

Member Force-Deformation Relationship in Local C.S.

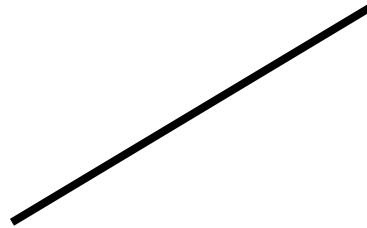
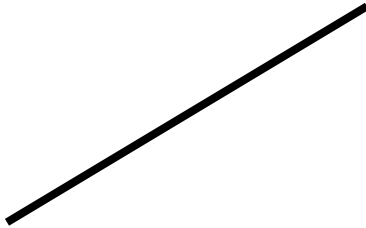
$$\mathbf{q} = \mathbf{k}' \mathbf{d}$$

$$\begin{Bmatrix} q_{Nx'} \\ q_{Ny'} \\ m_{Nz'} \\ q_{Fx'} \\ q_{Fy'} \\ m_{Fz'} \end{Bmatrix} = \begin{bmatrix} \frac{AE}{L} & 0 & 0 & -\frac{AE}{L} & 0 & 0 \\ 0 & \frac{12EI}{L^3} & \frac{6EI}{L^2} & 0 & -\frac{12EI}{L^3} & \frac{6EI}{L^2} \\ 0 & \frac{6EI}{L^2} & \frac{4EI}{L} & 0 & -\frac{6EI}{L^2} & \frac{2EI}{L} \\ -\frac{AE}{L} & 0 & 0 & \frac{AE}{L} & 0 & 0 \\ 0 & -\frac{12EI}{L^3} & -\frac{6EI}{L^2} & 0 & \frac{12EI}{L^3} & -\frac{6EI}{L^2} \\ 0 & \frac{6EI}{L^2} & \frac{2EI}{L} & 0 & -\frac{6EI}{L^2} & \frac{4EI}{L} \end{bmatrix} \begin{Bmatrix} d_{Nx'} \\ d_{Ny'} \\ \theta_{Nz'} \\ d_{Fx'} \\ d_{Fy'} \\ \theta_{Fz'} \end{Bmatrix}$$

Local and Global
CS

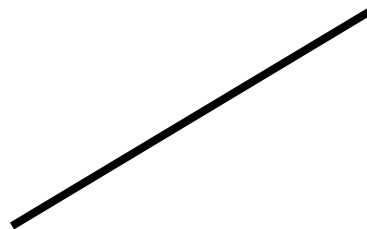
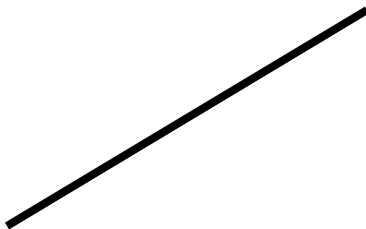
Local Coordinate System

Global Coordinate System



Local Coordinate System

Global Coordinate System



Member Force-Deformation Relationship: Global C.S.

$$\mathbf{q} = \mathbf{k}' \mathbf{d}$$

But $\mathbf{d} = \mathbf{T}\mathbf{D}$

So $\mathbf{q} = \mathbf{k}'\mathbf{T}\mathbf{D}$

We want $\mathbf{Q} = \mathbf{T}^t \mathbf{q}$

Therefore $\mathbf{Q} = \mathbf{T}^t \mathbf{k}' \mathbf{T} \mathbf{D}$

and $\mathbf{k} = \mathbf{T}^t \mathbf{k}' \mathbf{T}$