STAT 341 - Elizabeth Thompson

Homework 1 Solutions

2.2.22, 2.4.11, 2.4.28, 2.5.25, 3.2.5, 3.2.19 (2.2.22)

- (a) $\{E1, E2\}$
- (b) $\{S1, S2, T1, T2\}$
- (c) $\{A, I\}$

(2.4.11)

(a)
$$P(A^C \cap B^C) = 1 - P(A \cup B)$$

= $1 - [P(A) + P(B) - P(A \cap B)]$
= $1 - [0.65 + 0.55 - 0.25] = 0.05$

(b) $P[(A^C \cap B) \cup P(A \cap B^C)] = P(A \cup B) - 2P(A \cap B)$ = 0.65 + 0.55 - 2 × 0.25 = 0.70

(c)
$$P(A \cup B) = 0.95$$

- (d) $P[(A \cap B)^C] = 1 P(A \cup B) = 1 0.25 = 0.75$
- (e) $P[(A^C \cap B) \cup P(A \cap B^C) | A \cup B]$ = $\frac{P[(A^C \cap B) \cup P(A \cap B^C)]}{P(A \cup B)} = 0.70/0.95 = 70/95$
- (f) $P(A \cap B | A \cup B) = P(A \cap B) / P(A \cup B) = 0.25 / 0.95 = 25 / 95$

(g)
$$P(B|A^C) = P(A^C \cap B)/P(A^C) = [P(B) - P(A \cap B)]/[1 - P(A)]$$

= $[0.55 - 0.25]/[1 - 0.65] = 30/35$

(2.4.28)

Let B be the event that a donation is received; let A_1, A_2 and A_3 denote the events that the call is placed to Belle Meade, Oak Hill, and Antioch, respectively. Then,

$$P(B) = \sum_{i=1}^{3} P(B|A_i) P(A_i) = 0.60 \times \frac{1000}{4000} + 0.55 \times \frac{1000}{4000} + 0.35 \times \frac{2000}{4000} = 0.46$$

(2.5.25)

 $P(\text{at least one double six in } n \text{ throws}) = 1 - P(\text{no double sixes in } n \text{ throws}) = 1 - \left(\frac{35}{36}\right)^n$ By trial and error, n = 25.

(3.2.5)

P(At least 7 work) = P(3 or fewer are out)

$$=\sum_{k=0}^{3} {}_{10}C_k(0.05)^k(0.95)^{10-k} = 0.599 + 0.315 + 0.075 + 0.010 = 0.999$$

(3.2.19)

P(At least twice as many black bears as tan in 6 sightings)

 $= P(0 \tan, 6 \operatorname{black}) + P(1 \tan, 5 \operatorname{black}) + P(2 \tan, 4 \operatorname{black})$

$$\frac{{}_{3}C_{0}\times_{6}C_{6}}{{}_{9}C_{6}} + \frac{{}_{3}C_{1}\times_{6}C_{5}}{{}_{9}C_{6}} + \frac{{}_{3}C_{2}\times_{6}C_{4}}{{}_{9}C_{6}} = \frac{64}{84}$$