

Figure 1. Haar wavelet filters for scales  $\tau_j = 2^{j-1}, j = 1, 2, ..., 7$ .



**Figure 2.** D(4), C(6) and LA(8) wavelet filters for scales  $\tau_j = 2^{j-1}$ , j = 1, 2, ..., 7.



Figure 3. Haar scaling filters for scales  $\lambda_{J_0} = 2^{J_0}, J_0 = 1, 2, \dots, 7$ .



**Figure 4.** D(4), C(6) and LA(8) scaling filters for scales  $\lambda_{J_0} = 2^{J_0}$ ,  $J_0 = 1, 2, ..., 7$ .



**Figure 5.** LA(8) DWT coefficients for simulated FD(0.4) time series and sample ACSs.



**Figure 6.** SDFs for an FD(0.4) process (top plot) and for nonboundary LA(8) wavelet coefficients in  $\mathbf{W}_1$ ,  $\mathbf{W}_2$ ,  $\mathbf{W}_3$  and  $\mathbf{W}_4$ . The vertical axes are all in units of decibels (i.e., we plot  $\log_{10} (S_X(f))$  versus f). The vertical lines in the top plot denote the nominal pass-bands for the four  $\mathbf{W}_j$ .



**Figure 7.** ACSs at  $\tau = 1, \ldots 4$  for Haar, D(4) and LA(8) wavelet coefficients  $W_{j,t}$ ,  $j = 1, \ldots 4$ , of an FD(0.4) process. The ACS values are plotted as deviations from zero (some are not visible because they are so close to zero).



**Figure 8a.** Correlation between the Haar wavelet coefficients  $W_{j,t}$  and  $W_{j',t'}$  formed from an FD(0.4) process and for levels satisfying  $1 \le j < j' \le 4$ .

$$j' = 2 j' = 3 j' = 4$$

$$j' = 2 j' = 3 j' = 4$$

$$0.2 0.0 j = 1$$

$$0.2 0.0 j = 1$$

$$0.2 0.0 j = 2$$

$$0.0 j = 2$$

$$0.0 j = 2$$

$$0.0 j = 2$$

$$0.0 j = 3$$

$$0.2 0.0 j = 3$$

Figure 8b. As in Figure 8a, but now using the LA(8) DWT.



Figure 9. Simulated FD(0.4) time series X of Figure 5 (bottom panel), above which are five series that were bootstrapped from X using an LA(8) DWT.



Figure 10. SDFs for AR(1) processes (top plot) with  $\phi = 0.9$  (thick curve) and -0.9 (thin) and for corresponding nonboundary LA(8) wavelet coefficients in  $\mathbf{W}_1$  to  $\mathbf{W}_4$  (bottom four plots). The vertical axes are in decibels, and the vertical lines in the top plot denote the nominal pass-bands for the four  $\mathbf{W}_j$ .



Figure 11. Flow diagram illustrating the analysis of **X** into  $\mathbf{W}_{3,0}, \ldots, \mathbf{W}_{3,7}$  (recall that  $N_j \equiv N/2^j$ ).



Figure 12. Flow diagram illustrating the analysis of X into  $\mathbf{W}_{3,0}$ ,  $\mathbf{W}_{3,1}$ ,  $\mathbf{W}_{2,1}$  and  $\mathbf{W}_{1,1}$ , which is identical to a partial DWT of level  $J_0 = 3$ .



Figure 13. Flow diagram illustrating the analysis of X into  $W_{2,0}$ ,  $W_{3,2}$ ,  $W_{3,3}$  and  $W_{1,1}$ , an arbitrary disjoint dyadic decomposition.