# **Chapter 2: Genes in Pedigrees**

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#### 2.1.1 GRAPHICAL REPRESENTATION OF PEDIGREES:

• Three graphical representations.

The parent-offspring links.

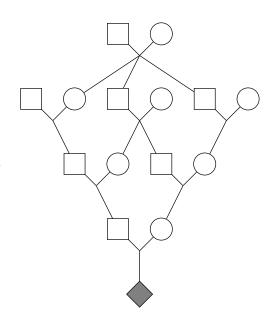
- —often animal pedigrees.
- —too many crossing lines.

The sibship representation.

- -often human pedigrees
- —"tramlines" (J.H.Edwards)

The marriage-node graph. - see figure (Cannings et al., 1978)

- Founders and non-founders (no half-founders): assumed unrelated.
- Gender: male, female, and unknown. (square, circle, diamond)
- Shading or labelling of individuals



#### 2.1.2 SPECIFICATION OF PEDIGREES:

- Unique individual identifiers ("names")
- Parent-offspring trios.
   (default: ind, dad, mom)
- Specification of founders. (parent "names" =0)
- Gender: male, female, and unknown. (1, 2, 0) or (M, F, U)
- Phenotypic, covariate, and marker data.
- "Chronological" (partial) ordering of pedigrees.

name	dad	mom	sex	other data
101	0	0	1	
102	0	0	2	
201	101	102	2	
204	101	102	1	
206	101	102	1	
fred	0	0	1	
203	0	0	2	
joe	fred	201	1	
jane	204	203	2	
dave	204	203	1	
hugh	joe	jane	1	
etc				

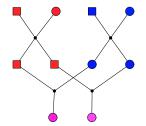
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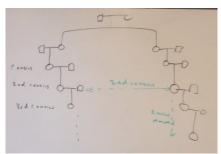
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#### 2.1.3 TYPES OF RELATIONSHIP:

- Related : individuals having a common ancestor (implies a biological relationship)
- Inbred: individuals whose parents are related (implies the maternal and paternal genes can descend from single ancestral gene).
- Unilateral (one-sided) and bilateral (two-sided) relationships: unilateral: half-sibs, aunt, niece, cousins bilateral: sibs, double first cousins, etc.
- Cousin-type relationships:
   Half, full, and double cousins:



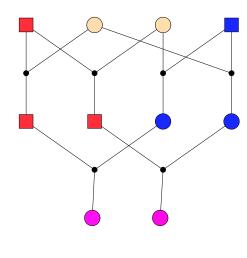
 $n^{th}$  cousins k times removed

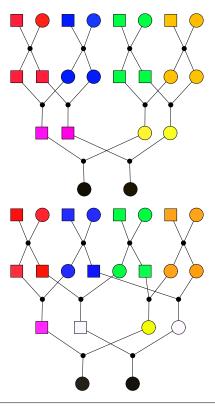


### 2.1.4 More complex relationships:

Quadruple half first cousins; and

quadruple second cousins





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## 2.2.1 GENE IDENTITY BY DESCENT (iba):

• RELATIVES ARE SIMILAR because they have *ibd* genes, that are copies of the same gene in a common ancestor.

NOTE: ibd is defined relative to given pedigree or time point

## • Basic assumption:

- *ibd* genes are of the same allelic type; ignores mutation
- non-*ibd* genes are of independent types; ignores structure beyond the pedigree.

Recall the basic Mendelian genetics examples of Homework-1.

## • Framework for analysis of genetic data on pedigrees:

A pedigree or relationship determines probabilities of *ibd*, which determine probabilities of joint genotypes which determine probabilities of joint phenotypes that is, similarity among relatives.

#### 2.2.2 KINSHIP and INBREEDING:

• The simplest pedigree-defined probabilities of gene *ibd* are the coefficients of kinship  $(\psi)$  and inbreeding (f), which measure *ibd* between two genes.

$$\psi(B,C) = \Pr(homologous\ genes\ segregating\ from\ B\ and\ C\ are\ ibd)$$

$$f(B) = \Pr(homologous\ genes\ in\ B\ are\ ibd)$$

$$= \psi(M_B, F_B)$$

where  $M_B$  and  $F_B$  are the parents of B.

Note at a single locus:

randomly chosen from  $\equiv$  segregating from

but for two of more loci we must define what "randomly chosen" should mean, and the relevant definition is that of Mendelian segregation.

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#### 2.2.3 KINSHIP EXAMPLES via PATH COUNTING:

Half sibs:  $(1/2) \times (1/2) \times (1/2) = 1/8$ 

Two genes from an inbred (f) parent:

$$1 \times f + (1/2) \times (1 - f) = (1/2)(1 + f)$$

Half sibs with inbred (f) parent: (1+f)/8

Full sibs: 1/8 + 1/8 = 1/4

First cousins:  $(1/4) \times (1/2) \times (1/2) = (1/16)$ 

Double first cousins: 1/16 + 1/16 = 1/8

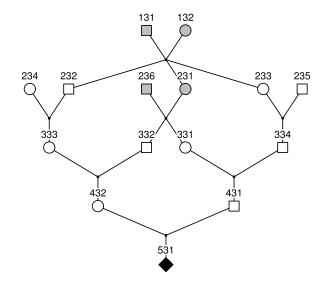
General formula (Wright, 1922):

$$\psi = \sum_{A} \sum_{P(A)} \frac{1}{2} (1 + f_A) \left(\frac{1}{2}\right)^{n_1(P(A)) + n_2(P(A))}$$

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## **EXAMPLE: The JV pedigree (Goddard et al., 1996):**



2 ancestors, each with 3 paths, each with  $n_1 = n_2 = 3$ : and 2 ancestors, each with 1 path, each with  $n_1 = n_2 = 2$ .  $2 \times 3 \times (\frac{1}{2})^7 + 2 \times 1 \times (\frac{1}{2})^5 = 7/64$ 

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 $F_B$ 

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#### 2.2.4 RECURSIVE METHOD:

$$\psi(B,C) = \frac{1}{2}(\psi(M_B,C) + \psi(F_B,C))$$

provided B is not C nor an ancestor of C

$$\psi(B,B) = \frac{1}{2}(1+f_B) = \frac{1}{2}(1+\psi(M_B,F_B))$$

Boundary conditions:

$$\psi(A,A) = \frac{1}{2} \text{ and } \psi(A,C) = 0$$

if A is a founder, and not an ancestor of C

Expanding up the JV pedigree, among the grandparents, we have 3 first-cousin pairs and a sib pair. The kinship of first cousins is 1/16, and of sibs is 1/4, so overall we have

$$\frac{1}{4}(3\frac{1}{16} + \frac{1}{4}) = \frac{7}{64}$$

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#### 2.2.5 INBREEDING and GENOTYPE FREQUENCIES:

- MYTH: Recessive diseases are more frequent in genetic isolates. This is because isolates are "more inbred"
- TRUTH-1: the more inbred individuals within any population have higher probability of being affected.
- Consider a recessive disease allele a with freq q, and an individual with inbreeding coefficient f (aa individuals are affected.)

$$Pr(aa) = q^{2}(1-f) + qf = q^{2} + fq(1-q)$$

$$Pr(Aa) = 2q(1-q)(1-f)$$

$$Pr(AA) = (1-q)^{2} + fq(1-q)$$

See population mixtures and Wahlund variance (see 1.2.4), For two alleles, see homework 2, # 4:  $\sigma_f^2 = \sum_i \alpha_i (q_i - \bar{q})^2$ :

$$\Pr(aa) = q^2 + \sigma_f^2 \text{ and } \Pr(AA) = (1-q)^2 + \sigma_f^2$$
  
 $\Pr(Aa) = 2q(1-q) - 2\sigma_f^2$ 

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## Population subdivision vs inbreeding:

- In population subdivision, people marry those more similar, hence more homozygosity in offspring.
- In inbreeding, people marry relatives, and hence more similar, and hence ... Inbreeding is a form of population subdivision.

Autozygosity (ibd) vs. inbreeding

- Autozygous ≡ having ibd genes
- ullet inbred  $\equiv$  having non-zero prob of being autozygous

$$\Pr(ibd \mid \text{affected}) = \frac{qf}{q^2 + fq(1-q)} = \frac{f}{q + f(1-q)}$$

which  $\geq f$ , increases as q decreases, and  $\rightarrow$  1 as  $q \rightarrow$  0.

TRUTH-2: In a population with varying levels of inbreeding, the affected people have higher probability of being inbred.

Suppose a proportion  $\alpha$  of the population  $(Pop_1)$  has inbreeding coefficient f and others  $(Pop_2)$  are not inbred:

$$\Pr(\text{affected } aa) = (1 - \alpha)q^2 + \alpha(q^2 + fq(1 - q))$$

$$= q^2 + \alpha fq(1 - q)$$

$$\Pr(Pop_1 \mid \text{affected}) = \frac{\alpha(q^2 + fq(1 - q))}{q^2 + \alpha fq(1 - q)}$$

$$= \frac{\alpha(q + f - fq)}{(q + \alpha f - \alpha fq)}$$

which is always  $\geq \alpha$  and  $\rightarrow 1$  as  $q \rightarrow 0$ .

TRUTH-3: The affected inbred people in the population have higher probability of being autozygous (*ibd*):

$$\Pr(ibd \mid affected) = \frac{\alpha fq}{q^2 + \alpha fq(1-q)} = \frac{\alpha f}{q + \alpha f(1-q)}$$

Same form as before with f now becoming  $\alpha f$ .

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