Chem 455 – Homework # 1A Due Monday Oct 2 by noon in Prof. Ginger's mailbox in Bagley

Late homework is not accepted for ANY credit.
Turn in only this front page. Keep the following pages and all of your work for future reference.

This homework set is intended as a quick way for you to test your math skills and refresh them up to the level needed to ***begin*** CHEM 455. Questions of these types will appear in lectures and exams, so treat this seriously. *You will be graded on whether you complete this part of the homework, not on how many questions you answer correctly*.

This homework consists of two "self-tests". Questions appear on one side of the sheet and the answers are on the back. Please try all of the problems in the first self-test before looking at the answers and recording your score below. If you get everything right on the first self-test, then there is no need to do the second one. Most students improve dramatically by the second time through.

Name:_____

Did you get all questions 1A-18A correct on the first try? (circle an answer) YES / NO

Mark an "X" through those questions you got wrong the first time you attempted them.

1A	2A	3A	4A	5A	6A	7A	8A	9A	10A	11A	12A	13A	14A	15A	16A	17A	18A
1B	2B	3B	4B	5B	6B	7B	8B	9B	10B	11B	12B	13B	14B	15B	16B	17B	18B

MATHEMATICS SELF-TUTORIAL, CHEM455

Evaluate and/or simplify the expressions without a calculator. While you are allowed to use a calculator on the homeworks and exams, most students who complain that the exams are "too long" also lose time on "remedial" topics.

Do not convert fractions to decimals. Complete this page entirely before turning to the next page.

QUESTION SET A

1A) use the quadratic equation to solve $2x^2 - x + 8 = 0$ for x

2A) if y = (5+2i), what is $(y^*)(y)$

3A) express (2+3i) / (4-2i) in the form a+bi

4A) $\int_0^{\pi} \sin(x) = ?$

5A) $(a^2bc^{-1})(ab^{-3}) = ?$

6A) |i| = ?

7A) |2-7i| = ?

8A) express 3+3i in $re^{i\theta}$ form

9A) express $2e^{(i\pi/3)}$ in a+bi form

10A) Dimensional analysis: What are the units for angular momentum? Show that Planck's constant has units of angular momentum.

11A) For values of x which are close to 1, $\ln(x) \approx x - 1$. This problem uses a Taylor expansion to show that this is true. Use a Taylor Series to approximate ln(1.05) = ? to first order.

12A) $f(x) = (x^{4/3} - 2x^{-2})^5$ $^{df}/_{dx} = ?$ (no need to multiply out)

13A) $f(x) = (1 - x^4)/x$ $^{df}/_{dx} = ?$ (no need to multiply out)

14A) simplify $e^{2\ln 3}$

15A) find the maximum and minimum of the equation $f(x) = x^3 - 27x$ over the range x=-5..5

16A) $\int_{x=1}^{3} 2x^2 dx = ?$

17A) $\frac{\partial}{\partial x}\left(2x^4y^6 + \frac{3}{x^2}\right) = ?$

18A) For objects with a radius of 2 meters, what are the a) circle's perimeter, b) circle's area, c) sphere's surface area, and d) sphere's volume? (express as multiples of π. Include units!)

Grade questions 1A-17A. Make sure that you understand the answers before turning to the next page.

	ANSWER SET A	REASONS
1A)	$\frac{1+3i\sqrt{7}}{4}, \frac{1-3i\sqrt{7}}{4}$	$x = \frac{-b \pm \sqrt{b^2-4ac}}{2a}$
2A)	29	$(a+bi)(a-bi)=a^2+b^2$
3A)	$\frac{1}{10}+\frac{4}{5}i$	$\frac{a+bi}{c+di} = \frac{a+bi}{c+di}\cdot\left(\frac{c-di}{c-di}\right)$
4A)	2	$\int \sin(x) = -\cos(x)$
5A)	$a^3b^{-2}c^{-1}$	$a^x a^y = a^{x+y}$
6A)	1	$\lvert y\rvert = \sqrt{y^* y}$
7A)	$\sqrt{53}$	$\lvert y\rvert = \sqrt{y^* y}$
8A)	$\sqrt{18}e^{i\pi/4}$	$a+bi=\lvert a+bi\rvert e^{i\ atan(b/a)}$
9A)	$1+i\sqrt{3}$	$e^{i\theta}=\cos(\theta)+i\sin(\theta)$
10A)	$kg\cdot m^2\cdot s^{-1}$	$J\cdot s = N\cdot m\cdot s = kg\cdot m\cdot s^{-2}\cdot m\cdot s = kg\cdot m^2\cdot s^{-1}$
11A)	$\ln(x) = \ln(a) + (x-a)(1/a)$ $\ln(1.05) = 0 + (1.05-1)(1/1) = 0.05$	Taylor Series: $f(x) = f(a) + (x-a)f'(a) + (1/2!)(x-a)^2 f''(a)\ldots$ To first order, for $x \approx 1$, set $a=1$ so that $\ln x \approx (x-1)$
12A)	$5(x^{4/3} - 2x^{-2})^4(^4/_3 x^{1/3} + 4x^{-3})$	for $f(x) = cx^n$, $^{df}/_{dx} = ncx^{n-1}$, where c is a constant
13A)	$-4x^3(^1/_x) + (1-x^4)(-1/x^2)$	$^d/_{dx}(g(x)\cdot h(x)) = (^d/_{dx}g(x))(h(x)) + (g(x))(^d/_{dx}h(x))$ you will make fewer mistakes with the product rule
14A)	$(e^{\ln 3})^2 = (3)^2 = 9$	$e^{\ln x} = x$
15A)	x = 3 is min, x = -3 is max	min occurs at $^{df}/_{dx} = 0$ and $^{d^2f}/_{dx^2} > 0$ max occurs at $^{df}/_{dx} = 0$ and $^{d^2f}/_{dx^2} < 0$
16A)	$\frac{2}{3}x^3\Big\rvert_{x=1}^{3} = \frac{2}{3}(27-1) = \frac{52}{3}$	$\int ax^n dx = \left(\frac{1}{n+1}\right)ax^{n+1} \quad for\ n \neq -1$
17A)	$8x^3y^6 - 6/x^3$	Partial derivatives treat all other variables as constants.
18A)	4π meters, 4π (meters)^2	perimeter of circle = $2\pi r$, area of circle = πr^2 (hint: perimeter = $\frac{\partial}{\partial r}$ (area))
	16π (meters)^2, $^{32}/_3\,\pi$ (meters)^3	surface area of sphere = $4\pi r^2$, volume of sphere = $^4/_3\pi r^3$ (hint: surface area = $\frac{\partial}{\partial r}$(volume))

If you feel comfortable with questions 1A-18A and answered them all correctly on the first try, you may skip questions 1B-18B. If you want more practice or missed any of the previous questions, complete this page of questions. Complete this page entirely before turning to the next page, which contains the answers.

QUESTION SET B

1B) use the quadratic equation to solve $x^2 + x + 1 = 0$ for x

2B) if y = (3-i), what is $(y^*)(y)$

3B) express (5+i) / (1-9i) in the form a+bi

4B) $\int_0^{2\pi} \sin(x) = ?$

5B) $2^3 \cdot 4 = 2^?$

6B) $|1+i| = ?$

7B) $|3-i| = ?$

8B) express 3+4i in $re^{i\theta}$ form

9B) express $3e^{(i\pi/4)}$ in a+bi form

10B) Dimensional analysis: Show that Planck's constant times the speed of light divided by wavelength has units of energy.

11B) For small values of θ, $\sin(\theta) \approx ?$

12B) $f(x) = (5x^3 + x^{2/3})^4$ $\quad {}^{df}/_{dx} = ?$ (no need to multiply out)

13B) $f(x) = {}^{(1+x)}/_{(x^2-2)}$ $\quad {}^{df}/_{dx} = ?$ (no need to multiply out)

14B) simplify $2e^{3\ln 2}$

15B) find the maximum and minimum of the equation $f(x) = x^3 - 48x$ over the range x=-5..+5

16B) $\int_{x=1}^{2} 2x^3 dx = ?$

17B) $\partial/\partial t\ (8st^{-2} - 3s^{-3}t^4)$

18B) For objects with a radius of 3 meters, what are the a) circle's perimeter, b) circle's area, c) sphere's surface area, and d) sphere's volume? (express as multiples of π. Include units!)

ANSWER SET B

If you need more practice with differentiation and integrals, check out the worked problems at:
http://www.math.ucdavis.edu/~kouba/ProblemsList.html

1B) $\frac{-1}{2}+\frac{i\sqrt{3}}{2}, \frac{-1}{2}-\frac{i\sqrt{3}}{2}$

2B) 10

3B) $\frac{-2+23i}{41}$

4B) 0

5B) 5

6B) $\sqrt{2}$

7B) $\sqrt{10}$

8B) $5e^{\text{atan}(4/3)}$

9B) $\frac{3\sqrt{2}}{2}+i\frac{3\sqrt{2}}{2}$

10B) $J \cdot s \cdot m \cdot s^{-1} \cdot m^{-1} = J$

11B) θ

12B) $4(5x^3 + x^{2/3})^3 (15x^2 + {}^2/_3 x^{-1/3})$

13B) $\frac{1}{x^2-2}-\frac{2x(1+x)}{(x^2-2)^2}$

14B) $2(e^{\ln 2})^3 = 2 \cdot 2^3 = 2^4 = 16$

15B) x = 4 is min, x = -4 is max

16B) $\frac{15}{2}$

17B) $-16st^{-3} - 12s^{-3}t^3$

18B) 6π meters, 9π (meters)^2, 36π (meters)^2, 36π (meters)^3