| Why Focus on the DWT?<br>Why Focus on the DWT?<br>• let $\mathbf{X} = [X_0, X_1, \dots, X_{N-1}]^T$ represent a time series<br>• can formulate DWT as an orthonormal transform $\mathcal{W}$ yielding<br>$N$ DWT coefficients $\mathbf{W} = \mathcal{W}\mathbf{X}$ , where $\mathcal{W}^T \mathcal{W} = I_N$<br>• each wavelet coefficient can be interpreted as a difference be-<br>tween localized weighted averages over certain scales<br>• three basic properties of the DWT<br>1. yields additive decomposition (multiresolution analysis)<br>- reexpresses $\mathbf{X}$ as sum of several new time series, each of<br>which is associated with a particular scale (or scales)<br>- starting point for wavelet-based signal extraction<br>2. yields a scale-based analysis of variance (wavelet variance)<br>3. tends to decorrelate certain time series | • oxygen isotope records <b>X</b> from Antarctic ice core<br>$ \begin{array}{c} \overset{-62}{-} & -62$ |
|--|---|























| <ul> <li><b>'2nd Generation' Denoising: III</b></li> <li>Huerta (2005) proposes a Bayesian approach involving a multivariate normal prior with a covariance matrix that accounts for clustering</li> <li><b>'</b>1st generation' denoising also suffers from problem of overall significance of multiple hypothesis tests</li> <li><b>'</b>2nd generation' work integrates idea of 'false discovery rate' (Benjamini and Hochberg, 1995) into denoising (see Wink and Roerdink, 2004, for a recent applications-oriented discussion)</li> </ul> | <ul> <li>A Sampling of Recent Advances: I</li> <li>Aykroyd and Mardia (2003) give a way to describe shape change and shape differences in curves, by constructing a deformation function in terms of a wavelet decomposition</li> <li>Johnstone <i>et al.</i> (2004) propose a deconvolution method involving a combination of fast Fourier and fast wavelet transforms that can recover a blurred function observed in white noise, with application to simulated light detection and ranging data suggested by underwater remote sensing</li> <li>Oh and Li (2004) use a spherical wavelet approach developed for multiscale representation and analysis of scattered data to estimate the entire temperature field for every location on the globe from scattered surface air temperatures observed by a network of weather-stations</li> </ul> |
|---|--|
|---|--|

| References: I   |  |
|---|--|
| • R. G. Aykroyd and K. V. Mardia (2003), 'A Wavelet Approach to Shape Analysis for<br>Spinal Curves,' <i>Journal of Applied Statistics</i> , <b>30</b> (6), pp. 605–23  |  |
| • Y. Benjamini and Y. Hochberg (1995), 'Controlling the False Discovery Rate: A Practical and Powerful Approach to Multiple Testing,' <i>Journal of the Royal Statistical Society, Series B</i> , <b>57</b> , pp. 289300  |  |
| <ul> <li>M. Breakspear, M. J. Brammer, E. T. Bullmore, P. Das and L. M. Williams (2004),<br/>'Spatiotemporal Wavelet Resampling for Functional Neuroimaging Data,' Human Brain<br/>Mapping, 23, pp. 1–25</li> </ul>   |  |
| <ul> <li>E. Bullmore, Chris Long, John Suckling, Jalal Fadili, Gemma Calvert, Fernando Zelaya, T. Adrian Carpenter and Mick Brammer (2001), 'Colored Noise and Computational Inference in Neurophysiological (fMRI) Time Series Analysis: Resampling Methods in Time and Wavelet Domains,' <i>Human Brain Mapping</i>, 12, pp. 61–78</li> </ul> |  |
| • T. Cai and B. W. Silverman (2001), 'Incorporating Information on Neighboring Coefficients into Wavelet Estimation,' <i>Sankhya Series B</i> , <b>63</b> , pp. 127–48  |  |
| <ul> <li>M. S. Crouse, R. D. Nowak and R. G. Baraniuk (1998), 'Wavelet-Based Statistical Signal<br/>Processing Using Hidden Markov Models,' <i>IEEE Transactions on Signal Processing</i>, 46,<br/>pp. 886–902</li> </ul>   |  |
| 32  |  |
| References: II  |  |
| • P. L. Dragotti and M. Vetterli (2003), 'Wavelet Footprints: Theory, Algorithms, and Applications,' <i>IEEE Transactions on Signal Processing</i> , <b>51</b> , pp. 1306–23  |  |
| <ul> <li>P. Fryzlewicz and G. P. Nason (2006), 'Haar-Fisz Estimation of Evolutionary Wavelet<br/>Spectra,' Journal of the Royal Statistical Society: Series B (Statistical Methodology),<br/>68(4), pp. 611–34</li> </ul>   |  |
| <ul> <li>P. Fryzlewicz, S. Van Bellegem and R. Von Sachs (2003), 'Forecasting Non-Stationary Time<br/>Series by Wavelet Process Modelling,' Annals of the Institute of Statistical Mathematics,<br/>55(4), pp. 737–64</li> </ul>  |  |
| • A. Gupta, S. D. Joshi and S. Prasad (2005), 'A New Approach for Estimation of Statistically<br>Matched Wavelet,' <i>IEEE Transactions on Signal Processing</i> , <b>53</b> (5), pp. 1778–93   |  |
| • H.–C. Huang and N. Cressie (2000), 'Deterministic/Stochastic Wavelet Decomposition for Recovery of Signal from Noisy Data,' <i>Technometrics</i> , <b>42</b> , pp. 262–76   |  |
| • G. Huerta (2005), 'Multivariate Bayes Wavelet Shrinkage and Applications,' <i>Journal of Applied Statistics</i> , <b>32</b> (5), pp. 529–42   |  |
| <ul> <li>I. M. Johnstone, G. Kerkyacharian, D. Picard, and M. Raimondo (2004), 'Wavelet De-<br/>convolution in a Periodic Setting,' <i>Journal of the Royal Statistical Society: Series B</i><br/>(Statistical Methodology), 66(3), pp. 547–73</li> </ul>   |  |
| 60 G  |  |