

*Measurement, Design, and Analytic Techniques in Mental
Health and Behavioral Sciences*

*Lecture 8 (Feb 6, 2007): SAS Proc MI and Proc
MiAnalyze*

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SAS combining procedures of MI

- The Mianalyze procedure in SAS combines the results of analyses of imputations and generate statistical inferences.
- Syntax

```
PROC MIANALYZE <options>;  
  BY variables;  
  CLASS variables;  
  MODELEFFECTS effects;  
  TEST;  
  STDERR;
```

Summary of Proc MiAnalyze Options

Specific Input data sets

COV, CORR, or EST type data set
parameter estimates and standard errors
parameter estimates
parameter information
covariance matrices
 $(XX')^{-1}$

Options

DATA=
DATA=
PARAMS=
PARMINFO=
COVB=
XPXI=

Specify statistical analysis

parameters under the null hypothesis
level for the confidence interval

THETA0=
ALPHA

Descriptions of other commands

- The statement MODELEFFECTS lists the effects to be analyzed. Variables in this statement that are not specified in a CLASS statement are assumed to be continuous.
- The statement TEST can test the hypothesis about linear combinations of parameters. An F statistics is used to test jointly the null hypothesis ($H_0 : L\beta = 0$) in a single TEST statement.

Example 1, using regression analysis with class

- Combine results from a regression model with continuous covariates

```
proc mi data=MonotoneData noprint out=outmi seed=501213;
  class female;
  monotone reg (mh1 mh2 mh3 mh4/details);
  var  female age mh1 mh2 mh3 mh4 ;
  run;
proc reg data=outmi outest=outreg covout noprint;
  model mh4= age mh1 mh2 mh3;
  by  _imputation_;
  run;
proc mianalyze data=outreg;
  modeleffects Intercept age mh1 mh2 mh3;
  test mh1=mh2=mh3;
  run;
```

Results

Multiple Imputation Parameter Estimates

| Parameter | Estimate | Std Error | 95% Confidence | Limits | DF |
|-----------|-----------|-----------|----------------|----------|--------|
| Intercept | 4.782181 | 0.514103 | 3.77355 | 5.790814 | 1210.3 |
| age | -0.012707 | 0.007356 | -0.02716 | 0.001750 | 432.31 |
| mh1 | 0.098358 | 0.044554 | 0.01092 | 0.185799 | 897.68 |
| mh2 | 0.242225 | 0.043256 | 0.15703 | 0.327418 | 249.34 |
| mh3 | 0.339826 | 0.037684 | 0.26585 | 0.413800 | 788.98 |

Results, cont

Multiple Imputation Parameter Estimates

| Parameter | Minimum | Maximum | Theta0 | t for H0: | |
|-----------|-----------|-----------|--------|------------------|---------|
| | | | | Parameter=Theta0 | Pr > t |
| Intercept | 4.669552 | 4.937240 | 0 | 9.30 | <.0001 |
| age | -0.015818 | -0.010066 | 0 | -1.73 | 0.0848 |
| mh1 | 0.086720 | 0.109104 | 0 | 2.21 | 0.0275 |
| mh2 | 0.220644 | 0.258681 | 0 | 5.60 | <.0001 |
| mh3 | 0.325534 | 0.348182 | 0 | 9.02 | <.0001 |

Results, cont

The MIANALYZE Procedure

Test: Test 1

Test Specification

| Parameter | -----L Matrix----- | | | | | |
|-----------|--------------------|-----|----------|-----------|-----------|---|
| | Intercept | age | mh1 | mh2 | mh3 | C |
| TestPrm1 | 0 | 0 | 1.000000 | -1.000000 | 0 | 0 |
| TestPrm2 | 0 | 0 | 0 | 1.000000 | -1.000000 | 0 |

Results, cont

Multiple Imputation Variance Information

| Parameter | Between | Within | Total | DF |
|-----------|----------|----------|----------|--------|
| TestPrm1 | 0.000473 | 0.004561 | 0.005128 | 326.88 |
| TestPrm2 | 0.000505 | 0.004211 | 0.004817 | 252.71 |

Multiple Imputation Variance Information

| Parameter | Relative Increase in Variance | Fraction Missing Information | Relative Efficiency |
|-----------|-------------------------------|------------------------------|---------------------|
| TestPrm1 | 0.124380 | 0.116014 | 0.977323 |
| TestPrm2 | 0.143919 | 0.132650 | 0.974156 |

SAS Output

Multiple Imputation Parameter Estimates

| Parameter | Estimate | Std Error | 95% Confidence Limits | |
|-----------|-----------|-----------|-----------------------|----------|
| TestPrm1 | -0.143867 | 0.071611 | -0.28474 | -0.00299 |
| TestPrm2 | -0.097602 | 0.069401 | -0.23428 | 0.03908 |

Multiple Imputation Parameter Estimates

t for H0:

| Parameter | Minimum | Maximum | C | Parameter=C | Pr > t |
|-----------|-----------|-----------|---|-------------|---------|
| TestPrm1 | -0.171960 | -0.111540 | 0 | -2.01 | 0.0454 |
| TestPrm2 | -0.127537 | -0.066854 | 0 | -1.41 | 0.1609 |

Mixed-effect regression analysis with class

- Use mixed-effect regression with discrete covariates
- ```
proc mi data=MonotoneData noprint out=outmi seed=501213;
 class male;
 monotone reg (mh1 mh2 mh3 mh4/details);
 var male age mh1 mh2 mh3 mh4 ;
run;

proc mixed data=outmi;
 class male;
 model mh4=male age mh1 mh2 mh3 /solution covb;
 by _imputation_;
 ods output solutionf=mxparms CovB=mxcovb;
run;

proc mianalyze parms=mxparms;
 class male;
 modeleffects Intercept male age mh1 mh2 mh3;
run;
```

# Results

## Multiple Imputation Parameter Estimates

| Parameter | male     | Estimate  | Std Error | 95% Confidence Limits |          | DF     |
|-----------|----------|-----------|-----------|-----------------------|----------|--------|
| Intercept | .        | 4.541591  | 0.548015  | 3.46576               | 5.617417 | 749.76 |
| male      | 0        | 0.307126  | 0.224783  | -0.13375              | 0.747996 | 1760   |
| male      | 1.000000 | 0         | .         | .                     | .        | .      |
| age       | .        | -0.012175 | 0.007360  | -0.02664              | 0.002292 | 436.68 |
| mh1       | .        | 0.096506  | 0.044519  | 0.00914               | 0.183875 | 933.56 |
| mh2       | .        | 0.242102  | 0.043226  | 0.15697               | 0.327234 | 250.3  |
| mh3       | .        | 0.341579  | 0.037700  | 0.26757               | 0.415585 | 774.07 |

# Results

## The MIANALYZE Procedure

### Multiple Imputation Parameter Estimates

| Parameter | male     | Minimum   | Maximum   |
|-----------|----------|-----------|-----------|
| Intercept | .        | 4.394153  | 4.691847  |
| male      | 0        | 0.232033  | 0.351137  |
| male      | 1.000000 | 0         | 0         |
| age       | .        | -0.015273 | -0.009524 |
| mh1       | .        | 0.084952  | 0.107302  |
| mh2       | .        | 0.220599  | 0.258667  |
| mh3       | .        | 0.326980  | 0.349701  |

## Results, cont

### Multiple Imputation Parameter Estimates

| Parameter | male     | Theta0 | t for H0:        |         |
|-----------|----------|--------|------------------|---------|
|           |          |        | Parameter=Theta0 | Pr >  t |
| Intercept | .        | 0      | 8.29             | <.0001  |
| male      | 0        | 0      | 1.37             | 0.1720  |
| male      | 1.000000 | 0      | .                | .       |
| age       | .        | 0      | -1.65            | 0.0988  |
| mh1       | .        | 0      | 2.17             | 0.0304  |
| mh2       | .        | 0      | 5.60             | <.0001  |
| mh3       | .        | 0      | 9.06             | <.0001  |

## A generalized linear model (genmod)

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- This example illustrates the use of a generalized linear model (normal error and identity link function) to analyze imputed data sets and save parameter estimates and corresponding covariate matrices and then combine them to generate statistical inferences.

- $E(Y) = X'\beta$  and  $var(y) = \sigma^2$ , where  $\sigma$  is called the scale parameter.

- ```
proc genmod data=outmi;
    model mh4= age  mh1 mh2 mh3/covb;
    by _Imputation_;
    ods output ParameterEstimates=gmparms  CovB=gmcovb;
run;
proc mianalyze parms=gmparms;
    modeleffects  Intercept  age mh1 mh2 mh3;
run;
```

Results

Multiple Imputation Parameter Estimates

| Parameter | Estimate | Std Error | 95% Confidence Limits | | DF |
|-----------|-----------|-----------|-----------------------|----------|--------|
| Intercept | 4.782181 | 0.512725 | 3.77624 | 5.788121 | 1197.4 |
| age | -0.012707 | 0.007337 | -0.02713 | 0.001713 | 427.88 |
| mh1 | 0.098358 | 0.044435 | 0.01115 | 0.185569 | 888.19 |
| mh2 | 0.242225 | 0.043149 | 0.15724 | 0.327211 | 246.87 |
| mh3 | 0.339826 | 0.037585 | 0.26605 | 0.413605 | 780.68 |

Results, cont

| Parameter | Minimum | Maximum | Theta0 | t for H0: | |
|-----------|-----------|-----------|--------|------------------|---------|
| | | | | Parameter=Theta0 | Pr > t |
| Intercept | 4.669552 | 4.937240 | 0 | 9.33 | <.0001 |
| age | -0.015818 | -0.010066 | 0 | -1.73 | 0.0840 |
| mh1 | 0.086720 | 0.109104 | 0 | 2.21 | 0.0271 |
| mh2 | 0.220644 | 0.258681 | 0 | 5.61 | <.0001 |
| mh3 | 0.325534 | 0.348182 | 0 | 9.04 | <.0001 |

MI with a general linear model (GLM) model

- This example illustrates the use of a generalized linear model to analyze imputed data sets and save parameter estimates and corresponding covariate matrices and then combine them to generate statistical inferences.

- ```
proc glm data=outmi;
 model mh4=age mh1 mh2 mh3/inverse;
 by _Imputation_;
 ods output ParameterEstimates=glmparms
 InvXPX=glmxpxi;

run;

proc mianalyze parms=glmparms;
modeleffects Intercept age mh1 mh2 mh3;
run;
```

# output

## Multiple Imputation Parameter Estimates

| Parameter | Estimate  | Std Error | 95% Confidence Limits |          | DF     |
|-----------|-----------|-----------|-----------------------|----------|--------|
| Intercept | 4.782181  | 0.514103  | 3.77355               | 5.790814 | 1210.3 |
| age       | -0.012707 | 0.007356  | -0.02716              | 0.001750 | 432.31 |
| mh1       | 0.098358  | 0.044554  | 0.01092               | 0.185799 | 897.68 |
| mh2       | 0.242225  | 0.043256  | 0.15703               | 0.327418 | 249.34 |
| mh3       | 0.339826  | 0.037684  | 0.26585               | 0.413800 | 788.98 |

## Output, cont

```

 t for H0:
Parameter Minimum Maximum Theta0 Parameter=Theta0 Pr > |t|
Intercept 4.669552 4.937240 0 9.30 <.0001
age -0.015818 -0.010066 0 -1.73 0.0848
mh1 0.086720 0.109104 0 2.21 0.0275
mh2 0.220644 0.258681 0 5.60 <.0001
```

## An example using a logistic regression

---

- This example illustrates the use of a logistic regression model to analyze imputed data sets and save parameter estimates and corresponding covariate matrices and then combine them to generate statistical inferences.

# SAS Code

---

```
data exam3;
 set example.education6;
 run;
 proc mi data=exam3
 out=outmi seed=501213;
 class npcerad ;
 monotone discrim (npcerad=mmselast npgender educ npdage/details);
 var mmselast npgender educ npdage npcerad ;
 run;
data outmi2;
 set outmi;
 if mmselast <=24 then cogimpair=1;
 else cogimpair=0;
 run; proc logistic data=outmi2;
 model cogimpair= npgender educ npdage npcerad/covb;
 by _imputation_;
 ods output ParameterEstimates=lgsparms Covb=lgcovb;
 run; proc mianalyze parms=lgsparms covb=lgcovb;
 modeleffects npgender educ npdage npcerad;
 run;
```

# SAS Output

## Model Information

```
PARMS Data Set WORK.LGSPARMS
COVB Data Set WORK.LGCOVB
Number of Imputations 5
```

## Multiple Imputation Variance Information

```
-----Variance-----
Parameter Between Within Total DF

npgender 0.009341 0.028195 0.039404 49.431
educ 0.000126 0.000651 0.000802 112.06
npdage 0.000010892 0.000111 0.000124 359.96
npcerad 0.001183 0.004365 0.005784 66.461
```

## SAS Output, cont

---

### Multiple Imputation Variance Information

| Parameter | Relative Increase in Variance | Fraction Missing Information | Relative Efficiency |
|-----------|-------------------------------|------------------------------|---------------------|
| npgender  | 0.397558                      | 0.311760                     | 0.941308            |
| educ      | 0.232945                      | 0.203033                     | 0.960978            |
| npdage    | 0.117837                      | 0.110344                     | 0.978408            |
| npcerad   | 0.325080                      | 0.267058                     | 0.949297            |



## Output, cont

### Multiple Imputation Parameter Estimates

| Parameter | Estimate  | Std Error | 95\% Confidence Limits |          | DF     |
|-----------|-----------|-----------|------------------------|----------|--------|
| npgender  | -0.393643 | 0.198504  | -0.79246               | 0.005178 | 49.431 |
| educ      | 0.132880  | 0.028328  | 0.07675                | 0.189009 | 112.06 |
| npdage    | 0.049236  | 0.011135  | 0.02734                | 0.071133 | 359.96 |
| npcerad   | 1.280466  | 0.076055  | 1.12864                | 1.432296 | 66.461 |

# Output, cont

## Multiple Imputation Parameter Estimates

| Parameter | Minimum   | Maximum   | Theta0 | t for H0:        |         |
|-----------|-----------|-----------|--------|------------------|---------|
|           |           |           |        | Parameter=Theta0 | Pr >  t |
| npgender  | -0.474383 | -0.227524 | 0      | -1.98            | 0.0529  |
| educ      | 0.119974  | 0.150788  | 0      | 4.69             | <.0001  |
| npdage    | 0.046631  | 0.054650  | 0      | 4.42             | <.0001  |
| npcerad   | 1.244445  | 1.326876  | 0      | 16.84            | <.0001  |

## Example on combining correlation coefficients

---

- Fisher's  $z$  transformation of the sample correlation  $r$  is

$$z = \frac{1}{2} \log\left(\frac{1+r}{1-r}\right).$$

The statistic  $z$  is approximately normal with mean

$$\log\left(\frac{1+\rho}{1-\rho}\right)$$

and variance  $1/(n-3)$ . Here  $\rho$  is the population correlation, and  $n$  is the sample size.

# SAS Code

---

```
proc corr data=outmi fisher (biasadj=no);
 var mh2 mh3;
 by _imputation_;
 ods output FisherPearsonCorr = outz;
run;
```

```
data outz;
 set outz;
 StdZ=1./sqrt(Nobs-3);
run;
```

```
proc mianalyze data=outz;
 ods output ParameterEstimates=parms;
 modeleffects Zval;
 stderr stdZ;
run;
```