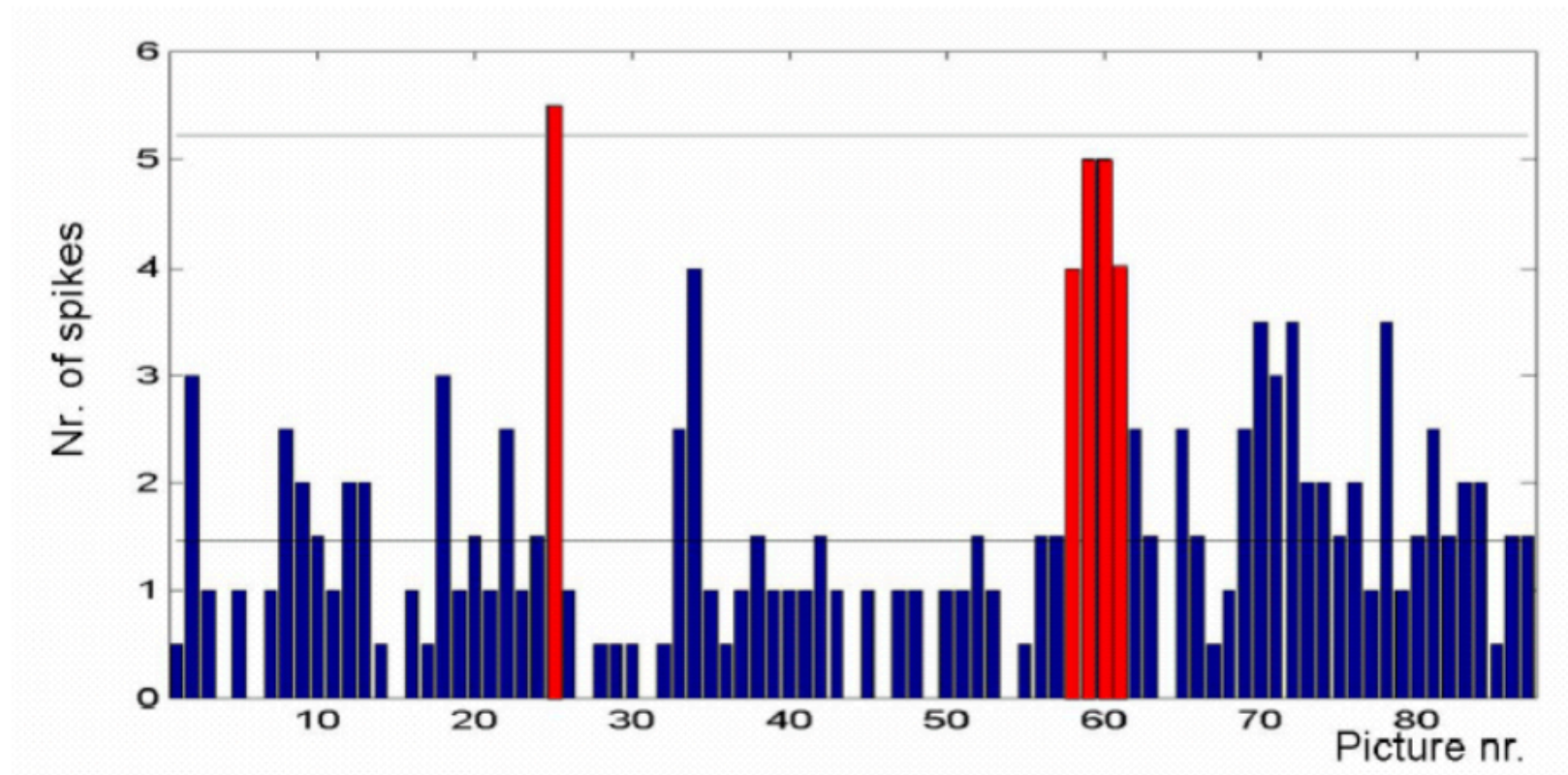
figure;
imagesc(spiketrain)
xlabel('time')
ylabel('trial')

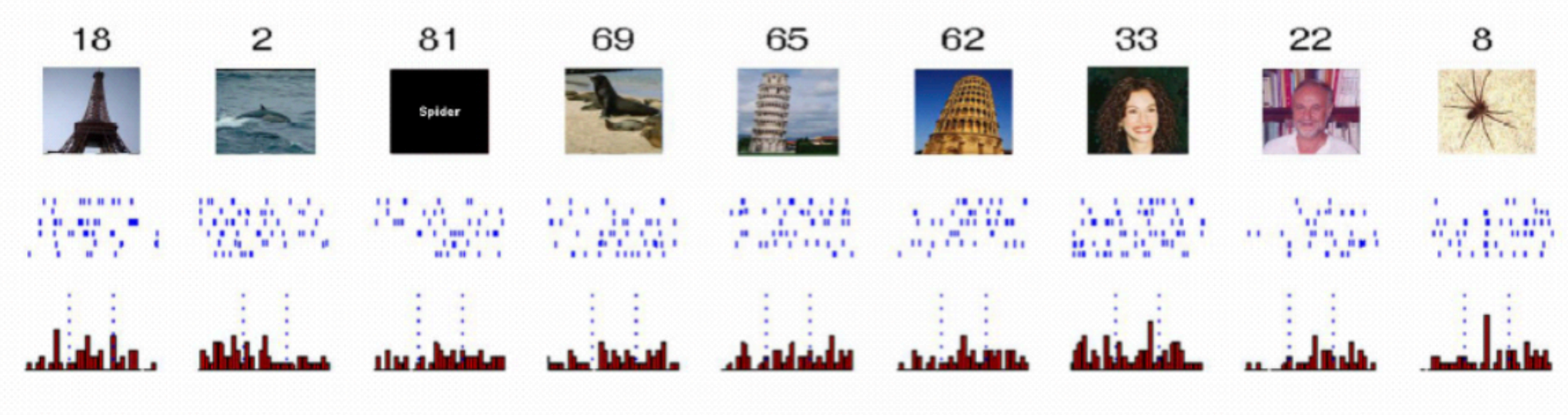
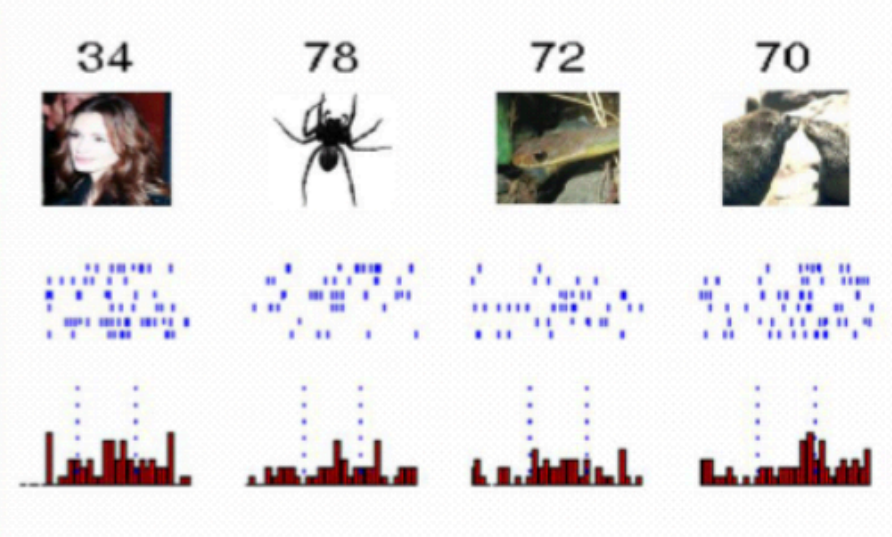
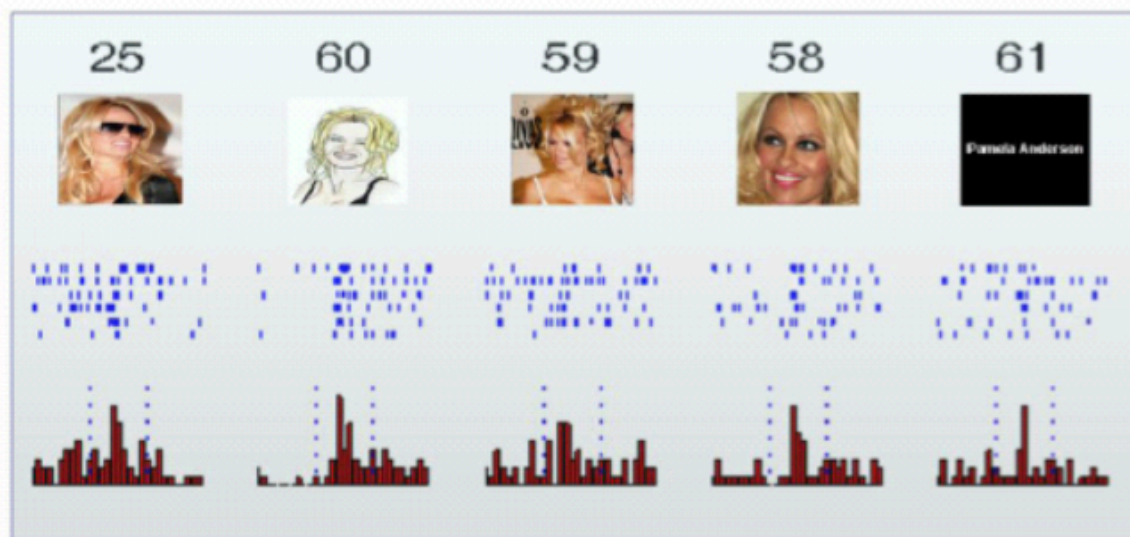
%Compute the average spike rate, and standard
deviation
rate_per_trial=1/T * sum(spiketrain,2)
mean_rate_per_trial = mean(rate_per_trial)
std_dev_rate_per_trial = std(rate_per_trial)
```

Hand out HW

# Complex feature representation

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60



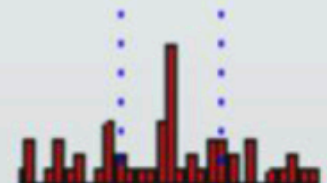
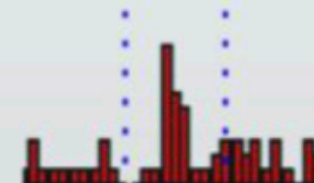
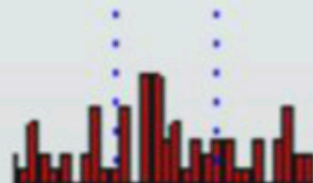
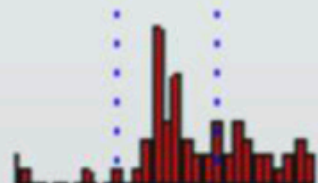
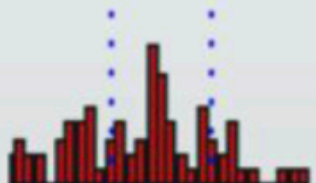
59



58



61



nature

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## LETTERS

# Invariant visual representation by single neurons in the human brain

R. Quian Quiroga<sup>1,2†</sup>, L. Reddy<sup>1</sup>, G. Kreiman<sup>3</sup>, C. Koch<sup>1</sup> & I. Fried<sup>2,4</sup>