#### Chem 455 – Homework # 1A

Due Friday April 4 by noon in Soumya Samai's mailbox in Bagley Hall

Late homework is not accepted for ANY credit.

5B

6B

7B

8B

9B

10B 11B 12B 13B 14B 15B 16B 17B 18B

4B

1B

2B

3B

Turn in only this front page. Keep the following pages and all of your work for future reference.

This homework set is intended as a quick way for you to test your math skills and refresh them up to the level needed to *begin* CHEM 455. Questions of these types will appear in lectures and exams, so treat this seriously. You will be graded on whether you complete this part of the homework, not on how many questions you answer correctly.

This homework consists of two "self-tests". Questions appear on one side of the sheet and the answers are on the back. Please try all of the problems in the first self-test before looking at the answers and recording your score below. If you get everything right on the first self-test, then there is no need to do the second one. Most students improve dramatically by the second time through.

Nam	ıe:							_									
Did you get all questions 1A-18A correct on the first try? (circle an answer) YES / NO																	
Mark an "X" through those questions you got wrong the first time you attempted them.																	
1A	2A	3A	4A	5A	6A	7A	8A	9A	10A	11A	12A	13A	14A	15A	16A	17A	18A

### MATHEMATICS SELF-TUTORIAL, CHEM455

**Evaluate and/or simplify the expressions without a calculator**. While you are allowed to use a calculator on the homeworks and exams, most students who complain that the exams are "too long" also lose time on "remedial" topics.

Do not convert fractions to decimals. Complete this page entirely before turning to the next page.

## **QUESTION SET A**

- 1A) use the quadratic equation to solve  $2x^2 x + 8 = 0$  for x
- 2A) if y = (5+2i), what is  $(y^*)(y)$
- 3A) express (2+3i)/(4-2i) in the form a+bi
- $4A) \qquad \int_{0}^{\pi} \sin(x) = ?$
- 5A)  $(a^2bc^{-1})(ab^{-3}) = ?$
- 6A) |i| = ?
- 7A) |2-7i| = ?
- 8A) express 3+3i in  $re^{i\theta}$  form
- 9A) express  $2e^{(i\pi/3)}$  in a+bi form
- 10A) Dimensional analysis: What are the units for angular momentum? Show that Planck's constant has units of angular momentum.
- 11A) For values of x which are close to 1,  $ln(x) \approx x 1$ . This problem uses a Taylor expansion to show that this is true. Use a Taylor Series to approximate ln(1.05) = ? to first order.
- 12A)  $f(x) = (x^{4/3} 2x^{-2})^5$   $df/_{dx} = ?$  (no need to multiply out)
- 13A)  $f(x) = (1 x^4)/x$  df/<sub>dx</sub> = ? (no need to multiply out)
- 14A) simplify e<sup>2ln3</sup>
- 15A) find the maximum and minimum of the equation  $f(x) = x^3 27x$  over the range x=-5..5
- 16A)  $\int_{x=1}^{3} 2x^2 dx = ?$
- 17A)  $\frac{\partial}{\partial x} \left( 2x^4 y^6 + \frac{3}{x^2} \right) = ?$
- For objects with a radius of 2 meters, what are the a) circle's perimeter, b) circle's area, c) sphere's surface area, and d) sphere's volume? (express as multiples of  $\pi$ . Include units!)

Grade questions 1A-17A. Make sure that you understand the answers before turning to the next page.

	ANSWER SET A	<u>REASONS</u>
1A)	$1 + 3i\sqrt{7}  1 - 3i\sqrt{7}$	$abox{-}b\pm\sqrt{b^2-4ac}$
	4, 4	$x = {2a}$

2A) 29 
$$(a+bi)(a-bi)=a^2+b^2$$

3A) 
$$\frac{1}{10} + \frac{4}{5}i$$
 
$$\frac{a+bi}{c+di} = \frac{a+bi}{c+di} \cdot \left(\frac{c-di}{c-di}\right)$$

5A) 
$$a^3b^{-2}c^{-1}$$
  $a^xa^y = a^{x+y}$ 

$$7A) \quad \sqrt{53} \qquad |y| = \sqrt{y^* y}$$

8A) 
$$\sqrt{18}e^{i\pi/4}$$
  $a+bi=|a+bi|e^{i \operatorname{atan}(b/a)}$ 

9A) 
$$1+i\sqrt{3}$$
  $e^{i\theta}=\cos(\theta)+i\sin(\theta)$ 

$$10A) \quad kg \cdot m^2 \cdot s^{-1} \qquad \qquad J \cdot s = N \cdot m \cdot s = kg \cdot m \cdot s^{-2} \cdot m \cdot s = kg \cdot m^2 \cdot s^{-1}$$

11A) 
$$\ln(x) = \ln(a) + (x-a)(1/a)$$
 Taylor Series:  $f(x) = f(a) + (x-a)f'(a) + (1/2!)(x-a)^2 f''(a) \dots$   
  $\ln(1.05) = 0 + (1.05 - 1)(1/1) = 0.05$  To first order, for  $x \approx 1$ , set  $a=1$  so that  $\ln x \approx (x-1)$ 

12A) 
$$5(x^{4/3} - 2x^{-2})^4(^4/_3x^{1/3} + 4x^{-3})$$
 for  $f(x) = cx^n$ ,  $^{df}/_{dx} = ncx^{n-1}$ , where c is a constant

13A) 
$$-4x^3(^1/_x) + (1-x^4)(-1/x^2)$$
  $^d/_{dx}(g(x)\cdot h(x)) = (^d/_{dx}g(x))(h(x)) + (g(x))(^d/_{dx}h(x))$  you will make fewer mistakes with the product rule

14A) 
$$(e^{\ln 3})^2 = (3)^2 = 9$$
  $e^{\ln x} = x$ 

15A) 
$$x = 3$$
 is min,  $x = -3$  is max min occurs at  $^{df}/_{dx} = 0$  and  $^{d^2f}/_{dx^2} > 0$  max occurs at  $^{df}/_{dx} = 0$  and  $^{d^2f}/_{dx^2} < 0$ 

16A) 
$$\frac{2}{3}x^3\Big|_{x=1}^3 = \frac{2}{3}(27-1) = \frac{52}{3}$$
  $\int ax^n dx = \left(\frac{1}{n+1}\right)ax^{n+1}$  for  $n \neq -1$ 

17A) 
$$8x^3y^6 - 6/x^3$$
 Partial derivatives treat all other variables as constants.

18A) 
$$4\pi$$
 meters,  $4\pi$  (meters)<sup>2</sup> perimeter of circle =  $2\pi$ r, area of circle =  $\pi$ r<sup>2</sup> (hint: perimeter =  $\frac{\partial}{\partial r}$  (area))

16π (meters)<sup>2</sup>, <sup>32</sup>/<sub>3</sub>π (meters)<sup>3</sup> surface area of sphere = 
$$4\pi r^2$$
, volume of sphere =  $\frac{4}{3}\pi r^3$  (hint: surface area =  $\frac{\partial}{\partial r}$  (volume))

If you feel comfortable with questions 1A-18A and answered them all correctly on the first try, you may skip questions 1B-18B. If you want more practice or missed any of the previous questions, complete this page of questions. Complete this page entirely before turning to the next page, which contains the answers.

# QUESTION SET B

- 1B) use the quadratic equation to solve  $x^2 + x + 1 = 0$  for x
- 2B) if y = (3-i), what is  $(y^*)(y)$
- 3B) express (5+i)/(1-9i) in the form a+bi
- $4B) \qquad \int\limits_{0}^{2\pi} \sin(x) = ?$
- 5B)  $2^3 \cdot 4 = 2^?$
- 6B) |1+i| = ?
- 7B) |3-i| = ?
- 8B) express 3+4i in  $re^{i\theta}$  form
- 9B) express  $3e^{(i\pi/4)}$  in a+bi form
- 10B) Dimensional analysis: Show that Planck's constant times the speed of light divided by wavelength has units of energy.
- 11B) For small values of  $\theta$ ,  $\sin(\theta) \approx$ ?
- 12B)  $f(x) = (5x^3 + x^{2/3})^4$   $df_{dx} = ?$  (no need to multiply out)
- 13B)  $f(x) = {(1+x)/(x^2-2)}$   ${df/dx} = ?$  (no need to multiply out)
- 14B) simplify  $2e^{3ln2}$
- 15B) find the maximum and minimum of the equation  $f(x) = x^3 48x$  over the range x=-5..+5
- 16B)  $\int_{x=1}^{2} 2x^3 dx = ?$
- 17B)  $\partial/\partial t (8st^{-2} 3s^{-3}t^4)$
- 18B) For objects with a radius of 3 meters, what are the a) circle's perimeter, b) circle's area, c) sphere's surface area, and d) sphere's volume? (express as multiples of  $\pi$ . Include units!)

# **ANSWER SET B**

If you need more practice with differentiation and integrals, check out the worked problems at: http://www.math.ucdavis.edu/~kouba/ProblemsList.html

1B) 
$$\frac{-1}{2} + \frac{i\sqrt{3}}{2}, \frac{-1}{2} - \frac{i\sqrt{3}}{2}$$

- 2B) 10
- $3B) \qquad \frac{-2+23i}{41}$
- 4B) 0
- 5B) 5
- 6B)  $\sqrt{2}$
- 7B)  $\sqrt{10}$
- 8B)  $5e^{atan(4/3)}$
- 9B)  $\frac{3\sqrt{2}}{2} + i\frac{3\sqrt{2}}{2}$
- 10B)  $J \cdot s \cdot m \cdot s^{-1} \cdot m^{-1} = J$
- 11B) θ
- 12B)  $4(5x^3 + x^{2/3})^3 (15x^2 + \frac{2}{3}x^{-1/3})$
- 13B)  $\frac{1}{x^2-2} \frac{2x(1+x)}{(x^2-2)^2}$
- 14B)  $2(e^{\ln 2})^3 = 2 \cdot 2^3 = 2^4 = 16$
- 15B) x = 4 is min, x = -4 is max
- 16B)  $\frac{15}{2}$
- 17B)  $-16st^{-3} 12s^{-3}t^3$
- 18B)  $6\pi$  meters,  $9\pi$  (meters)<sup>2</sup>,  $36\pi$  (meters)<sup>3</sup>